

$$\mathbb{R}^n \times_n \mathbb{R} \overset{\nabla}{\infty} \mathbb{C}$$

$$\mathbb{R}^n \times_n \mathbb{R} \overset{\nabla}{\infty} \mathbb{C} \xleftarrow{\begin{matrix} \text{() \\ \text{symp} \text{ FT} \end{matrix}} \mathbb{R}^n \times_n \mathbb{R} \overset{\nabla}{\infty} \mathbb{C}$$

$${}_{y|\eta} \overset{\nabla}{F} = \int_{dx} \int_{d\xi}^{\mathbb{R}^n \ n\mathbb{R}} {}_{x|\xi} F \exp i \underline{y|\xi - x|\eta} \text{ symp Fourier}$$

$$\overset{\nabla}{F}^\vee = F$$

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$${}_{y|\eta} \hat{F} = \int_{dx} \int_{d\xi}^{\mathbb{R}^n \ n\mathbb{R}} {}_{x|\xi} F \exp i \underline{y|x + \xi|\eta} \text{ orth Fourier}$$

$$\hat{F}^\wedge = F \circ (-I)$$

$$\mathcal{W}(F) = \int_{dy} \int_{d\eta}^{\mathbb{R}^n \ n\mathbb{R}} {}_{y|\eta} \overset{\nabla}{F} \exp i \underline{Q|\eta - y|P}$$

$${}^x \overline{\mathcal{W}(F) \phi} = \int_{dy} \int_{d\eta}^{\mathbb{R}^n \ n\mathbb{R}} {}_{x \frac{1}{2} y|\eta} F \exp i \underline{x - y|\eta} {}^y \phi$$

$$\mathcal{W}(F_1) \mathcal{W}(F_2) = \mathcal{W}(F_1 \# F_2)$$

$${}_{x|\xi} \overline{F_1 \# F_2} = \sum \frac{1}{\alpha! \beta!} \partial_x^\alpha \partial_\xi^\beta F_1 \partial_x^\beta \partial_\xi^\alpha F_2$$

$${}_{x\xi} \overline{h_1 \# h_2} = {}_{y\eta} h_1 {}_{z\zeta} h_2 \exp \left( -2i \left[ \begin{matrix} y - x & \eta - \xi \\ -1 & 0 \end{matrix} \middle| \begin{matrix} 0 & 1 \\ -1 & 0 \end{matrix} \right] \begin{bmatrix} z - x \\ \zeta - \xi \end{bmatrix} \right) = e^{i\mathcal{L}} (h_1 \# h_2) (x\xi | x\xi)$$

$$\mathcal{L} = \frac{\partial}{\partial z^j} \frac{\partial}{\partial \eta_j} - \frac{\partial}{\partial y^j} \frac{\partial}{\partial z_j}$$