

$$A \in \overline{\overline{\mathcal{PO} \cup \overline{X}}} \xrightarrow{\text{equiv}} \overline{\overline{\mathcal{PO} \cup \overline{X}}} / \sim \ni \overline{A} \text{ Boole Alg}$$

$$A \sim B \Leftrightarrow \overline{A} = \overline{B} \Leftrightarrow 1 = \begin{cases} \overline{A \rightarrow B} \\ \overline{B \rightarrow A} \end{cases} \Leftrightarrow \text{ableitbar } \overline{\overline{\overline{\mathcal{PO} \cup \overline{X}}}} \ni \begin{cases} A \rightarrow B \\ B \rightarrow A \end{cases}$$

$$\overline{A} \leq \overline{B} \Leftrightarrow \overline{A \rightarrow B} = 1 \Leftrightarrow \underline{A \rightarrow B} \text{ ableitbar}$$

$$\overline{A} = 1 \Leftrightarrow A \in \overline{\overline{\overline{\mathcal{PO} \cup \overline{X}}}} \text{ ableitbar}$$

$$\overline{A} \leq \overline{B} \Rightarrow \overline{\gamma \circ A} \leq \overline{\gamma \circ B}$$

$$A \sim B \Rightarrow \gamma \circ A \sim \gamma \circ B$$

Ableitung $A_1 | \cdot | A_n | \underline{A \rightarrow B}$

$$R_1 \ni \underline{A \rightarrow B} | \overline{\gamma \circ \underline{A \rightarrow B}}$$

$$\Rightarrow \text{Ableitung } A_1 | \cdot | A_n | \underline{A \rightarrow B} | \overline{\gamma \circ \underline{A \rightarrow B}} = \underline{\gamma \circ A} \rightarrow \underline{\gamma \circ B}$$

$$\overline{\bigwedge_x A} \stackrel{=}{=} \bigwedge_{t \neq x} \overline{l_x^t \circ A} : \overline{\bigvee_x A} \stackrel{=}{=} \bigvee_{t \neq x} \overline{l_x^t \circ A}$$

$$\overline{\bigwedge_x A} \rightarrow \overline{l_x^t \circ A} \in R_0 \Rightarrow \text{unt Schranke } \overline{\bigwedge_x A} \leq \overline{l_x^t \circ A}$$

$$\text{unt Schranke } \overline{B} \leq \overline{l_x^t \circ A} \Rightarrow \bigwedge_{t \neq x} \overline{B \rightarrow l_x^t \circ A} \in \overline{\overline{\overline{\mathcal{PO} \cup X}}}$$

$$x \neq y \in X \vdash [A \cup B] \Rightarrow y \neq x \Rightarrow \overline{B \rightarrow l_x^y \circ A} \in \overline{\overline{\overline{\mathcal{PO} \cup X}}} \Rightarrow \text{Abl } A_1 | \dots | A_n | \overline{B \rightarrow l_x^y \circ A}$$

$$\overline{B \rightarrow l_x^y \circ A} | \overline{B \rightarrow \bigwedge_x A} \in R_1 \Rightarrow \text{Abl } A_1 | \dots | A_n | \overline{B \rightarrow l_x^y \circ A} | \overline{B \rightarrow \bigwedge_x A}$$

$$\Rightarrow \overline{B \rightarrow \bigwedge_x A} \in \overline{\overline{\overline{\mathcal{PO} \cup X}}} \Rightarrow \overline{B} \leq \overline{\bigwedge_x A} \text{ grosste unt Schranke}$$

$$\overline{\bigvee_x A} \rightarrow \overline{\bigwedge_x \bar{A}} \in R_0 \ni \overline{\bigwedge_x \bar{A}} \rightarrow \overline{\bigvee_x A}$$

$$\Rightarrow \overline{\bigvee_x A} = \overline{\neg \bigwedge_x \bar{A}} = \neg \overline{\bigwedge_x \bar{A}} = \neg \bigwedge_{t \neq x} \overline{l_x^t \circ \bar{A}} = \bigvee_{t \neq x} \overline{\neg l_x^t \circ \bar{A}} = \bigvee_{t \neq x} \overline{l_x^t \circ \neg \bar{A}} = \bigvee_{t \neq x} \overline{l_x^t \circ A}$$