

$$\text{Banach } \overset{\delta}{\Delta}_0 \ni \underset{\text{voll}}{\mathfrak{H}} \xrightarrow[q \text{ contr}]{\mathcal{L}} \mathfrak{H} \Rightarrow \bigvee_{o \in \mathfrak{H}} \begin{cases} \overset{o}{\mathcal{L}} = o \\ \mathfrak{H} \Big|_{\mathcal{L}} = o \end{cases}$$

$$\text{Eind : } \overset{o}{\mathcal{L}} = \dot{o} \Rightarrow o | \dot{o} = \overset{o}{\mathcal{L}} \mid \overset{\dot{o}}{\mathcal{L}} \leq q o | \dot{o} \Rightarrow o | \dot{o} = 0 \Rightarrow o = \dot{o}$$

$$\text{Ex : } \mathfrak{H} \ni \mathfrak{h} \text{ bel } \mathbb{N} \xrightarrow[\text{folg}]{\overset{\mathfrak{h}}{\mathcal{L}}} \mathfrak{H} : \overset{\mathfrak{h}}{\mathcal{L}} = \overset{\mathfrak{h} \circ \mathfrak{h} \circ \mathfrak{h} \circ \mathfrak{h}}{\mathcal{L}} \begin{cases} \overset{\mathfrak{h}^0}{\mathcal{L}} = \mathfrak{h} & n = 0 \\ \overset{\mathfrak{h}^{n+1}}{\mathcal{L}} = \overset{\mathfrak{h}}{\mathcal{L}} \overset{\mathfrak{h}^n}{\mathcal{L}} & 0 \leq n \circlearrowright n+1 \end{cases}$$

$$\overset{\mathfrak{h}^n}{\mathcal{L}} \mid \overset{\mathfrak{h}^{n+1}}{\mathcal{L}} \leq q^n \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}}$$

$$n \circlearrowright n+1 : \overset{\mathfrak{h}^{n+1}}{\mathcal{L}} \mid \overset{\mathfrak{h}^{n+2}}{\mathcal{L}} \leq q \underbrace{\overset{\mathfrak{h}^n}{\mathcal{L}} | \overset{\mathfrak{h}^{n+1}}{\mathcal{L}}}_{\text{ind}} \leq q q^n \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}} = q^{n+1} \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}}$$

$$\overset{\mathfrak{h}}{\mathcal{L}} \underset{\text{Cau}}{\rightsquigarrow}$$

$$\bigwedge_{\varepsilon} \bigvee_{\ell}^{>0} q^\ell \leq \varepsilon \frac{1-q}{\mathfrak{h} | \mathfrak{h}}$$

$$\bigwedge_{\ell \leq m < n} \overset{\mathfrak{h}^m}{\mathcal{L}} \mid \overset{\mathfrak{h}^n}{\mathcal{L}} \leq \overset{\mathfrak{h}^m}{\mathcal{L}} \mid \overset{\mathfrak{h}^{m+1}}{\mathcal{L}} + \overset{\mathfrak{h}^{m+1}}{\mathcal{L}} \mid \overset{\mathfrak{h}^{m+2}}{\mathcal{L}} + \dots + \overset{\mathfrak{h}^{n-1}}{\mathcal{L}} \mid \overset{\mathfrak{h}^n}{\mathcal{L}}$$

$$\leq q^m \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}} + q^{m+1} \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}} + \dots + q^{n-1} \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}}$$

$$= q^m \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}} \underbrace{1 + q + \dots + q^{n-m}}_{\mathfrak{h}} \leq q^m \underbrace{\mathfrak{h} | \mathfrak{h}}_{\mathfrak{h}} \underbrace{1 + q + \dots}_{\mathfrak{h}} = q^m \frac{\mathfrak{h} | \mathfrak{h}}{1-q} \leq q^\ell \frac{\mathfrak{h} | \mathfrak{h}}{1-q} \leq \varepsilon$$

$$\mathfrak{H} \text{ voll} \Rightarrow \overset{\mathfrak{h}^n}{\mathcal{L}} \underset{\text{stet}}{\rightsquigarrow} o \in \mathfrak{H} \Rightarrow \overset{o}{\mathcal{L}} \underset{\substack{\rightsquigarrow \\ \mathfrak{h} = n+1}}{\mathfrak{h}^n \mathcal{L} = \mathfrak{h}^{n+1}} \rightsquigarrow o \Rightarrow \overset{o}{\mathcal{L}} = o$$