

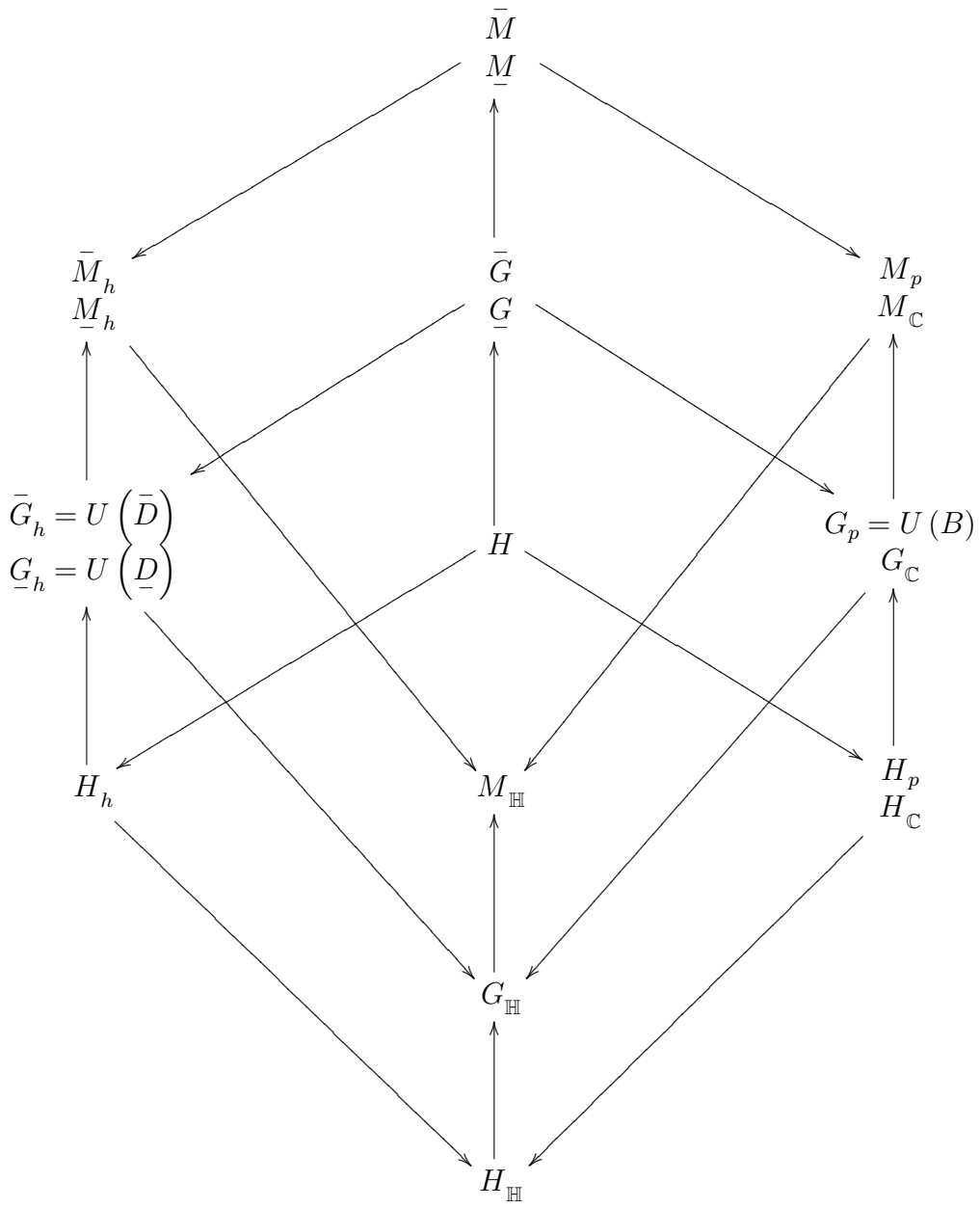
$$G/H = \frac{q \in G}{jqj^* = q^{-1}}$$

$$G \ni g \Rightarrow g^* j g = j$$

$$U \ni g \Rightarrow g^* g = 1$$

$$j_z = 1 + 2j^* z j = \overbrace{j^{-1} z}^{-1} j + z = j_{-z}^{-1}$$

$$j^* z = -z^* j \Rightarrow \begin{cases} j j_z^* j^* = j_{-z} \\ j_z^* = j_{-z}^* \end{cases}$$



$$j \underbrace{j+z}_{-1} j + \underbrace{j^{-1} + z^{-1}}_{-1} = j$$

$$j^{-1} + z^{-1} = j^{-1} + z^{-1} j^{-1} = z^{-1} j^{-1} + j^{-1} = z^{-1} \underbrace{j+z}_{-1} j^{-1}$$

$$\Rightarrow \underbrace{j^{-1} + z^{-1}}_{-1} = j \underbrace{j+z}_{-1} z = j \underbrace{j+z}_{-1} \underbrace{j+z-j}_{-1} = j - j \underbrace{j+z}_{-1} j$$

$${}^z \mathbf{c} = j \underbrace{j+z}_{-1} \underbrace{j-z}_{-1} = 2j \underbrace{j+z}_{-1} j - j = 2j \tilde{j}^{-z} j - j$$

$$j \underbrace{j+z}_{-1} \underbrace{j-z}_{-1} = -j \underbrace{j+z}_{-1} \underbrace{z-j}_{-1} = -j \underbrace{j+z}_{-1} \underbrace{z+j-2j}_{-1} = -j + 2j \underbrace{j+z}_{-1} j$$

$$\tilde{j}^{-z} = \underbrace{1+\tilde{j}z}_{-1} \tilde{j} = \underbrace{\tilde{j}j+\tilde{j}z}_{-1} \tilde{j} = \underbrace{\tilde{j} \overbrace{j+z}^{-1}}_{-1} \tilde{j} = \underbrace{j+z}_{-1} \Rightarrow j \tilde{j}^{-z} j = j \underbrace{j+z}_{-1} j$$

$$\tilde{\mathbf{c}}^{-1} = \mathbf{c}$$

$${}^z \mathbf{c} + j = 2j \underbrace{j+z}_{-1} \mathbf{c} j = 2j \underbrace{2j \overbrace{j+z}^{-1}}_{-1} j = \underbrace{j \overbrace{j+z}^{-1}}_{-1} j = j + z$$

$${}^w \mathbf{c}^{-1} = \underbrace{j-w}_{-1} \underbrace{j+w}_{-1} j^{-1} = 2 \underbrace{j-w}_{-1} - j^{-1}$$

$$\underbrace{j-w}_{-1} \underbrace{j+w}_{-1} j^{-1} = - \underbrace{w-j}_{-1} \underbrace{w+j}_{-1} j^{-1} = - \underbrace{w-j}_{-1} \underbrace{w-j+2j}_{-1} j^{-1} = - j^{-1} - 2 \underbrace{w-j}_{-1} = 2 \underbrace{j-w}_{-1} - j^{-1}$$

$$\begin{cases} \overline{z+w} = \tilde{z} + \tilde{w} \\ \tilde{z}^{-1} = \tilde{z}^{-1} \sim \\ \overline{xyx} = \tilde{x} \tilde{y} \tilde{x} \end{cases}$$

$$\tilde{z}z = 1 = \tilde{j}j \Rightarrow {}^z\tilde{\mathbf{c}}j = -\tilde{j}{}^z\mathbf{c}$$

$$\begin{aligned} {}^z\mathbf{c} &= 2j \underbrace{j+z}_{-1} j - j = 2 \underbrace{j \underbrace{j+z}_{-1} j - j}_{-1} + j = j - 2 \underbrace{j^{-1} + z^{-1}}_{-1} = j - 2 \underbrace{\tilde{j} + \tilde{z}}_{-1} \\ \Rightarrow {}^z\tilde{\mathbf{c}} &= \tilde{j} - 2 \underbrace{j+z}_{-1} \Rightarrow {}^z\tilde{\mathbf{c}}j = \tilde{j}j - 2 \underbrace{j+z}_{-1} j = 1 - 2 \underbrace{j+z}_{-1} j \\ \tilde{j}{}^z\mathbf{c} &= 2 \tilde{j}j \underbrace{j+z}_{-1} j - \tilde{j}j = 2 \underbrace{j+z}_{-1} j - 1 \end{aligned}$$

$$\tilde{w}j = -\tilde{j}w \Rightarrow {}^w\tilde{\mathbf{c}} = {}^w\mathbf{c}^{-1}$$

$$\begin{aligned} \underbrace{\tilde{j} + \tilde{w}j}_{-1} &= 1 + \tilde{w}j = 1 - \tilde{j}w = \tilde{j} \underbrace{j-w}_{-1} \Rightarrow \underbrace{j-w}_{-1} = j \underbrace{\tilde{j} + \tilde{w}j}_{-1} \Rightarrow \underbrace{j-w}_{-1} = \tilde{j} \underbrace{\tilde{j} + \tilde{w}}_{-1} \tilde{j} \\ \Rightarrow {}^w\tilde{\mathbf{c}} &= \underbrace{2j \underbrace{j+\tilde{w}j}_{-1} j - j}_{-1} = 2 \tilde{j} \underbrace{\tilde{j} + \tilde{w}}_{-1} \tilde{j} - \tilde{j} = 2 \underbrace{j-w}_{-1} - \tilde{j} = {}^w\mathbf{c}^{-1} \end{aligned}$$

$$\tilde{w}j = \tilde{j}w \Rightarrow j{}^w\tilde{\mathbf{c}} = {}^w\mathbf{c} \tilde{j}$$

$$\begin{aligned} j \underbrace{\tilde{j} + \tilde{w}}_{-1} &= 1 + j\tilde{w} = 1 + w\tilde{j} = \underbrace{j+w}_{-1} \tilde{j} \Rightarrow j \underbrace{j+w}_{-1} = \underbrace{\tilde{j} + \tilde{w}}_{-1} \tilde{j} \\ \Rightarrow {}^w\mathbf{c} \tilde{j} &= 2j \underbrace{j+w}_{-1} - 1 = 2 \underbrace{\tilde{j} + \tilde{w}}_{-1} \tilde{j} - 1 = j{}^w\tilde{\mathbf{c}} \end{aligned}$$

$${}^n\mathbb{K}_n \xrightarrow{\mathbf{c}} {}^n\mathbb{K}_n$$

$$\mathbf{U} \qquad \qquad \mathbf{U}$$

$${}^n\mathbb{K}_n^{\mathbf{U}} \xrightarrow{\mathbf{c}} {}^n\mathbb{K}_n^{\mathbf{U}}$$

$${}^n\mathbb{K}_n^{\mathbf{c}} \ni z$$

$$j = 1$$

$$\tilde{z} = \tilde{z}^*$$

$${}^z\mathbf{c} = \underbrace{1+z}_{-1} \underbrace{1-z}$$

$${}^w\mathbf{c} = -w \Leftrightarrow w^* \mathbf{c} w = 1$$

$$V = {}^n\mathbb{K}_n^{\mathbb{C}} = \begin{cases} {}^n\mathbb{R}_n^{\mathbb{C}} \\ {}^n\mathbb{C}_n^{\mathbb{C}} \\ {}^n\mathbb{H}_n^{\mathbb{C}} \end{cases}$$

$$\overset{\beta}{\Gamma} = \overset{*}{\Gamma}$$

$$e \in V^{\beta} = {}^n\mathbb{K}_n^{\psi} = \begin{cases} {}^n\mathbb{R}_n^{\psi} \\ {}^n\mathbb{C}_n^{\psi} \\ {}^n\mathbb{H}_n^{\psi} \end{cases}$$

$$V_{\beta} = {}^n\mathbb{K}_n^{\vartheta} = \begin{cases} {}^n\mathbb{R}_n^{\vartheta} \\ {}^n\mathbb{C}_n^{\vartheta} \\ {}^n\mathbb{H}_n^{\vartheta} \end{cases}$$

$$M = {}^n\mathbb{K}_n^{\mathbb{U}} = \begin{cases} {}^n\mathbb{R}_n^{\mathbb{U}} \\ {}^n\mathbb{C}_n^{\mathbb{U}} \\ {}^n\mathbb{H}_n^{\mathbb{U}} \end{cases} \quad \text{group case}$$

$$\begin{array}{ccc} {}^n\mathbb{K}_n^{\mathbb{C}} & \xrightarrow{\mathbf{c}} & {}^n\mathbb{K}_n^{\mathbb{C}} \\ \uparrow & & \uparrow \\ {}^n\mathbb{K}_n^{\vartheta} & \xrightarrow{\mathbf{c}} & {}^n\mathbb{K}_n^{\mathbb{U}} \end{array}$$

$${}^z\mathbf{c} = e^z \tilde{e} \underbrace{e-z}_{-1} = \underbrace{1-e\tilde{z}^*}_{-1} e \tilde{e} \underbrace{e-z}_{-1} = \underbrace{e-\tilde{z}^*}_{-1} \underbrace{e-z}_{-1}$$

$$\tilde{y}^* = -y \Rightarrow {}^y\mathbf{c} = \underbrace{e+y}_{-1} \underbrace{e-y}_{-1}$$

$$1 - {}^z \mathbf{c} {}^w \mathbf{c}^* = 2 \underbrace{\frac{e+z}{-1}} \underbrace{z-w} \underbrace{\frac{e-w}{-1}}$$

$$1 - {}^z \mathbf{c} {}^w \mathbf{c}^* \Delta = 2^r \frac{e+z}{-1} \Delta^{-1} \frac{z-w}{-1} \Delta \frac{e-w}{-1} \Delta^{-1}$$

$$\begin{aligned} & \underbrace{1 - \frac{e+z}{-1} \frac{e-z}{-1} \overbrace{\frac{e+w}{-1} \frac{e-w}{-1}}^*}_{-1} = \overbrace{1 - \frac{e+z}{-1} \frac{e-z}{-1} \frac{e+w}{-1} \frac{e-w}{-1}} \\ & = \frac{e+z}{-1} \overbrace{\left(\frac{e+z}{-1} \frac{e-w}{-1} - \frac{e-z}{-1} \frac{e+w}{-1} \right)} \frac{e-w}{-1} = 2 \frac{e+z}{-1} \frac{z-w}{-1} \frac{e-w}{-1} \end{aligned}$$