

$$\mathbb{Z} \subset \mathbb{Z}_{\mathbb{C}}$$

$$r_{\mathbb{C}} = r: \quad a_{\mathbb{C}} = 2a$$

$$\mu_{\mathbb{C}} = 2\mu: \quad \nu_{\mathbb{C}} = \nu/2$$

$${}_x\Phi_{\mathbb{C}}^{2\mu} = {}_{x^2}\Phi^{\mu}$$

$$\Phi_{\mathbb{C}}^{2\mu} \star \Phi_{\mathbb{C}}^{2\mu} = \frac{2^{2|\mu|}}{d_X^{\mu}} (d_X/r)_{\mu} (d_Z/2r)_{\mu}$$

$$\frac{\Phi_{\mathbb{C}}^{2\mu} \star \Phi_{\mathbb{C}}^{2\mu}}{\Phi_{\mathbb{C}}^{2\mu} \star \Phi_{\mathbb{C}}^{2\mu}} = \frac{\Gamma_{\nu+2\mu}^{\mathbb{C}}}{\Gamma_{\nu}^{\mathbb{C}}} = \prod_j \frac{\Gamma_{\nu+2\mu_j - a_{\mathbb{C}}(j-1)/2}}{\Gamma_{\nu - a_{\mathbb{C}}(j-1)/2}}$$

$$= \prod_j \frac{\Gamma_{\nu+2\mu_j - a(j-1)}}{\Gamma_{\nu - a(j-1)}} = \prod_j \frac{\Gamma_{2(\nu/2 + \mu_j - a(j-1)/2)}}{\Gamma_{2(\nu/2 - a(j-1)/2)}}$$

$$= \prod_j \frac{2^{2\mu_j} \Gamma_{\nu/2 + \mu_j - a(j-1)/2} \Gamma_{1/2 + \nu/2 + \mu_j - a(j-1)/2}}{\Gamma_{\nu/2 - a(j-1)/2} \Gamma_{1/2 + \nu/2 - a(j-1)/2}} = 2^{2|\mu|} \left(\frac{\nu}{2}\right)_{\mu} \left(\frac{\nu+1}{2}\right)_{\mu}$$