$$\begin{split} G_{\mathbb{R}} &= \frac{g \in G_{\mathbb{C}}}{g\left(z^{\sharp}\right) = \left(gz\right)^{\sharp}} \\ K_{\mathbb{R}} &= G_{\mathbb{R}} \ \cap \ K_{\mathbb{C}} \end{split}$$