

$$\mathfrak{G} |_{\mathfrak{U}} \mathbb{I} = \mathfrak{G}_1 |_{\mathfrak{U}} \mathbb{I} \times \mathfrak{G}_- |_{\mathfrak{U}} \mathbb{I}$$

$$\mathfrak{G} |_{\mathfrak{O}} \mathbb{I} = \mathfrak{G}_1 |_{\mathfrak{O}} \mathbb{I} \times \mathfrak{G}_> |_{\mathfrak{O}} \mathbb{I} \times \mathfrak{G}_< |_{\mathfrak{O}} \mathbb{I} \xrightarrow{\text{exp}} \mathfrak{G}_1 |_{\mathfrak{O}} \mathbb{I} \times \mathfrak{G}_> |_{\mathfrak{O}} \mathbb{I} \times \mathfrak{G}_< |_{\mathfrak{O}} \mathbb{I} \underset{\text{hull}}{\subset} \mathfrak{G} |_{\mathfrak{O}} \mathbb{I}$$

$$\mathfrak{G} |_{\mathfrak{O}} \mathbb{I} = \mathfrak{G}_1 |_{\mathfrak{O}} \mathbb{I} \times \mathfrak{G}_- |_{\mathfrak{O}} \mathbb{I}$$

$$\mathfrak{G}_1 |_{\mathfrak{U}} \mathbb{I} = \frac{L \mathbb{I} \partial_L}{L \in \mathfrak{G} |_{\mathbb{I}}} = \frac{L \mathbb{I}^* - L \mathbb{I}^* \mathbb{I} \partial_L}{\mathbb{I} \in \mathbb{I}} = \mathfrak{G} |_{\mathbb{I}}$$

$$\mathfrak{G}_- |_{\mathfrak{U}} \mathbb{I} = \frac{\mathbb{I} - L \mathbb{I}^* \partial_L}{L \in \mathbb{I}}$$

$$\mathfrak{G}_- |_{\mathfrak{E}} \mathbb{I} \text{ weights of } \mathfrak{K} S_0$$

$$S_0 \in \mathfrak{U} |_{\mathfrak{U}} \mathbb{I}$$

$$\mathfrak{G}_> |_{\mathfrak{O}} \mathbb{I} = \frac{\mathbb{I} \partial_L}{\mathbb{I} \in \mathbb{I}} = \mathbb{I} = \langle \mathfrak{U}(\mathbb{I}) \rangle_{-2\varrho_n}$$

$$\mathfrak{G}_< |_{\mathfrak{O}} \mathbb{I} = \frac{L \mathbb{I}^* \partial_L}{\mathbb{I} \in \mathbb{I}} = \mathbb{I}^\# = \langle \mathfrak{U}(\mathbb{I}) \rangle_{2\varrho_n}$$

$$\mathfrak{G}^{0:\pm i} |_{\mathfrak{O}} \mathbb{I} \lambda \text{ weights of } iL \partial_L \mathfrak{K} \in \mathfrak{G} |_{\mathfrak{U}} \mathbb{I}$$

$$\left( \mathfrak{b}_{-i} + \mathfrak{b}_0 + \mathfrak{b}_i \right) \underset{\text{refl}}{\ast} = -\mathfrak{b}_{-i} + \mathfrak{b}_0 - \mathfrak{b}_i$$

$$\overbrace{\mathbb{I} + L \mathbb{I} + L \mathbb{I}^* \mathbb{I}}^{\ast} \underset{\text{inv}}{=} \mathbb{I} + L \mathbb{I} + L \mathbb{I}^* \mathbb{I}$$

$$\underline{a - z \check{a} z} \partial_z \ast \underline{b - z \check{b} z} \partial_z = 2 \underline{z \check{a} b - z \check{b} a} \partial_z$$

$$\underline{a - z \check{a} z} \partial_z \ast \underline{z \check{b} c - z \check{c} b} \partial_z = X_{\underline{abc - a \check{c} b}}$$

$$\underline{\check{v} w} \ast \delta = \check{v} \underline{w \delta} + \underline{\check{v} \delta} w$$

$$\underline{u \delta - z \check{u} \delta} \partial_z = \underline{u - z \check{u} z} \partial_z \ast \delta = u \delta - \underline{z \check{u} z} \delta + \underline{z \delta} \check{u} z + z \check{u} \underline{z \delta} \Rightarrow$$

$$\underline{z \check{u} z} \delta = z \check{u} \underline{z \delta} + z \underline{\check{u} \delta} z + \underline{z \delta} \check{u} z \Rightarrow \underline{u \check{v} w} \delta = u \check{v} \underline{w \delta} + u \underline{\check{v} \delta} w + \underline{u \delta} \check{v} w \Rightarrow \underline{\check{v} w} \ast \delta = \check{v} \underline{w \delta} + \underline{\check{v} \delta} w$$

$$\underline{\check{b} c} \ast i \underline{\check{u} u} = \check{b} \underline{i \check{c} u} + i \underline{\check{b} u} c \Rightarrow \underline{\check{b} c} \ast \underline{\check{a} d} = \check{b} \underline{\check{c} a d} - \underline{\check{a} d} b c$$

$$\underline{z \check{b} c} \check{a} d - \underline{z \check{a} d} \check{b} c = z \check{b} \underline{\check{c} a d} - z \underline{\check{a} d} b c$$

$$\underline{z^* a d} \times \underline{z^* b z} = z \overbrace{a d b}^* z$$

$$\underline{z^* a d} \times \underline{z^* b z} = \underline{z^* a d} \overset{*}{b} z + z \overset{*}{b} \underline{z^* a d} - \underline{z^* b z} \overset{*}{a} d = z \overbrace{a d b}^* z$$

$$z = c$$

$$\mathfrak{b} \times \mathfrak{t} = \mathfrak{R} \underbrace{\mathfrak{X}_b \times \mathfrak{X}_t}_{\mathfrak{X}_c} \Rightarrow X_a \times X_b = 4p\mathfrak{R}a \times b$$

$$\text{symm } X_a \times X_a = 4p\mathfrak{R}a \times a$$

$$\text{K-inv } a = \sum_k \lambda^k e_k \Rightarrow \text{root deco}$$