

$$\zeta E_{w_1^z - w_2^z}^\mu = \zeta_{z^g} E_{\overline{w_1^g}^{w_1^g} - \overline{w_2^g}^{w_2^g}}^\mu$$

$$\overline{0 \cdot \underline{\dot{g}}^*}^w + w^w = \overline{w^g}^{wg} w_{\underline{\dot{g}}^*} \xRightarrow{\text{pol}} \overline{0 \cdot \underline{\dot{g}}^*}^z + w^z = \overline{w^g}^{zg} z_{\underline{\dot{g}}^*} \Rightarrow w_1^z - w_2^z = \overline{w_1^g}^{w_1^g} - \overline{w_2^g}^{w_2^g} z_{\underline{\dot{g}}^*}$$

$$\text{LHS} = \zeta E_{\overline{w_1^g}^{w_1^g} - \overline{w_2^g}^{w_2^g} z_{\underline{\dot{g}}^*}}^\mu = \text{RHS}$$

$$\zeta \overline{\mathbf{t}_{z^w} \mathbf{1}} = \zeta + z^w \mathbf{1}$$

$$\begin{array}{ccccc} Z_{\Delta} \overline{\mathbb{C}} \mathbf{x} T^{-n-\nu} & \xrightarrow[\underline{z \Delta_w}]{z U G_w^{n-}} & Z_{\Delta} \overline{\mathbb{C}} \mathbf{x} T^{-n-\nu} & \xleftarrow{\mathbf{t}_{z^w}} & Z_{\Delta} \overline{\check{\mathbb{C}}} \mathbf{x} T^{-\nu} \\ \uparrow \begin{array}{l} z g^{n-} \\ U T g^{-n-\nu} \end{array} & & \downarrow \begin{array}{l} w g^{n-} \\ U T g^{*- \nu} \end{array} & & \downarrow \begin{array}{l} w g^{* \nu} \\ K T g^{*- \nu} \end{array} \\ Z_{\Delta} \overline{\mathbb{C}} \mathbf{x} T^{-n-\nu} & \xrightarrow[\underline{z g G_{wg}^{n-}}]{z g U G_{wg}^{n-}} & Z_{\Delta} \overline{\mathbb{C}} \mathbf{x} T^{-n-\nu} & \xleftarrow{\mathbf{t}_{z g^{wg}}} & Z_{\Delta} \overline{\check{\mathbb{C}}} \mathbf{x} T^{-\nu} \end{array}$$

$$w g^{n-} \mathbf{t}_{z^w} \mathbf{1} = w g^{*-n} \mathbf{t}_{z g^{wg}} \overline{w g^{* \nu} \mathbf{1}}$$

$$\overline{z g^{wg}}_K w g^{* \nu} = z g \mathbf{t}_{-wg}^* w g^{* \nu} = z \mathbf{t}_{-w}^* \mathbf{t}_{0 g^{*-w} K} w g^{*-1} \mathbf{t}_{wg}^* \mathbf{t}_{-wg}^* w g^{* \nu} = z \mathbf{t}_{-w}^* \mathbf{t}_{0 g^{*-w}} = z^w + 0 g^{*-w}$$

$$\Rightarrow \zeta \text{LHS} = w g^{*-n} z^w + 0 g^{*-w} + \zeta_K w g^{* \nu} \mathbf{1} = w g^{*-n} z g^{wg} w g^{* \nu} + \zeta_K w g^{* \nu} \mathbf{1} = w g^{*-n} (z g^{wg} + \zeta)_K w g^{* \nu} \mathbf{1} = \zeta \text{RHS}$$

$$\zeta \overbrace{z G_w \times z^{w+} \mathbf{1}}^{\zeta} = \zeta + z \Delta_{-w}^n (\zeta + z)^{w-z^w} \mathbf{1} = \zeta \Delta_{-w^z}^n z \Delta_w^n \zeta^{w^z z} B_w^{-1} \mathbf{1}$$

$$\zeta \overbrace{z G_w \times z^{w+} \Delta_{-w}^n}^{\zeta} = \zeta + z \Delta_{-w}^n (\zeta + z)^{w-z^w} \Delta_{-w}^n = z \Delta_w^n \zeta \Delta_{-w^z}^n \zeta^{w^z z} B_w^{-1} B_{-w}^n = z \Delta_w^n -\zeta_U^{z G_w^{-1}} B_{\omega+w-z}^n Q_w$$

$$z G_z = {}_U \mathfrak{g}_z^{-1} {}_U \mathfrak{g}_z^{-*} = \overbrace{z B_z^{1/2} \mathfrak{t}_{zz}^*}^{-1} \overbrace{z B_z^{1/2} \mathfrak{t}_{zz}^*}^{-*} = \mathfrak{t}_{-zz}^* z B_z^{-1/2} z B_z^{-1/2} \mathfrak{t}_{-zz} = \mathfrak{t}_{-zz}^* z B_z^{-1} \mathfrak{t}_{-zz}$$

$$\Rightarrow z G_w = \mathfrak{t}_{-wz}^* z B_w^{-1} \mathfrak{t}_{-zw} \Rightarrow \begin{cases} \zeta_U^{z G_w} + z^w & = \zeta^{w^z z} B_w^{-1} = (\zeta + z)^w - z^w \\ \zeta_U^{z G_w} & = \zeta \mathfrak{t}_{-wz}^* z B_w^{-1} = \zeta B_{w^z}^{-1} B_w^{-1} = \zeta + z B_w^{-1} \end{cases}$$

$$\Rightarrow \text{LHS} = \zeta_z B_w^{-n/p} z^w + \zeta^z B_w \mathbf{1} = \text{RHS}$$

$$\zeta^{w^z z} B_w^{-1} B_\omega \zeta B_{w^z} = \zeta^{w^z} B_{\omega^w B_z^{-1}} \zeta B_{w^z} \stackrel{\text{JP33}}{=} \zeta B_{\omega^w B_z^{-1} + w^z} = \zeta B_{\underbrace{\omega + w - z}_{Q_w} B_z^{-1}} = \zeta^z B_w^{-1} B_{\omega + w - z} Q_w$$

$$\Rightarrow \zeta^{w^z z} B_w^{-1} \Delta_\omega^n \zeta B_{-w^z}^n = \zeta^z B_w^{-1} \Delta_{\omega + w - z}^n Q_w$$

$$\begin{array}{ccc}
D \begin{array}{c} \Delta_w^2 \\ \Delta_w \end{array} Z \begin{array}{c} \Delta_w \\ \Delta_w \end{array} \overset{n^-}{\mathbb{C}} \mathfrak{X} T^{-n-\nu} & \xleftarrow[\Delta_w^{-\nu-n}]{U G_w^{-n^-} \mathfrak{t}_{\sim w}} & Z \begin{array}{c} \Delta_w \\ \Delta_w \end{array} \overset{\check{\mathbb{C}}}{\mathfrak{X}} T^{-\nu} \\
\uparrow g \overset{n^-}{\mathbb{K}}_{\nu+n} & & \downarrow \begin{array}{c} w \check{g}^*_{\mathbb{K}} \\ w \check{g}^*_{\mathbb{T}} \end{array} \\
D \begin{array}{c} \Delta_w^2 \\ \Delta_w \end{array} Z \begin{array}{c} \Delta_w \\ \Delta_w \end{array} \overset{n^-}{\mathbb{C}} \mathfrak{X} T^{-n-\nu} & \xleftarrow[\Delta_{wg}^{-\nu-n}]{U G_{wg}^{-n^-} \mathfrak{t}_{\sim wg}} & Z \begin{array}{c} \Delta_w \\ \Delta_w \end{array} \overset{\check{\mathbb{C}}}{\mathfrak{X}} T^{-\nu}
\end{array}$$

$$\zeta|z \overbrace{g^{-1} \mathbb{K} \left[ \zeta+z B_{-w}^n (\zeta+z)^w - z^w \right] \mathbb{A}} = w \check{g}^*_{\mathbb{T}} \zeta+z \Delta_{wg}^n (\zeta+z)^{wg} - z^{wg} \overbrace{w \check{g}^*_{\mathbb{K}} \mathbb{A}}$$

$$\begin{aligned}
& \zeta|z \overbrace{g \mathbb{K} \left[ \zeta+z \Delta_{wg}^n (\zeta+z)^{wg} - z^{wg} \right] \overbrace{w \check{g}^*_{\mathbb{K}} \mathbb{A}}} = \zeta+z g^{-n} (\zeta+z) g \Delta_{wg}^n \overbrace{(\zeta+z) g^{wg} - z g^{wg} \overbrace{w \check{g}^*_{\mathbb{K}} \mathbb{A}}} \\
& = \zeta+z g^{-n} (\zeta+z) g \Delta_{wg}^n \overbrace{(\zeta+z) g^{wg} \overbrace{w \check{g}^*_{\mathbb{K}} \mathbb{A}} - z g^{wg} \overbrace{w \check{g}^*_{\mathbb{K}} \mathbb{A}}} = \zeta+z g^{-n} (\zeta+z) g \Delta_{wg}^n (\zeta+z)^w + 0 g^{-w} - z^w - 0 g^{-w} \mathbb{A} \\
& = \zeta+z B_{-w}^n w \check{g}^*_{\mathbb{T}} (\zeta+z)^w - z^w \mathbb{A}
\end{aligned}$$

$$\begin{array}{ccc}
D \begin{array}{c} \Delta_w^2 \\ \Delta_w \end{array} Z \begin{array}{c} \Delta_w \\ \Delta_w \end{array} \overset{n^-}{\mathbb{C}} \mathfrak{X} T^{-n-\nu} & \xleftarrow{\mathcal{I}} & D \begin{array}{c} \Delta_w^2 \\ \Delta_w \end{array} \mathbb{K} \mathfrak{X} T^{-\nu} \\
\mathcal{I} \overbrace{\Delta_w^{-\nu} B_w^{-\check{\mathbb{C}}}} \mathbb{A} & = & \Delta_w^{-\nu-n} U G_w^{-n^-} \mathfrak{t}_{\sim w} \mathbb{A} \\
\zeta|z \overbrace{\mathcal{I} \overbrace{\Delta_w^{-\nu} B_w^{-\check{\mathbb{C}}}} \mathbb{A}} & = & z \Delta_w^{-\nu-n} z + \zeta B_{-w}^n (\zeta+z)^w - z^w \mathbb{A} = z \Delta_w^{-\nu} \zeta B_{-w^z}^n \zeta^{wz} B_w^{-1} \mathbb{A}
\end{array}$$

$$\begin{aligned}
& \overset{-1}{g} \overset{\check{\mathbb{K}}}{\mathbb{V}} \overbrace{\Delta_w^{-\nu} B_w^{-\check{\mathbb{C}}}} \mathbb{A} = w \check{g}^*_{\mathbb{T}} \Delta_{wg}^{-\nu} B_{wg}^{-\check{\mathbb{C}}} w \check{g}^*_{\mathbb{K}} \mathbb{A} \\
& \mathcal{I} \overbrace{\overset{-1}{g} \overset{\check{\mathbb{K}}}{\mathbb{V}} \overbrace{\Delta_w^{-\nu} B_w^{-\check{\mathbb{C}}}} \mathbb{A}} = \mathcal{I} \overbrace{w \check{g}^*_{\mathbb{T}} \Delta_{wg}^{-\nu} B_{wg}^{-\check{\mathbb{C}}} w \check{g}^*_{\mathbb{K}} \mathbb{A}} = w \check{g}^*_{\mathbb{T}} \mathcal{I} \overbrace{\Delta_{wg}^{-\nu} B_{wg}^{-\check{\mathbb{C}}} w \check{g}^*_{\mathbb{K}} \mathbb{A}} \\
& = w \check{g}^*_{\mathbb{T}} \Delta_{wg}^{-\nu} U G_{wg}^{-n^-} \mathfrak{t}_{\sim wg} w \check{g}^*_{\mathbb{K}} \mathbb{A} = \overset{-1}{g} \overset{\check{\mathbb{K}}}{\mathbb{V}} \overbrace{\Delta_w^{-\nu} U G_w^{-n^-} \mathfrak{t}_{\sim w} \mathbb{A}} = \overset{-1}{g} \overset{\check{\mathbb{K}}}{\mathbb{V}} \overbrace{\mathcal{I} \overbrace{\Delta_w^{-\nu} B_w^{-\check{\mathbb{C}}}} \mathbb{A}}
\end{aligned}$$

$$(-n)_{\zeta} \underbrace{\zeta}_{\rightarrow w^z} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \zeta^{wz} B_w^{-1} K_b^{\zeta} = \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \underbrace{\mathfrak{K}}_{\rightarrow \zeta} \underbrace{B_w^{-1} \mathfrak{K} K_b^{\zeta}}_{\rightarrow \zeta} \text{poly } \zeta$$

$$\begin{aligned} \text{RHS} &= \underbrace{z B_w^{-1} \mathfrak{K} K_b^{\zeta}}_{\rightarrow \zeta} \underbrace{\mathfrak{K}}_{\rightarrow \zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} = \underbrace{K_b^{\zeta} K_{b^w B_z^{-1}}^{\zeta}}_{\rightarrow \zeta} \underbrace{\mathfrak{K}}_{\rightarrow \zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} = \underbrace{b^w B_z^{-1} K_{\partial}^{\zeta}}_{\rightarrow \zeta} \underbrace{0}_{\rightarrow \zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} = \underbrace{b^w B_z^{-1} K_{\partial}^{\zeta}}_{\rightarrow \zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \\ &= (-n)_{\zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \underbrace{b^w g_z^{-1} K_{\zeta^{wz}}^{\zeta}}_{\rightarrow \zeta} = (-n)_{\zeta} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \underbrace{b K_{\zeta^{wz} B_w^{-1}}^{\zeta}}_{\rightarrow \zeta} = \bar{\text{LHS}} \end{aligned}$$

$$\zeta|z \overbrace{\mathcal{I} \Delta_w^{-\lambda} B_w^{-1} \mathfrak{A}}^{\zeta} = z \Delta_w^{-\lambda-n} \zeta \overbrace{z B_w \mathfrak{K} z^{w+} \mathfrak{A}}^{\zeta} = z \Delta_w^{-\lambda} \zeta B_{w^z}^n \zeta^{wz} B_w^{-1} \mathfrak{A} = z \Delta_w^{-\lambda-n} z + \zeta B_w^n (\zeta+z)^w - z^w \mathfrak{A}$$

$$\begin{aligned} \mathcal{I} \overbrace{g^{-1} \mathfrak{K} z \Delta_w^{-\lambda} z B_w^{-1} \mathfrak{A}}^{\zeta} &= \mathcal{I} \overbrace{g^{-1} \mathfrak{K} z \Delta_w^{-\lambda} g^{-1} \mathfrak{K} z B_w^{-1} \mathfrak{A}}^{\zeta} = \mathcal{I} \overbrace{T G_{wg}^{-\lambda} w g^{\lambda} z B_{wg}^{-1} w g^{\lambda} \mathfrak{A}}^{\zeta} \\ &= \underbrace{w g^{\lambda}}_T \mathcal{I} \overbrace{T G_{wg}^{-\lambda} z B_{wg}^{-1} w g^{\lambda} \mathfrak{A}}^{\zeta} = \underbrace{w g^{\lambda}}_T \underbrace{z G_{wg}^{-\lambda-n} z B_{wg}}_{\zeta g^{wg+}} \underbrace{w g^{\lambda}}_K \mathfrak{A} \\ &= \underbrace{w g^{\lambda}}_T \underbrace{z G_{wg}^{-\lambda-n} z B_{wg}}_T \underbrace{w g^{\lambda} n w g^{\lambda} z^{w+} \mathfrak{A}}_U = \underbrace{z G_{wg}^{-\lambda-n}}_T \underbrace{w g^{\lambda+n}}_T \underbrace{z B_{wg} w g^{\lambda} z^{w+} \mathfrak{A}}_U \\ &= \overbrace{g^{-1} \mathfrak{K} z \Delta_w^{-\lambda-n}}^{\zeta} \overbrace{g^{-1} \mathfrak{K} z B_w z^{w+} \mathfrak{A}}^{\zeta} = \overbrace{g^{-1} \mathfrak{K} z \Delta_w^{-\lambda-n} z B_w z^{w+} \mathfrak{A}}^{\zeta} = \overbrace{g^{-1} \mathfrak{K} \mathcal{I} \Delta_w^{-\lambda} z B_w^{-1} \mathfrak{A}}^{\zeta} \end{aligned}$$

$$\zeta \overbrace{z B_w \mathfrak{K} z^{w+} K_{\omega}^{-\nu}}^{\zeta} = \zeta + z \underbrace{\mathfrak{b}^n}_{\rightarrow w} (\zeta+z)^w - z^w K_{\omega}^{-\nu} = \underbrace{z}_{\rightarrow w} \underbrace{\mathfrak{b}^n}_{\rightarrow w} \zeta \underbrace{\mathfrak{b}^n}_{\rightarrow w} \zeta^{wz} B_w^{-1} K_{\omega}^{-\nu} = \underbrace{z}_{\rightarrow w} \underbrace{\mathfrak{b}^n}_{\rightarrow w} \frac{1}{(-n)_{\nu}} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{\mathfrak{b}^n}_{\rightarrow \zeta} \underbrace{\mathfrak{K}}_{\rightarrow \zeta} \underbrace{z B_w^{-1} \mathfrak{K} K_{\omega}^{-\nu}}_{\rightarrow \zeta}$$

$$\mathfrak{A} \in D_{\Delta}^2 Z_{\Delta} \underbrace{\mathbb{C} \mathfrak{X} \mathbb{C}}_{\lambda+n} \leftarrow D_{\Delta}^2 Z_{\Delta} \underbrace{\mathbb{C} \mathfrak{X} \mathbb{C}}_{\lambda} \ni \mathfrak{A}$$

$$\begin{aligned} \zeta|z \overbrace{\mathcal{I} \Delta_w^{-\lambda} B_w^{-1} \mathfrak{K} E_{\omega}^{-\nu}}^{\zeta} &= z \Delta_w^{-\lambda-n} \zeta \overbrace{z B_w \mathfrak{K} z^{w+} E_{\omega}^{-\nu}}^{\zeta} = z \Delta_w^{-\lambda-n} \zeta + z B_w^n (\zeta+z)^w - z^w E_{\omega}^{-\nu} \\ &= \underbrace{z \Delta_w^{-\lambda} \zeta B_{w^z}^n \zeta^{wz} B_w^{-1} E_{\omega}^{-\nu}}_{\rightarrow \zeta} = \underbrace{z \Delta_w^{-\lambda}}_{\rightarrow \zeta} \frac{1}{(-n)_{\nu}} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{B_{\zeta}^n \mathfrak{K}}_{\rightarrow \zeta} \underbrace{z B_w^{-1} \mathfrak{K} E_{\omega}^{-\nu}}_{\rightarrow \zeta} \\ &\Rightarrow \underbrace{z B_w^{\lambda}}_{\rightarrow \zeta} \zeta|z \overbrace{\mathcal{I} \Delta_w^{-\lambda} B_w^{-1} \mathfrak{K} E_{\omega}^{-\nu}}^{\zeta} = \frac{1}{(-n)_{\nu}} \underbrace{w^z}_{\rightarrow \zeta} \underbrace{B_{\zeta}^n \mathfrak{K}}_{\rightarrow \zeta} \underbrace{z B_w^{-1} \mathfrak{K} E_{\omega}^{-\nu}}_{\rightarrow \zeta} \end{aligned}$$

$$\underbrace{w^{z+} B_{\zeta}^n \rtimes \eta}_{} = \overbrace{\partial_{w^{z+} B_{\zeta}^n} \eta}^0 = \overbrace{1 - \zeta (w^z + \partial)}^n \eta = \zeta B_{w^z}^n \zeta^{w^z} B_{\partial}^n \eta$$

$$\zeta|z \overbrace{g \rtimes \eta} = {}^z g^{-\nu} - \zeta_K {}^z g|z g_S$$

$${}^z g \underline{\mathcal{K}}_w = {}^z g^{-\nu} {}^z \underline{\mathcal{K}}_w {}^w \underline{g}^{*\nu}$$

$$\zeta|z \overbrace{\tilde{\mathcal{K}}_w} = \zeta + {}^z \underline{\mathcal{K}}_w \Rightarrow g \rtimes \tilde{\mathcal{K}}_w = \tilde{\mathcal{K}}_{w^{-1}} {}^w \underline{g}^{*\nu}$$

$$\zeta|z \overbrace{g \rtimes \tilde{\mathcal{K}}_w} = \zeta \overbrace{{}^z g^{-\nu} \rtimes {}^z g \tilde{\mathcal{K}}_w} = \zeta \underline{{}^z g}^{-\nu/p} \zeta_U {}^z g|z g \tilde{\mathcal{K}}_w = \zeta + {}^z g^{-\nu} \zeta_U {}^z g + {}^z g \tilde{\mathcal{K}}_w$$

$$= \zeta + {}^z g^{-\nu} \zeta + {}^z g \underline{\mathcal{K}}_w = \zeta + {}^z \underline{\mathcal{K}}_{w^{-1}} {}^w \underline{g}^{*\nu} = \zeta|z \tilde{\mathcal{K}}_{w^{-1}} {}^w \underline{g}^{*\nu}$$

$${}^z \underline{\mathcal{K}}_w = \overbrace{1 - z\dot{w}}^{\nu} = {}^z G_w^{-\nu}$$

$${}^z g B_{wg} = {}^w \underline{g}^* {}^z B_w {}^z g \Rightarrow {}^z g G_{wg}^{-\nu} = {}^w \underline{g}^{*\nu} {}^z G_w^{-\nu} {}^z g^{-\nu}$$

$$\zeta|z \mathcal{K}_w = \zeta + {}^z \underline{\mathcal{K}}_w$$

$$g \rtimes \mathcal{K}_w = \mathcal{K}_{w^{-1}} {}^w \underline{g}^{*\nu}$$

$$\zeta|z \overbrace{g \rtimes \mathcal{K}_w} = \zeta + {}^z g^{-\nu} \zeta + {}^z g \mathcal{K}_w = \zeta + {}^z g^{-\nu} \zeta + {}^z g \mathcal{K}_{w^{-1}} = \zeta + {}^z \mathcal{K}_{w^{-1}} {}^w \underline{g}^{*\nu} = \zeta|z \mathcal{K}_{w^{-1}} {}^w \underline{g}^{*\nu}$$

$$\zeta|z \mathcal{K}_w {}^z k_w^{\nu+\lambda}$$

$$g \rtimes \underbrace{\mathcal{K}_w k_w^{\nu+\lambda}} = \underbrace{g \rtimes \mathcal{K}_w} \underbrace{g \rtimes k_w^{\nu+\lambda}} = \mathcal{K}_{w^{-1}} {}^w \underline{g}^{*\nu} k_{w^{-1}} {}^w \underline{g}^{\nu+\lambda} = \mathcal{K}_{w^{-1}} k_{w^{-1}} {}^w \underline{g}^{*\lambda}$$