

$$\mathbb{1} \in {}^r\mathbb{C}$$

$${}^r\mathbb{C}_r \triangleleft_{\sigma} {}^r\mathbb{C} \ni \mathbb{H}$$

$$\mathbb{H} \rtimes \mathbb{H} = \int_{dz}^{{}^r\mathbb{C}_r} \underbrace{{}^z\mathbb{H} \mathbb{1} - z\mathbb{H}^* \mathbb{1}}_{{}^z\mathbb{H} \mathbb{1} - z\mathbb{H}^* \mathbb{1}} \overleftarrow{{}^z\mathbb{H} \mathbb{1} - z\mathbb{H}^* \mathbb{1}}$$

$$\mathbb{1}_1 \rtimes \mathbb{1}_1 = 1$$

$$\overbrace{\begin{array}{c|c} A & B \\ \hline C & D \end{array}} \rtimes \mathbb{H} = \overbrace{\frac{-1}{A+zD} \overline{B+zD}}^{\frac{-1}{A+zD} \overline{B+zD}} \mathbb{H} \overleftarrow{\frac{-\lambda}{B+zD}}$$

$${}^z\mathbb{H} = \mathcal{D}_z \rtimes \mathbb{H} \text{ kernel}$$

$${}^z\mathcal{D}_w \mathbb{1} = \underbrace{\mathbb{1} - z\mathbb{H}^* \mathbb{1}}_{\mathbb{1} - z\mathbb{H}^* \mathbb{1}} \overleftarrow{\mathbb{1} - z\mathbb{H}^* \mathbb{1}}$$

$$\overline{{}^r\mathbb{C}_r^U \rtimes {}^r\mathbb{C}_r^U}_{\sigma: \bar{\sigma}} = {}^r\mathbb{C}_r^U \rtimes {}^r\mathbb{C}_r^{\sharp U}$$

$${}^r\mathbb{C}_r \triangleleft_{\sigma} \mathbb{C} = \sum_{\sigma}^{{}^r\bar{\mathbb{N}}} {}^r\mathbb{C}_r^U \rtimes {}^r\mathbb{C}_r^{\sharp U}$$

$${}^r\mathbb{C}_r \triangleleft_{\sigma} {}^r\mathbb{C} \stackrel{\text{K-branch}}{=} \sum_{\sigma}^{{}^r\bar{\mathbb{N}}} \underbrace{{}^r\mathbb{C} \rtimes {}^r\mathbb{C}_r^U}_{= \sum_i^r {}^r\mathbb{C}_r^U \sigma + \varepsilon_i} \rtimes {}^r\mathbb{C}_r^{\sharp U} = \sum_i^r \sum_{\sigma}^{{}^r\bar{\mathbb{N}}} {}^r\mathbb{C}_r^U \sigma + \varepsilon_i \rtimes {}^r\mathbb{C}_r^{\sharp U}$$

$${}^z\mathcal{D}_w = \sum_i^r \sum_{\sigma}^{{}^r\bar{\mathbb{N}}} {}^z\mathbb{f}_w^{\sigma}$$