

$$\begin{aligned}
{}^0\overline{\mathfrak{H}F} &= \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \overline{-iy}^n \overbrace{\frac{\partial^n}{n!} \frac{(1-x^2)^{n-\ell/2-1}}{1-x^2} \frac{-n}{1-ixy} iy \overline{\mathfrak{g}_x \times F}}^0 \\
&= \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \overline{-iy}^{m+n} \overbrace{\frac{\partial^n}{n!} \frac{(1-x^2)^{m+n-\ell/2-1}}{1-x^2} \frac{-n}{1-ixy} \frac{-m}{1+ixy} x \overline{\partial^m F}}^0
\end{aligned}$$

$${}^{iy}\overline{\mathfrak{g}_x \times H} = \frac{iy \overline{1-x^2}^n \overline{\partial_z^n H}}{1+ixy} \frac{1}{n!} = \frac{y \overline{1-x^2}^n}{1+ixy} \frac{x \overline{\partial_z^n H}}{i^n} \frac{1}{n!} = \frac{y^n (1-x^2)^n}{(1+ixy)^n} \frac{\overline{\partial_y^n H}}{n!}$$

$$\frac{1+ixy}{1+x^2y^2} = \frac{1}{1-ixy} = \frac{1-\bar{z}x}{1-x^2}$$

$$\int_{dx} \frac{(1-x^2)^{\ell/2}}{1-x^2} {}^x\overline{\Phi} {}^x\overline{\mathfrak{H}F} = \int_{dz} \frac{(1-z\bar{z})^\ell}{(1-z\bar{z})^2} {}^z\overline{\Phi} \frac{-\ell/2}{1-z^2} {}^zF$$

$$= \int_{dx} \frac{-1}{1-x^2} \int_{dy} \frac{1+y^2}{(1-y^2)^2} {}^{iy}\overline{\mathfrak{g}_x \times \overline{\Phi} F} \frac{(1-x^2)^\ell (1-y^2)^\ell}{(1+x^2y^2)^\ell} \frac{(1+ixy)^\ell}{(1-x^2)^{\ell/2} (1+y^2)^{\ell/2}}$$

$$= \int_{dx} \frac{B_{\mathbb{R}}}{1-x^2} \frac{\ell/2-1}{(1+y^2)^{\ell/2-1}} \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \frac{(1-\bar{z}x)^\ell}{(1-x^2)^\ell} {}^{iy}\overline{\mathfrak{g}_x \times \overline{\Phi} F} = \int_{dx} \frac{B_{\mathbb{R}}}{1-x^2} \frac{-\ell/2-1}{(1+y^2)^{\ell/2-1}} \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} {}^{iy}\overline{\mathfrak{g}_x \times \Delta_x^\ell \Phi F}$$

$$= \int_{dx} \frac{B_{\mathbb{R}}}{1-x^2} \frac{n-\ell/2-1}{(1+y^2)^{\ell/2-1}} \frac{x \overline{\partial^n \Delta_x^\ell \Phi}}{n!} \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \frac{-n}{1-ixy} \overline{-iy}^n {}^{iy}\overline{\mathfrak{g}_x \times F}$$

$$= \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \overline{-iy}^n \int_{dx} {}^x\overline{\Delta_x^\ell} {}^x\overline{\Phi} \frac{1}{n!} \overbrace{\frac{\partial^n}{n!} \frac{(1-x^2)^{n-\ell/2-1}}{1-x^2} \frac{-n}{1-ixy} iy \overline{\mathfrak{g}_x \times F}}^x$$

$$\Rightarrow {}^x\overline{\mathfrak{H}F} = {}^x\overline{\Delta_x^\ell} \int_{dy} \frac{(1-y^2)^{\ell-2}}{(1+y^2)^{\ell/2-1}} \overline{-iy}^n \overbrace{\frac{\partial^n}{n!} \frac{(1-x^2)^{n-\ell/2-1}}{1-x^2} \frac{-n}{1-ixy} iy \overline{\mathfrak{g}_x \times F}}^x$$

$$\begin{aligned}
& \stackrel{z = \zeta \mathfrak{g}_w}{=} \int_{dw}^{\mathbb{R}^D} w \Delta_w^{-p/2} \int_{d\mu_0(z)}^{\pi^{-1}(0)} \zeta_{\mathbb{C}\Delta_w}^{\mathfrak{g}_w} \Delta_{\zeta \mathfrak{g}_w}^{\ell} \zeta_{\mathfrak{g}_w \bar{\Phi}} \zeta_{\mathbb{C}\Delta_{\bar{\zeta} \mathfrak{g}_w}}^{-\ell/2} \zeta_{\mathfrak{g}_w} F = \int_{dw}^{\mathbb{R}^D} w \Delta_w^{-p/2} \int_{d\mu_0(\zeta)}^{\pi^{-1}(0)} \zeta_{\mathbb{C}\Delta_{\zeta \mathfrak{g}_w}}^{\mathfrak{g}_w} \Delta_{\zeta \mathfrak{g}_w}^{\ell} \zeta_{\mathfrak{g}_w \bar{\Phi}} \zeta_{\mathbb{C}\Delta_{\bar{\zeta} \mathfrak{g}_w}}^{-\ell/2} \zeta_{\mathfrak{g}_w} F \\
& = \int_{dw}^{\mathbb{R}^D} w \Delta_w^{-\ell/2 - p/2} \int_{d\mu_0(\zeta)}^{\pi^{-1}(0)} \zeta_{\mathbb{C}\Delta_{\zeta}}^{\mathfrak{g}_w} \Delta_{\zeta}^{\ell} \zeta_{\mathbb{C}\Delta_{\bar{\zeta}}}^{-\ell/2} \bar{\zeta}_{\mathfrak{g}_w} \Delta_w^{\ell} \zeta_{\mathfrak{g}_w \bar{\Phi}} \zeta_{\mathfrak{g}_w} F = \int_{dw}^{\mathbb{R}^D} w \Delta_w^{-\ell/2 - p/2} \int_{d\mu_0(\zeta)}^{\pi^{-1}(0)} \zeta_{\mathbb{C}\Delta_{\zeta}}^{\mathfrak{g}_w} \Delta_{\zeta}^{\ell} \zeta_{\mathbb{C}\Delta_{\bar{\zeta}}}^{-\ell/2} \zeta_{\mathfrak{g}_w \bar{\Phi}} \zeta_{\mathfrak{g}_w} F
\end{aligned}$$