

$$\begin{aligned}
\mathfrak{E}|_{\mathfrak{U}\mathbb{L}} &= \mathfrak{E}_1^{\circ}|_{\mathfrak{U}\mathbb{L}} \times \mathfrak{E}_{-}^{\circ}|_{\mathfrak{U}\mathbb{L}} \times \sum_{\mathbb{1} \neq 0} \mathfrak{E}^{\mathbb{1}}|_{\mathfrak{U}\mathbb{L}} \\
&= \mathfrak{E}^{\circ}|_{\mathfrak{U}\mathbb{L}} \times \sum_{1 \leq i < j \leq r} \mathfrak{E}_{j-i}^{\times}|_{\mathfrak{U}\mathbb{L}} \times \sum_{0 \leq i \leq j \leq r} \mathfrak{E}_{j+i}^{\times}|_{\mathfrak{U}\mathbb{L}} \\
\mathfrak{E}_{-}^{\circ}|_{\mathfrak{U}\mathbb{L}} &= \mathbb{R} \frac{\overbrace{e_k - ze_k^*z} \partial_z}{1 \leq k \leq r} \mathbb{1} \rightarrow \mathbb{R} \\
\mathfrak{E}_1^{\circ}|_{\mathfrak{U}\mathbb{L}} &= \frac{\delta \in \mathfrak{E}(X)}{e_k \delta = 0}
\end{aligned}$$

$$\mathfrak{E}_{j-i}^{\times}|_{\mathfrak{U}\mathbb{L}} = \frac{X_a^- + 2\kappa \overbrace{\check{a}e_j - \check{e}_j a}}{a = \check{a} \in \mathbb{L}_j^i}: \quad 0 < i < j$$

$$\check{a}e_j - \check{e}_j a = \check{e}_i a - \check{a}e_i = \underbrace{e_i^* e_j}_a = \check{a} \underbrace{e_j - e_i}$$

$$\mathfrak{E}_{j+i}^{\times}|_{\mathfrak{U}\mathbb{L}} = \frac{X_a^- + 2\kappa \overbrace{\check{a}e_j - \check{e}_j a}}{a = -\check{a} \in \mathbb{L}_j^i}: \quad i < j$$

$$\check{a}e_j - \check{e}_j a = \check{a}e_i - \check{e}_i a = \check{a} \underbrace{e_j + e_i}_a = -\underbrace{e_j^* e_i}_a = \check{a}e = -\check{e}a$$

$$\mathfrak{E}_{2j}^{\times}|_{\mathfrak{U}\mathbb{L}} = \frac{X_a^- + \kappa \overbrace{\check{a}e_j - \check{e}_j a}}{a = -\check{a} \in \mathbb{L}_j^j}$$

$$\check{a}e_j - \check{e}_j a = 2\check{a}e_j = -2\check{e}_j a = 2\check{a}e = -2\check{e}a$$

$$\mathfrak{E}_j^r |_{\mathfrak{U}\mathbb{L}} = \frac{X_a^- + 2\kappa \overbrace{\check{a}e_j - \check{e}_j a}}{a \in {}^0\mathbb{L}_j}: \quad 0 = i < j$$

$$\check{a}e_j - \check{e}_j a = \check{a}e - \check{e}a$$

$$\mathfrak{E}^4 |_{\mathfrak{U}\mathbb{L}} = \frac{\mathfrak{b} \in \mathfrak{E} |_{\mathfrak{U}\mathbb{L}}}{\mathfrak{b} \times \underbrace{e_k - \check{e}_k}_{= \underbrace{e_k - \check{e}_k} \mathbb{1}} \mathfrak{b}}$$

$$\mathfrak{E}_{j-\varepsilon i}^r |_{\mathfrak{U}\mathbb{L}} = \mathfrak{E}^{\kappa \delta^j - \varepsilon \delta^i} |_{\mathfrak{U}\mathbb{L}} = \frac{X_a^- + \varepsilon i \# j \overbrace{\check{a}e_j - \check{e}_j a}}{a \in {}^i\mathbb{L}_j; \quad \check{a} = \varepsilon i}: \quad \varepsilon = 1:0:-1$$

$$\underbrace{e_k - \check{e}_k} \mathbb{1} = \kappa \underbrace{\partial_k^j - \varepsilon \delta_k^i}$$

$$X_a^- \times X_b^- = 2 \overbrace{\check{a}b - \check{b}a}$$

$$X_a^- \times \overbrace{\check{b}c - \check{c}b} = X_{\overbrace{abc - a\check{c}b}}^-$$

$$\overbrace{X_a^- + \varepsilon i \# j \check{a}e_j - \check{e}_j a} \times X_{e_k}^- = 2 \overbrace{\check{a}e_k - \check{e}_k a} + \varepsilon i \# j X_{\overbrace{e_k \check{e}_j a - e_k \check{a}e_j}}^-$$

$$1 \leq i < j \leq r \Rightarrow \text{RHS} = 2 \delta_k^i \overbrace{\check{a}e_i - \check{e}_i a} + \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + 2\kappa X_{\overbrace{\delta_k^j e_j \check{e}_j a - \delta_k^i e_i \check{e}_i a}}^- =$$

$$2 \delta_k^i \overbrace{\check{e}_j \check{a} - \check{a} e_j} + \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + \kappa X_{\overbrace{\delta_k^j a - \delta_k^i \check{a}}}^- = \kappa \underbrace{\partial_k^j - \varepsilon \delta_k^i} X_a^- + 2\kappa \overbrace{\check{a}e_j - \check{e}_j a}$$

$$1 \leq i = j \leq r \Rightarrow \text{RHS} = 2 \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + \kappa X_{\overbrace{\delta_k^j e_j \check{e}_j a - \delta_k^j e_j \check{a}e_j}}^- =$$

$$2 \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + \kappa \delta_k^j X_{\overbrace{a - \check{a}}}^- = 2\kappa \delta_k^j X_a^- + \kappa \overbrace{\check{a}e_j - \check{e}_j a}$$

$$0 = i < j \Rightarrow \text{RHS} = 2 \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + 2\kappa X_{\overbrace{\delta_k^j e_j \check{e}_j a}}^- = 2 \delta_k^j \overbrace{\check{a}e_j - \check{e}_j a} + \kappa \delta_k^j X_a^- = \kappa \delta_k^j \overbrace{X_a^- + 2\kappa \check{a}e_j - \check{e}_j a}$$

$$\mathfrak{E} |_{\mathfrak{E}\mathbb{L}} = \mathfrak{E}_1^{\mathcal{O}} |_{\mathfrak{E}\mathbb{L}} \times \mathfrak{E}_{-}^{\mathcal{O}} |_{\mathfrak{E}\mathbb{L}} \times \sum_{\mathbb{1} \neq 0} \mathfrak{E}^4 |_{\mathfrak{E}\mathbb{L}}$$

$$= \mathfrak{E}^{\mathcal{O}} |_{\mathfrak{E}\mathbb{L}} \times \sum_{1 \leq i < j \leq r} \mathfrak{E}_{j-i}^r |_{\mathfrak{E}\mathbb{L}} \times \sum_{0 \leq i \leq j \leq r} \mathfrak{E}_{j+i}^r |_{\mathfrak{E}\mathbb{L}}$$

$$\mathfrak{G}_-^o |_{\mathfrak{e}\mathbb{I}} = \langle 2ze_k^* e_k l_z | k \leq r \rangle \xrightarrow{\mathbb{1}} \mathbb{R}$$

$$\mathfrak{G}_1^o |_{\mathfrak{e}\mathbb{I}} = \frac{\delta \in \mathfrak{C}(X)}{e_k \delta = 0}$$

$$\mathfrak{G}_{j-i}^1 |_{\mathfrak{e}\mathbb{I}} = \frac{(z\check{a}e_j) \partial_z = (z\check{e}_i a) \partial_z}{a = \check{a} \in {}^i\mathbb{L}_j} : 0 < i < j$$

$$\mathfrak{G}_{j-i}^- |_{\mathfrak{e}\mathbb{I}} = \frac{(z\check{a}e_i) \partial_z = (z\check{e}_j a) \partial_z}{a = \check{a} \in {}^i\mathbb{L}_j} : 0 < i < j$$

$$\mathfrak{G}_{j+i}^1 |_{\mathfrak{e}\mathbb{I}} = \frac{a \partial_z}{a = -\check{a} \in {}^i\mathbb{L}_j} : i \leq j$$

$$\mathfrak{G}_{j+i}^- |_{\mathfrak{e}\mathbb{I}} = \frac{z\check{a}z \partial_z}{a = -\check{a} \in {}^i\mathbb{L}_j} : i \leq j$$

$$\mathfrak{G}_j^1 |_{\mathfrak{e}\mathbb{I}} = \frac{(b + 2z\check{b}e) \partial_z}{b \in {}^0\mathbb{L}_j} : 0 = i < j$$

$$\mathfrak{G}_j^- |_{\mathfrak{e}\mathbb{I}} = \frac{(z\check{b}z + 2z\check{e}b) \partial_z}{b \in {}^0\mathbb{L}_j} : 0 = i < j$$

$$\mathfrak{G}^1 |_{\mathfrak{e}\mathbb{I}} = \frac{\mathfrak{b} \in \mathfrak{G} |_{\mathfrak{e}\mathbb{I}}}{2\mathfrak{b} \times (\check{e}_k e_k) = \overline{(2\check{e}_k e_k)} \mathbb{1} \mathfrak{b}}$$

$$\mathfrak{G}_{j-i}^{\times} |_{\mathfrak{e}\mathbb{I}} = \mathfrak{G}^{\times \delta^j - \delta^i} |_{\mathfrak{e}\mathbb{I}}$$

$$2(\check{e}_k e_k) \mathbb{1} = \mathcal{X} \underbrace{\delta_k^j - \delta_k^i}$$

$$a \in {}^m\mathbb{L}_n$$

$$1 \leq m \neq n \leq r \Rightarrow (\check{a}e_n) \times (2\check{e}_k e_k) = 2\check{a} (e_n \check{e}_k e_k) - 2(e_k \check{e}_k a) e_n = 2\delta_k^n \check{a} e_n - (\delta_k^m + \delta_k^n) \check{a} e_n = (\delta_k^n - \delta_k^m) \check{a} e_n$$

$$\mathfrak{G}_{j+i}^{\times} |_{\mathfrak{e}\mathbb{I}} = \mathfrak{G}^{\times \delta^j + \delta^i} |_{\mathfrak{e}\mathbb{I}}$$

$$2(\check{e}_k e_k) \mathbb{1} = \mathcal{X} \underbrace{\delta_k^j + \delta_k^i}$$

$$a \rtimes (2z\check{e}_k e_k) = 2a\check{e}_k e_k = \underline{\delta_k^j + \delta_k^i} a$$

$$(2z\check{e}_k e_k) \rtimes (z\check{a}z) = 4(z\check{e}_k e_k) \check{a}z - 2(z\check{a}z) \check{e}_k e_k = 2z(e_k \check{e}_k a)z = \underline{\delta_k^j + \delta_k^i} z < \check{a}z$$

$$\mathfrak{E}_j^{\check{r}} |_{\mathfrak{e}\mathbb{I}} = \mathfrak{E}^{\check{r}\delta^j} |_{\mathfrak{e}\mathbb{I}}$$

$$2(\check{e}_k e_k) \mathbb{1} = \check{r}\delta_k^j$$

$$\begin{aligned} (b + 2\check{b}e) \rtimes_{\check{e}_k e_k} &= 2b \rtimes (\check{e}_k e_k) + 4(\check{b}e) \rtimes (\check{e}_k e_k) = 2b\check{e}_k e_k + 4(\check{b}(e\check{e}_k e_k) - (e_k \check{e}_k b)e) \\ &= \delta_k^j b + 4(\check{b}\delta_k^j e_j - \delta_k^j \check{b}e/2) = \delta_k^j (b + 2\check{b}e) \end{aligned}$$

$$\begin{aligned} 2(z\check{e}_k e_k) \rtimes (z\check{b}z + 2z\check{e}b) &= 4(z\check{e}_k e_k) \check{b}z - 2(z\check{b}z) \check{e}_k e_k + 4(\check{e}_k e_k) \rtimes (\check{e}b) = \\ 2z(e_k \check{e}_k b)z + 4(\check{e}_k (e_k \check{e}b) - (e\check{b}e_k)e_k) &= \delta_k^j z\check{b}z + 4\delta_k^j \check{e}_k b/2 = \delta_k^j (z\check{b}z + 2z\check{e}b) \end{aligned}$$

$$(2\check{e}_k e_k) \rtimes_{\mathfrak{G}} (2\check{e}_\ell e_\ell) = 4p\delta_{k:l}$$

$$\begin{aligned} \text{tr } \rtimes_{\mathfrak{G}} (2\check{e}_k e_k) \rtimes_{\mathfrak{G}} (2\check{e}_\ell e_\ell) &= \sum_{i < j} (\delta_k^j - \delta_k^i) (\delta_\ell^j - \delta_\ell^i) + \sum_{i < j} (\delta_k^j + \delta_k^i) (\delta_\ell^j + \delta_\ell^i) \\ &+ \sum_j 2\delta_k^j 2\delta_\ell^j 2 + \sum_j \delta_k^j \delta_\ell^j 4b = 4a \sum_{i < j} (\delta_k^j \delta_\ell^j + \delta_k^i \delta_\ell^i) + 4 \sum_j \delta_k^j \delta_\ell^j (2 + b) = \end{aligned}$$

$$\begin{cases} 4a \sum_{i < j} (\delta_k^j + \delta_k^i) + 4 \sum_j \delta_k^j (2 + b) = 4a \left(\sum_{k < j} 1 + \sum_{i < k} 1 + 4(2 + b) \right) = 4(a(r-1) + 2 + b) = 4p & k = \ell \\ 0 & k \neq \ell \end{cases}$$

$$M_{e_1}^\sharp$$

$$\text{prim pos roots} \begin{cases} \frac{M_{e_2}^\sharp - M_{e_1}^\sharp \dots M_{e_r}^\sharp M_{e_{r-1}}^\sharp}{2} & b = 0 \\ \frac{M_{e_1}^\sharp}{2}; \frac{M_{e_2}^\sharp - M_{e_1}^\sharp \dots M_{e_r}^\sharp M_{e_{r-1}}^\sharp}{2} & b > 0 \end{cases}$$