

$$\begin{aligned}
{}^x \widehat{\mathcal{B}F} &= \int_{d\delta^\ell(z)}^{S_\ell^{\mathbb{C}}} \overleftarrow{1+z^*}^{-1/2} {}^x \mathbf{e}_{c(z)-e} {}^z F \\
&= \int_{dU}^{G_\ell^{\mathbb{C}}} \int_{d\delta_U^\ell(z)}^{B_U} \overleftarrow{1+z^*}^{-1/2} {}^x \mathbf{e}_{c(z)-e} {}^z F = \int_{dU}^{G_\ell^{\mathbb{C}}} \int_{d\delta_U^\ell(z)}^{B_U} \overleftarrow{u+uz^*u}^{-1/2} {}^x \mathbf{e}_{c_u(z)-u} {}^z F
\end{aligned}$$

$$z \in U = Z_u^1 = Z_{e-u}^0 \Rightarrow c(z) - e = c_u(z) - u$$

$$\partial_\ell \Omega_{\triangleleft}^2 \mathbb{C} \xleftarrow[\text{unitary}]{\mathcal{I}} \mathbb{S}_\ell^{\mathbb{C}} \Omega_{\triangleleft}^2 \mathbb{C}$$

$${}^x \widehat{\mathcal{I}F} = \mathcal{I}_x \star F$$

$${}^z \mathcal{I}_x = \overleftarrow{1+z}^{-\ell a/2} c(z) - e \mathbf{e}_x$$

$$\mathcal{I} \underline{G}_w^{-\ell a/2} = f_w$$

$$\overleftarrow{\mathcal{I} \underline{G}_w^{-\ell a/2}} = \mathcal{I}_x \star \underline{G}_w^{-\ell a/2} = \underline{G}_w^{-\ell a/2} \overleftarrow{\mathcal{I}_x} \stackrel{\text{repr}}{\underset{\text{ker}}{=} } {}^w \overleftarrow{\mathcal{I}_x} = {}^x f_w$$

$$\mathcal{I} \underline{G}_w^{-\ell a/2} \star \mathcal{I} \underline{G}_w^{-\ell a/2} = f_w \star f_w \stackrel{\text{RSB}}{=} \underline{G}_w^{-\ell a/2} \stackrel{\text{CSB}}{=} \underline{G}_w^{-\ell a/2} \star \underline{G}_w^{-\ell a/2}$$

$$\partial_\ell \Omega_{\triangleleft}^2 \mathbb{C} \ni {}^x f$$

$$d_\ell x = \frac{2^{r\ell a/2}}{\Gamma_{ra/2}^\ell} \mathbf{e}^{-2x} d\mu_\ell(x)$$

$${}^x f_w = \overleftarrow{1+w^*}^{-\ell a/2} {}^x \mathbf{e}_{e-c(w)}$$

$$f_w \star f_w =$$

$$w \underline{G}_w^{-\ell a/2}$$

$$\begin{aligned} f_w \star f_w &= \int_{d_\ell x}^{\partial_\ell \Omega} x \bar{f}_w^x f_w^x = \frac{2^{r\ell a/2}}{\Gamma_{ra/2}^\ell} \int_{d_\ell x}^{\partial_\ell \Omega} e^{-2x} x \bar{f}_w^x f_w^x = \frac{2^{r\ell a/2}}{\Gamma_{ra/2}^\ell} \int_{d_\ell x}^{\partial_\ell \Omega} \overbrace{e^{-x^x} f_w^x}^* \underbrace{e^{-x^x} f_w^x} \\ &= \frac{2^{r\ell a/2}}{\Gamma_{ra/2}^\ell} \int_{d_\ell x}^{\partial_\ell \Omega} x e_{c(w)}^{-1} e_x^{-1} \overbrace{1+w^*}^{-\ell a/2} \overbrace{1+w}^{-\ell a/2} = \overbrace{1+w^*}^{-\ell a/2} \overbrace{1+w}^{-\ell a/2} \frac{2^{r\ell a/2}}{\Gamma_{ra/2}^\ell} \int_{d_\ell x}^{\partial_\ell \Omega} 2x e_{\Re c(w)}^{-1} \\ &= \overbrace{1+w^*}^{-\ell a/2} \overbrace{1+w}^{-\ell a/2} \frac{1}{\Gamma_{ra/2}^\ell} \int_{d_\ell x}^{\partial_\ell \Omega} x e_{\Re c(w)}^{-1} = \overbrace{1+w^*}^{-\ell a/2} \overbrace{1+w}^{-\ell a/2} \overbrace{\Re c(w)}^{-\ell a/2} = \overbrace{1-ww^*}^{-\ell a/2} = \text{RHS} \end{aligned}$$

$$\overline{\mathcal{I}_C \eta}^s = F_s \star \eta$$

$$\mathcal{I}_C F_t = \Phi_t$$

$$\overline{\mathcal{I}_C F_t}^s = F_s \star F_t = {}^s \Phi_t$$

$$\underline{S}_e^{\mathbb{C}} = \mathbb{R}e \times i \mathbb{R}e \times Z_{1/2}^{\mathbb{C}}(e) = \mathbb{C}e \times Z_{1/2}^{\mathbb{C}}(e)$$

$$\underline{S}_e^{\mathbb{R}} = \mathbb{R}e \times Z_{1/2}^{\mathbb{R}}(e)$$