

$$\left\{ \begin{array}{c} n_{\mathbb{C}}^{\mathbb{C}} \\ 2_{\mathbb{R}}^{\mathbb{C}} \\ n_{\mathbb{H}}^{\mathbb{C}} \\ 2_{\mathbb{C}}^{\mathbb{C}} \end{array} \right. \xrightarrow{\begin{array}{c|c} 0 & 1 \\ -1 & 0 \\ \hline 0 & \dagger \\ -\dagger & 0 \end{array}} \left\{ \begin{array}{c} n_{\mathbb{R}}^{\mathbb{C}} \\ 2_{\mathbb{R}}^{\mathbb{C}} \\ n_{\mathbb{C}}^{\mathbb{C}} \end{array} \right.$$

$$\Gamma = a + bi \Rightarrow \check{\Gamma} = \check{a} - \check{b}i \Rightarrow \underset{\mathbb{R}}{\Gamma} = \frac{a}{-b} \Big| \frac{b}{a} \xrightarrow{*_{\text{hom}}} \underset{\mathbb{R}}{\check{\Gamma}} = \frac{a}{-b} \Big| \frac{b}{\check{a}} = \frac{\check{a}}{\check{b}} \Big| \frac{-\check{b}}{\check{a}} = \frac{\check{a} - \check{b}i}{\mathbb{C}} = \underset{\mathbb{R}}{\check{\Gamma}}$$

$$\Gamma = a + bj \Rightarrow \check{\Gamma} = \check{a} - j\check{b} = \check{a} - \dagger b j \Rightarrow \underset{\mathbb{C}}{\Gamma} = \frac{a}{-\bar{b}} \Big| \frac{b}{\bar{a}} \xrightarrow{*_{\text{hom}}} \underset{\mathbb{C}}{\check{\Gamma}} = \frac{a}{-\bar{b}} \Big| \frac{b}{\bar{a}} = \frac{\check{a}}{\check{b}} \Big| \frac{-\dagger b}{\dagger \bar{a}} = \frac{\check{a} - \dagger b j}{\mathbb{C}} = \underset{\mathbb{C}}{\check{\Gamma}}$$

$$n_{\mathbb{R}}^{\mathbb{C}} \xrightarrow{\begin{array}{c|c} 1 & 0 \\ 0 & -1 \\ \hline 0 & -1 \\ -1 & 0 \end{array}} n_{\mathbb{C}}^{\mathbb{C}}$$

$$\left\{ \begin{array}{c} n_{\mathbb{C}}^{\mathbb{C}} \\ 2_{\mathbb{R}}^{\mathbb{C}} \\ n_{\mathbb{H}}^{\mathbb{C}} \\ 2_{\mathbb{C}}^{\mathbb{C}} \end{array} \right. = \left\{ \begin{array}{l} \underset{4}{\mathbb{R}}^{\mathbb{C}} \quad \underset{\mathbb{R}}{\Gamma} \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} \\ \hline \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} & 0 \end{array} = \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} \\ \hline \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} & 0 \end{array} \underset{\mathbb{R}}{\check{\Gamma}} \\ \underset{4}{\mathbb{C}}^{\mathbb{C}} \quad \underset{\mathbb{C}}{\Gamma} \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} \\ \hline \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} & 0 \end{array} = \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} \\ \hline \begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array} & 0 \end{array} \underset{\mathbb{C}}{\check{\Gamma}} \end{array} \right.$$

$$\frac{\bar{\sigma} \mid -\sigma i}{-i\bar{\sigma} \mid \sigma} \underset{\mathbb{C}_n}{\mathbb{C}} \frac{\sigma \mid \sigma i}{i\bar{\sigma} \mid \bar{\sigma}} = \underset{\mathbb{R}_n}{\mathbb{C}}$$

$$\Gamma = a + bi \in \underset{\mathbb{C}_n}{\mathbb{C}} \Rightarrow \underline{\Gamma} = \frac{\bar{\Gamma} \mid 0}{0 \mid \Gamma} = \underline{\Gamma}$$

$$\frac{\bar{\sigma} \mid -\sigma i}{-i\bar{\sigma} \mid \sigma} \frac{a - bi \mid 0}{0 \mid a + bi} \frac{\sigma \mid \sigma i}{i\bar{\sigma} \mid \bar{\sigma}} = \frac{\bar{\sigma} \mid -\sigma i}{-i\bar{\sigma} \mid \sigma} \underline{\Gamma} \frac{\sigma \mid \sigma i}{i\bar{\sigma} \mid \bar{\sigma}} = \underline{\Gamma} = \frac{a \mid b}{-b \mid a}$$

$$\sigma \in \mathbb{C}^U \Rightarrow \begin{cases} \frac{\bar{\sigma} \mid -j\bar{\sigma}}{\varkappa\bar{\sigma} \mid \varkappa j\bar{\sigma}} \underset{\mathbb{C}_n}{\mathbb{H}} \frac{\sigma \mid \varkappa\sigma}{\sigma j \mid -\varkappa\sigma j} = \underset{\mathbb{X}_n}{\mathbb{H}} & \underset{\mathbb{C}_n}{\mathbb{H}} = \frac{\sigma \mid \varkappa\sigma}{\sigma j \mid -\varkappa\sigma j} \underset{\mathbb{X}_n}{\mathbb{H}} \frac{\bar{\sigma} \mid -j\bar{\sigma}}{\varkappa\bar{\sigma} \mid \varkappa j\bar{\sigma}} \\ \underset{\mathbb{H}_n}{\mathbb{H}} = \frac{\bar{\sigma} \mid -j\bar{\sigma}}{-\varkappa i\bar{\sigma} \mid \varkappa j i\bar{\sigma}} \underset{\mathbb{C}_n}{\mathbb{H}} \frac{\sigma \mid \varkappa\sigma i}{\sigma j \mid \varkappa\sigma i j} & \frac{\sigma \mid \varkappa\sigma i}{\sigma j \mid \varkappa\sigma i j} \underset{\mathbb{H}_n}{\mathbb{H}} \frac{\bar{\sigma} \mid -j\bar{\sigma}}{-\varkappa i\bar{\sigma} \mid \varkappa j i\bar{\sigma}} = \underset{\mathbb{C}_n}{\mathbb{H}} \end{cases}$$

$$\frac{\bar{\sigma} \mid -j\bar{\sigma}}{\varkappa\bar{\sigma} \mid \varkappa j\bar{\sigma}} \frac{a \mid b}{-b \mid \bar{a}} \frac{\sigma \mid \varkappa\sigma}{\sigma j \mid -\varkappa\sigma j} = \frac{a + bj \mid 0}{0 \mid a - bj}$$

unit

$$\Gamma = a + bj \in \underset{\mathbb{H}_n}{\mathbb{H}} \Rightarrow \Gamma i \overset{*}{\Gamma} = i \Rightarrow \overset{*}{\Gamma}^{-1} = -i\Gamma i = -i \underline{a + bji} = a - bj$$

$$\frac{\bar{\sigma} \mid -j\bar{\sigma}}{-\varkappa i\bar{\sigma} \mid \varkappa j i\bar{\sigma}} \frac{a \mid b}{-b \mid \bar{a}} \frac{\sigma \mid \varkappa\sigma i}{\sigma j \mid \varkappa\sigma i j} = \frac{a + bj \mid 0}{0 \mid a + bj}$$

$$\Gamma \in \underset{\mathbb{K}_n}{\mathbb{K}} \Rightarrow \underline{\Gamma} = \frac{\Gamma \mid 0}{0 \mid \overset{*}{\Gamma}^{-1}} \Rightarrow \begin{cases} \overset{*}{\Gamma} = \frac{\Gamma \mid 0}{0 \mid \overset{*}{\Gamma}^{-1}} \\ \overset{*}{\Gamma}^{-1} = \frac{\overset{*}{\Gamma} \mid 0}{0 \mid \Gamma} \end{cases}$$