

$$\begin{cases} {}^n_{2\mathbb{K}_n}\mathbb{U} \\ {}^n_{1:1\mathbb{K}_n}\mathbb{U} \end{cases} = \begin{cases} \mathbb{J} \in {}^n_{2\mathbb{K}_n}\mathbb{C} & \mathbb{J} \frac{1 \mid 0}{0 \mid 1} \mathbb{J}^* = \frac{1 \mid 0}{0 \mid 1} \\ \mathbb{J} \in {}^n_{2\mathbb{K}_n}\mathbb{C} & \mathbb{J} \frac{1 \mid 0}{0 \mid -1} \mathbb{J}^* = \frac{1 \mid 0}{0 \mid -1} \end{cases}$$

$$\begin{cases} {}^n_{2\mathbb{R}_n}\mathbb{U} = {}^n_{2\mathbb{R}_n}\mathbb{C} \cap {}^n_{2\mathbb{C}_n}\mathbb{U} \\ {}^n_{2\mathbb{C}_n}\mathbb{U} = {}^n_{2\mathbb{C}_n}\mathbb{C} \cap {}^n_{2\mathbb{H}_n}\mathbb{U} \end{cases} \xrightarrow{\begin{array}{c} \frac{\pm \mid 0}{0 \mid \pm} \\ \frac{i \mid 0}{0 \mid i} \end{array}} \begin{cases} {}^n_{2\mathbb{C}_n}\mathbb{U} \\ {}^n_{2\mathbb{H}_n}\mathbb{U} \end{cases}$$

$$\begin{cases} {}^n_{1:1\mathbb{R}_n}\mathbb{U} = {}^n_{2\mathbb{R}_n}\mathbb{C} \cap {}^n_{1:1\mathbb{C}_n}\mathbb{U} \\ {}^n_{1:1\mathbb{C}_n}\mathbb{U} = {}^n_{2\mathbb{C}_n}\mathbb{C} \cap {}^n_{1:1\mathbb{H}_n}\mathbb{U} \end{cases} \xrightarrow{\begin{array}{c} \frac{\pm \mid 0}{0 \mid \pm} \\ \frac{i \mid 0}{0 \mid i} \end{array}} \begin{cases} {}^n_{1:1\mathbb{C}_n}\mathbb{U} \\ {}^n_{1:1\mathbb{H}_n}\mathbb{U} \end{cases}$$

$${}^n_{\mathbb{C}_n}\mathbb{U} = {}^n_{2\mathbb{R}_n}\mathbb{C} \cap {}^n_{\mathbb{H}_n}\mathbb{U} \xrightarrow{\frac{\pm \mid 0}{0 \mid \pm}} {}^n_{\mathbb{H}_n}\mathbb{U}$$

$$\left\{ \begin{array}{l} {}^n\mathbb{C}_n^{\mathbb{U}} \\ {}^n\mathbb{H}_n^{\mathbb{U}} \\ {}^n\mathbb{C}_n \end{array} \right. \xrightarrow{\begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \\ \hline 0 & \pm \\ \hline -\pm & 0 \end{array}} \left\{ \begin{array}{l} {}^n\mathbb{R}_n^{\mathbb{U}} \\ {}^n\mathbb{C}_n^{\mathbb{U}} \end{array} \right.$$

$$\begin{aligned} \Gamma \in {}^n\mathbb{C}_n^{\mathbb{U}} &\Rightarrow \Gamma \overset{*}{\Gamma} = 1 \xRightarrow{*_{\text{hom}}} \Gamma_{\mathbb{R}} \overset{*}{\Gamma}_{\mathbb{R}} = \underset{\mathbb{R}}{1} = \frac{1}{0} \Big| \frac{0}{1} \\ \Gamma \in {}^n\mathbb{H}_n^{\mathbb{U}} &\Rightarrow \Gamma \overset{*}{\Gamma} = 1 \xRightarrow{*_{\text{hom}}} \Gamma_{\mathbb{C}} \overset{*}{\Gamma}_{\mathbb{C}} = \underset{\mathbb{C}}{1} = \frac{1}{0} \Big| \frac{0}{1} \end{aligned}$$

$${}^n\mathbb{R}_{2n}^{\mathbb{U}} \xrightarrow{\begin{array}{c|c} 1 & 0 \\ \hline 0 & -1 \end{array}} {}^n\mathbb{C}_n^{\mathbb{U}}$$

$${}^n\mathbb{R}_n^{\mathbb{U}} = {}^n\mathbb{R}_n^{\mathbb{C}} \cap {}^n\mathbb{C}_n^{\mathbb{U}} \xrightarrow{\begin{array}{c|c} 1 & 0 \\ \hline 0 & -1 \end{array}} {}^n\mathbb{C}_n^{\mathbb{U}}$$

$${}^n\mathbb{C}_n^{\mathbb{U}} = {}^n\mathbb{C}_n^{\mathbb{C}} \cap {}^n\mathbb{H}_n^{\mathbb{U}} \xrightarrow{\begin{array}{c|c} 1 & 0 \\ \hline 0 & -1 \end{array}} {}^n\mathbb{H}_n^{\mathbb{U}}$$

$${}^n\mathbb{R}_{2n}^{\mathbb{U}} = {}^n\mathbb{R}_{2n}^{\mathbb{C}} \cap {}^n\mathbb{R}_{2n}^{\mathbb{C}} \xrightarrow{\begin{array}{c|c} 0 & 1 \\ \hline 1 & 0 \end{array}} {}^n\mathbb{R}_{2n}^{\mathbb{C}}$$

$$\bar{\sigma}\lambda + \bar{\mu}\nu = 0 \Rightarrow \frac{\bar{\sigma}}{\lambda} \Big| \frac{\bar{\mu}}{\bar{\nu}} \quad {}^n\mathbb{C}_{2n}^{\mathbb{C}} \quad \frac{\sigma}{\mu} \Big| \frac{\lambda}{\nu} = {}^n\mathbb{C}_{2n}^{\mathbb{C}}$$

$$\frac{\bar{\sigma}}{\lambda} \Big| \frac{\bar{\mu}}{\bar{\nu}} \quad \frac{a}{0} \Big| \frac{0}{a} \quad \frac{\sigma}{\mu} \Big| \frac{\lambda}{\nu} = \frac{a}{0} \Big| \frac{0}{a}$$

$$\sigma \in \mathbb{C}^U \Rightarrow \begin{cases} \frac{\kappa\bar{\sigma} \mid -\kappa j\bar{\sigma}}{-i\bar{\sigma} \mid j i\bar{\sigma}} \begin{matrix} n_{\mathbb{H}}^U \\ \mathbb{C}^n \end{matrix} \frac{\kappa\sigma \mid \sigma i}{\kappa\sigma j \mid \sigma i j} = \begin{matrix} n_{\mathbb{H}}^U \\ \mathbb{H}_*^n \end{matrix} \\ \begin{matrix} n_{\mathbb{H}}^U \\ \mathbb{C}^n \end{matrix} = \frac{\kappa\sigma \mid \sigma i}{\kappa\sigma j \mid \sigma i j} \begin{matrix} n_{\mathbb{H}}^U \\ \mathbb{H}_*^n \end{matrix} \frac{\kappa\bar{\sigma} \mid -\kappa j\bar{\sigma}}{-i\bar{\sigma} \mid j i\bar{\sigma}} \end{cases}$$

$$\frac{\kappa\bar{\sigma} \mid -\kappa j\bar{\sigma}}{-i\bar{\sigma} \mid j i\bar{\sigma}} \frac{a \mid b}{-b \mid \bar{a}} \frac{\kappa\sigma \mid \sigma i}{\kappa\sigma j \mid \sigma i j} = \frac{a + bj \mid 0}{0 \mid a + bj}$$

$$\Gamma = a + bj \in n_{\mathbb{H}_n}^U \Leftrightarrow \Gamma^{*-1} = \Gamma = a + bj$$

$$\frac{\bar{\sigma} \mid -\sigma i}{-i\bar{\sigma} \mid \sigma} \begin{matrix} n_{\mathbb{C}}^U \\ \mathbb{C}^n \end{matrix} \frac{\sigma \mid \sigma i}{i\bar{\sigma} \mid \bar{\sigma}} = \begin{matrix} n_{\mathbb{C}}^U \\ \mathbb{R}^n \end{matrix}$$

$$\Gamma \in n_{\mathbb{C}_n}^U \Rightarrow \bar{\Gamma} \in n_{\mathbb{C}_n}^U$$