

$$\underbrace{G_k - 2\zeta_k}_s = \frac{2(2\pi i)^k}{(k-1)!} \zeta_s \zeta_{s+1-k} = -\frac{2k}{B_k} \zeta_s \zeta_{s+1-k} \zeta_k$$