

$$\int_{dz/2\pi i}^{\overline{z-i} = \sqrt{2}} \frac{1}{z^2 - 2z + 3} = \frac{1}{2i\sqrt{2}}$$

$$z^2 - 2z + 3 = (z - a_+) (z - a_-) \Rightarrow {}^{a_+}\text{Res} \frac{1}{z^2 - 2z + 3}$$

$$\int_{dz/2\pi i}^{\overline{z} = r} \frac{z^\eta}{(z - a_1) \cdots (z - a_n)} = \sum_{1 \leq i \leq n} \overbrace{{}^{a_i}\text{Res} = {}^{a_i}\text{Ev} \frac{z^\eta}{\prod_{j \neq i} (z - a_j)}} = \sum_{1 \leq i \leq n} \frac{a_i^\eta}{\prod_{j \neq i} (a_i - a_j)}$$

$$\int_{dz/2\pi i}^{\overline{z} = 4} \frac{z^\eta}{(z - 1)(z - 2i)(z + 3)}$$

$$\int_{dz/2\pi i}^{\overline{z-1} = r} \frac{z^2}{(z + 1)(z - 1)^2} = \begin{cases} {}^{-1}\text{Res} = {}^{-1}\text{Ev} \frac{z^2}{(z - 1)^2} = \frac{1}{4} \\ {}^1\text{Res} = {}^1\text{Der} \frac{z^2}{(z + 1)} = \frac{3}{4} \end{cases} = 1$$

$$\int_{dz/2\pi i}^{\overline{z} = 1} \pi^z \mathbf{t}$$

$$z = e^{it}$$

$$\begin{cases} R(x:y) \text{ rational} \\ \text{no poles on } x^2 + y^2 = 1 \end{cases} \Rightarrow \int_{dt/2\pi}^{0|\pi} R(t_{\mathbf{c}}:t_{\mathbf{s}}) = \sum_{|\bar{z}| < 1} \text{Res} \frac{1}{z} R\left(\frac{z+z^{-1}}{2} : \frac{z-z^{-1}}{2i}\right)$$

$$z = e^{it} \Rightarrow \begin{cases} dz = izdt \\ t_{\mathbf{c}} = \frac{z+z^{-1}}{2} \\ t_{\mathbf{s}} = \frac{z-z^{-1}}{2i} \end{cases} \Rightarrow \text{LHS} = \frac{1}{2\pi i} \int_{|\bar{z}|=1} \frac{dz}{z} R\left(\frac{z+z^{-1}}{2} : \frac{z-z^{-1}}{2i}\right) = \text{RHS}$$

$$\int_{dt/2\pi}^{0|\pi} \begin{cases} \frac{1}{a+t_{\mathbf{s}}} = \begin{cases} \text{Res} \frac{2i}{z^2+2iaz-1} \frac{\text{Ev}}{\text{Der}} \frac{2i}{2z+2ia} \\ i\sqrt{a^2-1}-ia \end{cases} = \frac{1}{\sqrt{a^2-1}} \\ \frac{1}{2-t_{\mathbf{s}}} = \frac{1}{\sqrt{3}} \end{cases}$$

$$\int_{dt/\pi}^{0|\pi} \stackrel{\text{ev}}{=} \int_{dt/2\pi}^{0|\pi} \begin{cases} \frac{1}{a+t_{\mathbf{c}}} = \begin{cases} \text{Res} \frac{2}{z^2+2az+1} \frac{\text{Ev}}{\text{Der}} \frac{2}{2z+2a} \\ \pm(\sqrt{a^2-1}-a) \end{cases} \quad a \geq 1 \frac{1}{\sqrt{a^2-1}} \\ \frac{1}{3+2t_{\mathbf{c}}} = \frac{1}{\sqrt{5}} \\ \frac{1}{2+t_{\mathbf{c}}} \\ \frac{1}{5-3t_{\mathbf{c}}} \end{cases}$$

$$\int_{2dt/\pi}^{0|\pi/2} = \int_{dt/\pi}^{0|\pi} = \int_{dt/2\pi}^{0|\pi} \begin{cases} \frac{1}{a+t_{\mathbf{s}}^2} \\ \frac{a}{a^2+t_{\mathbf{s}}^2} = \frac{2a}{1+2a^2-t_{\mathbf{c}}} = \frac{1}{\sqrt{1+a^2}} \\ \frac{1}{1+t_{\mathbf{s}}^2} = \frac{1}{\sqrt{2}} \\ \frac{1}{2+t_{\mathbf{c}}^2} = \frac{1}{\sqrt{6}} \end{cases}$$

$$\int_{dt/2\pi}^{0|\pi} \frac{t_{\mathbf{s}}}{a+t_{\mathbf{s}}}$$

$$\int_{dt/2\pi}^{0|\pi} \frac{2t_{\mathbf{c}}}{5-4t_{\mathbf{c}}} \frac{2t_{\mathbf{c}}}{t_{\mathbf{c}}^2-t_{\mathbf{s}}^2} \text{Res} \frac{z^4+1}{-4z^2(z-1/2)(z-2)} = -\frac{1}{4} \begin{cases} {}^0\text{Der} \frac{z^4+1}{(z-1/2)(z-2)} = \frac{5}{2} \\ {}^{1/2}\text{Ev} \frac{z^4+1}{(z-2)z^2} = -\frac{17}{6} \end{cases} = \frac{1}{12}$$

$$\int_{dt/2\pi}^{0|\pi} e^{t\mathbf{c}} \underbrace{nt\mathbf{c} - t\mathfrak{f}}_{}$$

$$\int_{dt/2\pi}^{0|\pi} \frac{1}{1 + a^2 - 2a^t\mathbf{c}} = \begin{cases} \frac{1}{1 - a^2} & 0 < a < 1 \\ \frac{1}{a^2 - 1} & 1 < a \end{cases}$$

$$\int_{dt/2\pi}^{0|\pi} \left\{ \begin{array}{l} \frac{1}{(a + t\mathfrak{f})^2} = \text{Res} \left\{ \frac{-4z}{(z^2 + 2iaz - 1)^2} = \frac{-4z}{(z - a_+)^2 (z - a_-)^2} \right. \\ \left. \frac{1}{(b + a^t\mathbf{c})^2} = \frac{b}{(b^2 - a^2)^{3/2}} \right. \\ \frac{1}{(2 - t\mathfrak{f})^2} \\ \frac{1}{(1 + a^t\mathbf{c})^2} \end{array} \right. = {}^{a_+}\text{Der} \frac{-4z}{(z - a_-)^2} = \frac{a}{(a^2 - 1)^{3/2}}$$

$$\int_{2dt/\pi}^{0|\pi/2} \frac{1}{(a + t\mathfrak{f}^2)^2} = \frac{2a + 1}{2(a^2 + a)^{3/2}}$$

$$\overline{a} < 1: \int_{dt/\pi}^{0|\pi} \stackrel{\text{ev}}{=} \int_{dt/2\pi}^{0|\pi} \left\{ \frac{2t\mathbf{c}}{1 - 2a^t\mathbf{c} + a^2} \right. \\ \left. \frac{1}{1 - 2a^t\mathbf{c} + a^2} = \text{Res} \frac{z^n}{(z - a)(z - 1/a)} \right.$$

$$\int_{dt/2\pi}^{0|\pi} t\mathfrak{f}^{2k} = \frac{(2k)!}{4^k (k!)^2}$$