

$$\underline{\mathcal{P}}_p = \frac{x = \overset{*}{x} \in \Theta | \mathbb{1}}{px + xp = x}$$

$$\underline{\mathcal{P}}_p \ni x \Rightarrow \begin{cases} pxp = 0 \\ p \times \underline{p \times x} = x \end{cases}$$

$$px + xp = x \Rightarrow \begin{cases} pxp + xpp = xp \Rightarrow pxp = 0 \\ p \times \underline{p \times x} = x = p\underline{px - xp} - \underline{px - xp}p = px - pxp - pxp + xp = px + xp = x \end{cases}$$

$$\Theta | \mathbb{1} \xrightarrow{ip \times} \underline{\mathcal{P}}_p$$

$$y = \overset{*}{y} \Rightarrow ip \times y \in \underline{\mathcal{P}}_p$$

$$\widehat{ip \times y}^* = -iy \times p = ip \times y$$

$$\underline{p \times y}p + p\underline{p \times y} = \underline{py - yp}p + p\underline{py - yp} = pyp - ypp + ppy - pyp = py - yp \in i\underline{\mathcal{P}}_p$$

$$\begin{array}{ccccc} \underline{\mathcal{P}}_p & \xrightarrow{ip \times} & \underline{\mathcal{P}}_p & \xrightarrow{ip \times} & \underline{\mathcal{P}}_p \\ & \searrow & & \nearrow & \\ & & -\iota & & \end{array}$$

$$ip \times \underline{ip \times x} = -p \times \underline{p \times x} = -x$$

$$x \in \underline{\mathcal{P}}_p$$

$$\underline{\mathfrak{d}_x \mathfrak{b}}_p = \underline{q \times \widehat{p \times x} \times \mathfrak{b}_q}_p$$

$$\underline{\mathfrak{d}_{ip \times x} \mathfrak{b}}_p = \underline{i \widehat{q \times x} \times \mathfrak{b}_q}_p$$

$$\iota_K = \begin{array}{c|c} 1_K & 0 \\ \hline 0 & 0_{K^\perp} \end{array}$$

$$\underline{\mathcal{P}}_K = \begin{array}{c|c} K \blacktriangleright H \times_{\mathbb{U}|K} 0 & K \blacktriangleleft K^\perp \\ \hline K \overset{*}{\blacktriangleleft} K^\perp & 0 \end{array}$$

$$\mathcal{T} = {^K\blacktriangleleft}_{H_{\mathbb{U}|K}} K = \begin{cases} p{:}\top \in \mathcal{P} \times \mathbb{1} \\ p\top = \top \end{cases}$$

$$\mathcal{T} \leftarrow \mathbb{U}|\mathbb{1} \bowtie \mathcal{T}$$

$$g \bowtie \underline{p{:}\top} = \bigl(gp\ddot{g}{:}g\top\bigr)$$

$$p\top = \top \Rightarrow \underline{gp\ddot{g}}\,\underline{g\top} = \underline{gp}\,\underline{\dot{g}g\top} = \underline{gp}\top = g\underline{p\top} = g\top \Rightarrow \bigl(gp\ddot{g}{:}g\top\bigr) \in \mathcal{T}$$