

$$\mathbb{R} \ni \underline{\nu} \xrightarrow[\text{diff}]{} \mathbb{R} \Rightarrow \begin{cases} \underline{\nu} > 0 \Rightarrow \nu \text{ streng isoton} & \underline{\nu} \geq 0 \Rightarrow \nu \text{ isoton} \\ \underline{\nu} = 0 \Rightarrow \nu \text{ constant} & \\ \underline{\nu} \leq 0 \Rightarrow \nu \text{ antiton} & \underline{\nu} < 0 \Rightarrow \nu \text{ streng antiton} \end{cases}$$

$$x < y \in \mathbb{I} \xrightarrow[\text{MWS}]{} \bigvee_{x < o < y} {}^y\nu - {}^x\nu = \underbrace{y-x}_{>0} {}^o\nu$$

$$\begin{cases} {}^o\underline{\nu} > 0 \Rightarrow {}^y\nu - {}^x\nu > 0 \Rightarrow {}^y\nu > {}^x\nu & {}^o\underline{\nu} \geq 0 \Rightarrow {}^y\nu - {}^x\nu \geq 0 \Rightarrow {}^y\nu \geq {}^x\nu \\ {}^o\underline{\nu} = 0 \Rightarrow {}^y\nu - {}^x\nu = 0 \Rightarrow {}^y\nu = {}^x\nu & \\ {}^o\underline{\nu} \leq 0 \Rightarrow {}^y\nu - {}^x\nu \leq 0 \Rightarrow {}^y\nu \leq {}^x\nu & {}^o\underline{\nu} < 0 \Rightarrow {}^y\nu - {}^x\nu < 0 \Rightarrow {}^y\nu < {}^x\nu \end{cases}$$