

$$\begin{cases} X \times Y \xrightarrow{\eta} \bar{\mathbb{R}}_+ \\ Y \xrightarrow{x\eta} \bar{\mathbb{R}}_+^x \eta = |^x \eta| \end{cases} \Rightarrow \begin{cases} X \xrightarrow{\eta} \mathbb{R} \\ |\eta| \leqslant |\eta| \end{cases}$$

$$\begin{aligned} & \left\{ \begin{array}{l} \eta \leqslant \sum_k \eta^k \\ \eta^k \in X \times Y \xrightarrow{0} \mathbb{R}_+ \end{array} \right. \Rightarrow \left\{ \begin{array}{l} {}^x \eta_{\cdot} \leqslant \sum_k {}^x \eta_{\cdot}^k \\ {}^x \eta_{\cdot}^k \in Y \xrightarrow{0} \mathbb{R}_+ \end{array} \right. \\ & {}^x \eta^k = \int_{dy}^Y {}^x \eta_y^k = \int_{dy}^Y {}^x \eta_y^k \Rightarrow \frac{\eta^k \in X \xrightarrow{0} \mathbb{R}_+}{{}^x \eta = |^x \eta| \leqslant \sum_k \int_{dy} {}^x \eta_y^k = \sum_k {}^x \eta^k} \\ & \Rightarrow |\eta| \leqslant \sum_k \int_{dx} {}^x \eta^k = \sum_k \int_{dx} \int_{dy} {}^x \eta_y^k = \sum_k \int_{dxdy} {}^x \eta^k \Rightarrow |\eta| \leqslant |\eta| \end{aligned}$$

$$\mathbb{H}_{\frac{1}{m}} \mathbb{K} \boxtimes \mathbb{H}_{\frac{1}{m}} \mathbb{K} \xleftarrow{\exists} \mathbb{H} \times \mathbb{H}_{\frac{1}{m}} \mathbb{K} \xleftarrow{\exists} \mathbb{H}_{\frac{1}{m}} \mathbb{H}_{\frac{1}{m}} \mathbb{K}$$

$$\int_{d(u \times v)(x:y)}^{\mathbb{H} \times \mathbb{H}} {}^x \eta {}^y \eta' = \int_{du(x)}^{\mathbb{H}} {}^x \eta \int_{dv(y)}^{\mathbb{H}} {}^y \eta'$$

$$\int_{\mathbb{H} \times \mathbb{H}} \eta = \int_{\mathbb{H}_h}^{\mathbb{H}} \int_{\mathbb{H}_h}^{\mathbb{H}} {}^{h:h} \eta = \int_{\mathbb{H}_h}^{\mathbb{H}} \int_{\mathbb{H}_h}^{\mathbb{H}} {}^{h:h} \eta$$

$$\eta \in X \times Y \xrightarrow{\frac{1}{m}} \mathbb{1}$$

$$X_0 = \frac{x \in X}{{}^x \eta_{\cdot} \in Y \xrightarrow{\frac{1}{m}} \mathbb{1}}$$

$$X \xrightarrow{\eta} \mathbb{1}$$

$$\bigwedge_{x \in X_0} {}^x\gamma = \int\limits_{dy}^Y {}^x\gamma_\cdot = \int\limits_{dy}^Y {}^x\gamma_y$$

$$\stackrel{\text{FUB}}{\Rightarrow} |\chi_{X \llcorner X_0}| = 0$$

$$\gamma \in X \mathop{\triangleleft}\limits_m^1 \mathbb{1}$$

$$\int\limits_{dx}^X \gamma = \int\limits_{dxdy}^{X \times Y} \gamma$$

$$\bigvee \gamma^j \in {}^{X \times Y} \mathop{\triangleleft}\limits_m^1 \mathbb{1} || \gamma - \gamma^j || \leqslant 2^{-j}$$

$${}^x\alpha^j = \overline{{}^x\gamma_\cdot - {}^x\gamma^j} = |{}^x\gamma_\cdot - {}^x\gamma^j| = |{}^x\gamma_\cdot - \gamma^j| \in \mathbb{R}_+ \stackrel{\text{Lem}}{\Rightarrow} |\alpha^j| \leqslant |\gamma - \gamma^j| = \overline{|\gamma - \gamma^j|}$$

$$X_1 = \frac{x \in X}{{}^x\alpha^j \rightsquigarrow 0} \Rightarrow |\chi_{X \llcorner X_1}| = 0$$

$$\bigwedge_{0 \leqslant k} \bigwedge_{x \in X} {}^x\chi_{X \llcorner X_1} \leqslant \sum_{j \geqslant k} {}^x\alpha^j$$

$$\sum_{j \geqslant k} {}^x\alpha^j \stackrel{\text{OE}}{\leqslant} \infty \Rightarrow {}^x\alpha^j \rightsquigarrow 0 \Rightarrow x \in X \Rightarrow {}^x\chi_{X \llcorner X_1} = 0$$

$$|\chi_{X \llcorner X_1}| \leqslant \sum_{j \geqslant k} |\alpha^j| \leqslant \sum_{j \geqslant k} 2^{-j} = 2^{-k} \rightsquigarrow 0 \Rightarrow |\chi_{X \llcorner X_1}| = 0$$

$$\bigwedge_{x \in X_1} {}^x\gamma^j \in {}^{Y \mathop{\triangleleft}\limits_m^1} \mathbb{1} \Rightarrow || {}^x\gamma_\cdot - {}^x\gamma^j || = {}^x\alpha^j \rightsquigarrow 0 \Rightarrow {}^x\gamma_\cdot \in {}^{Y \mathop{\triangleleft}\limits_m^1} \mathbb{1} \Rightarrow x \in X_0 \Rightarrow X_1 \subset X_0 \Rightarrow$$

$${}^x\chi_{X \llcorner X_0} \leqslant {}^x\chi_{X \llcorner X_1} \Rightarrow |{}^x\chi_{X \llcorner X_1}| \geqslant |{}^x\chi_{X \llcorner X_0}| = 0$$

$${}^x\gamma^j = \int\limits_{dy}^Y {}^x\gamma^j_\cdot = \int\limits_{dy}^Y {}^x\gamma^j_y \Rightarrow \gamma^j \in X \mathop{\triangleleft}\limits_0^0 \mathbb{1}$$

$$\overline{\gamma - \gamma^j} \leqslant \gamma^i + \sum_{k \geqslant 0} \chi_{X \sqcup X_0}$$

$$\sum_{0 \leqslant k} {}^x \chi_{X \sqcup X_0} \stackrel{\text{OE}}{\leqslant} \infty \Rightarrow x \in X_0 \Rightarrow \overline{{}^x \gamma - {}^x \gamma^j} = \overline{\int_{dx}^X {}^x \gamma_{\cdot} - \int_{dx}^X {}^x \gamma_{\cdot}^j} = \overline{\int_{dx}^X {}^x \gamma_{\cdot} - \overline{{}^x \gamma_{\cdot}}}$$

$$\leqslant \int_{dx}^X \overline{{}^x \gamma_{\cdot} - {}^x \gamma_{\cdot}^j} = | \overline{{}^x \gamma_{\cdot} - {}^x \gamma_{\cdot}^j} | = \| {}^x \gamma_{\cdot} - {}^x \gamma_{\cdot}^j \| = {}^x \gamma^i \leqslant \text{RHS}$$

$$\Rightarrow \overline{\gamma - \gamma^j} = | \overline{\gamma - \gamma^j} | \leqslant | \gamma^i | + \sum_{0 \leqslant k} | {}^x \chi_{X \sqcup X_0} | = | \gamma^i | \rightsquigarrow 0 \Rightarrow \gamma \in \overset{X}{\bigtriangleup_m^1} \mathbb{1} \underset{\text{Def}}{\Rightarrow}$$

$$\mathbb{1} \ni \int_{dx}^X \gamma_{\cdot} \rightsquigarrow \int_{dx}^X \gamma^j = \int_{dxdy}^{X \times Y} \gamma^j \rightsquigarrow \int_{dxdy}^{X \times Y} \gamma_{\cdot} \Rightarrow \int_{dx}^X \gamma_{\cdot} = \int_{dxdy}^{X \times Y} \gamma_{\cdot}$$