

$$\underline{\mathbb{L}:\mathbb{N}}\rtimes \underline{\mathbb{L}:\mathbb{L}}=\underline{\mathbb{L}\;\mathbb{L}}+\underline{\mathbb{L}:\bar{\mathbb{L}}^1\ltimes \mathbb{N}}={^\mathbb{L}\mathfrak{N}}:\mathbb{N}_{\mathsf{q}}$$

$$\overbrace{\mathbb{L}\rtimes \mathbb{L}}^{\nu} = \mathbb{L}^{\mu}{}_{\mu}\mathbb{L}^{\nu}$$

$$\underbrace{\mathbb{L}^A}_{\mathsf{N}}={}^A\!\mathbb{L}_B{}^{j^B}$$

$$\det {}^x\! \mathfrak{N}=\det \mathbb{L}=1$$

$$\partial_\nu \underbrace{\mathbb{N}^A}_{\mathsf{N}}=0$$

$$\frac{\partial \mathbb{N}^A}{\partial \mathbb{N}^{j^B}}={}^A\!\mathbb{L}_B$$

Poincare invariance ${}^L\mathcal{L}_{\mathbf{N}, \mathbf{N}} = {}^{L \times L + L} \mathcal{L}_{A \bar{\mathbf{l}}_B^{-1} \bar{\mathbf{l}}_{\mu}^{jB} \bar{\mathbf{l}}_{\nu}^{jB} A \bar{\mathbf{l}}_B^{-1} \bar{\mathbf{l}}_{\nu}^{jB}}$

$$L \times L^\nu = L^\mu {}_\mu L^\nu$$

$$\underline{L} \underline{L} \times \underline{L}^\nu = \underline{L} \underline{L} \times L^\nu = \underline{L} \times \underline{L}^\nu = L^\mu {}_\mu L^\nu = \underline{L} \underline{L}^\mu {}_\mu L^\nu = \underline{L} \underline{L}^\mu {}_\mu L^\nu$$

$$\underline{L} \times \underline{L}^\mu {}_\mu \bar{\mathbf{l}}^\nu = L^\nu$$

$$\text{LHS} = \underbrace{L^\lambda {}_\lambda L^\mu} {}_{= \delta^\nu} {}_\mu \bar{\mathbf{l}}^\nu = L^\lambda \underbrace{L^\mu {}_\mu \bar{\mathbf{l}}^\nu} {}_{= \delta^\nu} = L^\nu$$

$$\begin{aligned} & \overline{A \bar{\mathbf{l}}_B^{-1} \mathbf{N} \frac{iA}{-1}} {}^A \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} = \mathbf{N}^{jB_*} {}^A \bar{\mathbf{l}}_B^{-1} \frac{iA}{-1} {}^A \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} \stackrel{\text{ev}}{=} \mathbf{N}^{jB_*} \frac{jB}{-1} {}^A \bar{\mathbf{l}}_B^{-1} {}^A \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} \stackrel{\text{unit}}{=} \mathbf{N}^{jB_*} \frac{jB}{-1} {}^B \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} \\ & = \mathbf{N}^{jB_*} \frac{jB}{-1} {}^B \underbrace{\underline{L} \underline{L}^\mu \bar{\mathbf{l}}^\nu} {}_D {}_\mu \bar{\mathbf{l}}^\nu {}_\nu \mathbf{N} = \mathbf{N}^{jB_*} \frac{jB}{-1} {}^B \underbrace{\underline{L} \times \underline{L}^\mu} {}_D {}_\mu \bar{\mathbf{l}}^\nu {}_\nu \mathbf{N} = \mathbf{N}^{jB_*} \frac{jB}{-1} {}^B \bar{\mathbf{l}}_D^\nu {}_\nu \mathbf{N} \\ & \overline{A \bar{\mathbf{l}}_B^{-1} \mathbf{N} \frac{iA}{-1}} {}^A \bar{\mathbf{l}}_D^\nu \mathbf{N} = \mathbf{N}^{jB_*} {}^A \bar{\mathbf{l}}_B^{-1} \frac{iA}{-1} {}^A \bar{\mathbf{l}}_D^\nu \mathbf{N} \stackrel{\text{ev}}{=} \mathbf{N}^{jB_*} \frac{jB}{-1} {}^A \bar{\mathbf{l}}_B^{-1} {}^A \bar{\mathbf{l}}_D^\nu \mathbf{N} \stackrel{\text{unit}}{=} \mathbf{N}^{jB_*} \frac{jB}{-1} \underbrace{\bar{\mathbf{l}}_A {}^A \bar{\mathbf{l}}_D^\nu} {}_{= {}^B \delta_D} \mathbf{N} = \mathbf{N}^{jB_*} \frac{jB}{-1} {}^j B \mathbf{N} \\ \text{RHS} & = \overline{A \bar{\mathbf{l}}_B^{-1} \mathbf{N} \frac{iA}{-1}} \underbrace{{}^A \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} - m {}^A \bar{\mathbf{l}}_D^\nu \mathbf{N}} = \overline{A \bar{\mathbf{l}}_B^{-1} \mathbf{N} \frac{iA}{-1}} {}^A \bar{\mathbf{l}}_C^\mu {}_\mu \bar{\mathbf{l}}^\nu {}^C \bar{\mathbf{l}}_D^\nu \mathbf{N} - m \overline{A \bar{\mathbf{l}}_B^{-1} \mathbf{N} \frac{iA}{-1}} {}^A \bar{\mathbf{l}}_D^\nu \mathbf{N} \\ & = \mathbf{N}^{jB_*} \frac{jB}{-1} {}^B \bar{\mathbf{l}}_D^\nu {}_\nu \mathbf{N} - m \mathbf{N}^{jB_*} \frac{jB}{-1} {}^j B \mathbf{N} = \mathbf{N}^{jB_*} \frac{jB}{-1} \underbrace{{}^B \bar{\mathbf{l}}_D^\mu \mathbf{N} - m {}^j B \mathbf{N}} = \text{LHS} \end{aligned}$$