

$\mathbb{K}\underbrace{\mathcal{L} \times \mathcal{L}}_{\mathcal{L} \in \mathcal{L}: \quad \mathbf{1} \in \mathcal{L}}$  = free K-vector space basis

$$\mathbb{K}\underbrace{\mathcal{L} \times \mathcal{L}}_{\mathcal{L} \in \mathcal{L}} = \mathbb{K}\underbrace{\mathcal{L} \times \mathcal{L}}_{\mathcal{L} \in \mathcal{L}} \cap \mathbb{K} \left\{ \underbrace{\alpha \mathcal{L} + \dot{\alpha} \mathcal{L}}_{\mathcal{L} \in \mathcal{L}} : \mathbf{1} - \alpha \mathcal{L} : \mathbf{1} - \dot{\alpha} \mathcal{L} : \mathbf{1} \right\} = \mathbb{K} \left\{ \underbrace{\alpha \mathcal{L} + \dot{\alpha} \mathcal{L}}_{\mathcal{L} \in \mathcal{L}} : \mathbf{1} - \alpha \mathcal{L} : \mathbf{1} - \dot{\alpha} \mathcal{L} : \mathbf{1} \right\}$$

