

$$x=\left[\begin{smallmatrix} t \\ \xi & \eta \end{smallmatrix}\right]\left.\begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array}\right]\left[\begin{smallmatrix} \xi \\ \eta \end{smallmatrix}\right]=\xi^t\eta-\eta^t\xi$$

$$x\mathbin{\overline{\times}} x = \frac{1}{2} \operatorname{tr} x\mathbin{\dot{\times}} x = \frac{1}{2} \operatorname{tr} \underbrace{\xi^t\eta}_{\xi^t\eta} - \underbrace{\eta^t\xi}_{\eta^t\xi} - \underbrace{\xi^*\bar{\eta}}_{\xi^*\bar{\eta}} - \underbrace{\bar{\xi}\eta^*}_{\bar{\xi}\eta^*} = \xi\xi^*\eta\eta^* - \xi\eta^*\eta\xi^* = \det\begin{bmatrix} \xi \\ \eta \end{bmatrix} \begin{bmatrix} * & * \\ \xi & \eta \end{bmatrix}$$

$$y=\left[\begin{smallmatrix} t \\ \sigma & \tau \end{smallmatrix}\right]\left.\begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array}\right]\left[\begin{smallmatrix} \sigma \\ \tau \end{smallmatrix}\right]=\sigma^t\tau-\tau^t\sigma$$

$$c=\left[\begin{smallmatrix} t \\ \alpha & \beta \end{smallmatrix}\right]\left.\begin{array}{c|c} 0 & 1 \\ -1 & 0 \end{array}\right]\left[\begin{smallmatrix} \alpha \\ \beta \end{smallmatrix}\right]=\alpha^t\beta-\beta^t\alpha$$

$$x\mathbin{\overline{\times}} c = \frac{1}{2} \operatorname{tr} x\mathbin{\dot{\times}} c = \frac{1}{2} \operatorname{tr} \underbrace{\xi^t\eta}_{\xi^t\eta} \underbrace{\beta^*\bar{\alpha}-\alpha^*\bar{\beta}}_{\beta^*\bar{\alpha}-\alpha^*\bar{\beta}} = \xi\alpha^*\eta\beta^* - \xi\beta^*\eta\alpha^* = \det\begin{bmatrix} \xi \\ \eta \end{bmatrix} \begin{bmatrix} * & * \\ \alpha & \beta \end{bmatrix}$$

$$y\mathbin{\overline{\times}} c = \frac{1}{2} \operatorname{tr} y\mathbin{\dot{\times}} c = \frac{1}{2} \operatorname{tr} \underbrace{\sigma^t\tau}_{\sigma^t\tau} \underbrace{\beta^*\bar{\alpha}-\alpha^*\bar{\beta}}_{\beta^*\bar{\alpha}-\alpha^*\bar{\beta}} = \sigma\alpha^*\tau\beta^* - \sigma\beta^*\tau\alpha^* = \det\begin{bmatrix} \sigma \\ \tau \end{bmatrix} \begin{bmatrix} * & * \\ \alpha & \beta \end{bmatrix}$$

$$x\mathbin{\overline{\times}} y = \frac{1}{2} \operatorname{tr} x\mathbin{\dot{\times}} y = \frac{1}{2} \operatorname{tr} \underbrace{\xi^t\eta}_{\xi^t\eta} \underbrace{\tau^*\bar{\sigma}-\sigma^*\bar{\tau}}_{\tau^*\bar{\sigma}-\sigma^*\bar{\tau}} = \xi\sigma^*\eta\tau^* - \xi\tau^*\eta\sigma^* = \det\begin{bmatrix} \xi \\ \eta \end{bmatrix} \begin{bmatrix} * & * \\ \sigma & \tau \end{bmatrix}$$

$$x\mathbin{\overline{\times}} c = \overbrace{\xi\alpha^*\eta\beta^* - \xi\beta^*\eta\alpha^*}^m = \int\limits_{d\sigma}^{\mathbb{C}_n\sqcup 0} \int\limits_{d\tau}^{\mathbb{C}_n\sqcup 0} \mathfrak{e}^{-\sigma\sigma^*-\tau\tau^*} \mathfrak{e}^{\xi\sigma^*+\eta\tau^*} \overbrace{\sigma\alpha^*\tau\beta^* - \sigma\beta^*\tau\alpha^*}^m$$

$$= \int\limits_{d\varphi:\psi}^{\mathbb{S}^{4n-1}} \int\limits_{dr}^{\mathbb{R}^>} r^{4n-1} \mathfrak{e}^{-\sigma\sigma^*-\tau\tau^*} \mathfrak{e}^{\xi\sigma^*+\eta\tau^*} \overbrace{\sigma\alpha^*\tau\beta^* - \sigma\beta^*\tau\alpha^*}^m$$

$$= \int\limits_{d\sigma}^{\mathbb{C}^n} \int\limits_{d\tau}^{\mathbb{C}^n} \mathfrak{e}^{-\sigma\sigma^*} \mathfrak{e}^{-\tau\tau^*} \mathfrak{e}^{\xi\sigma^*} \mathfrak{e}^{\eta\tau^*} w\mathbin{\overline{\times}} c$$

$${}^zE_w^{\mathbb{H}} = \int\limits_{d\vartheta}^{U(\mathbb{H})} \mathfrak{e}^{\xi\sigma^* + \eta\tau^*}$$