$$\mathcal{U} | L_{\infty}^2 C = L_{\infty}^2 C \times \overbrace{L_{\infty}^2 C}^{\mathbb{H}}$$