

$$\hbar: \underline{\mathfrak{q}^N} \in \mathbb{R} \triangleleft$$

$n\mathbb{R}_{\mathbb{C}}^n$  structure

$$\begin{array}{ccc}
 \hbar & \hbar & \hbar \\
 \downarrow & \nearrow & \downarrow \\
 \underline{\mathfrak{q}^N} & & \int \underline{\mathfrak{q}^N} \\
 \hbar & & \hbar \\
 \hbar \triangleleft \mathbb{R} & & \int \underline{\mathfrak{q}^N} \\
 \end{array}$$

$$\text{Trg } \Psi \in \mathfrak{h} \Rightarrow \int_{\underline{\mathfrak{q}^N}}^{\hbar} \Psi = \int_{\underline{\mathbb{L}^N}}^{\hbar} \underline{\mathfrak{u}} \times \Psi = \int_{\underline{\mathbb{L}^N}}^{\hbar} \underline{\mathfrak{u}}$$

$$\text{Trg } \Psi \in \mathfrak{h} \cap \tilde{\mathfrak{h}} \Rightarrow \int_{\underline{\mathfrak{q}^N}}^{\hbar \cap \tilde{\mathfrak{h}}} \underline{\mathfrak{u}} \times \Psi = \int_{\underline{\mathbb{L}^N}}^{\hbar \cap \tilde{\mathfrak{h}}} \underline{\mathfrak{u}} \times \Psi$$

$$\text{LHS} = \int_{\underline{\mathbb{L}^N}}^{\hbar \cap \tilde{\mathfrak{h}}} \underline{\mathfrak{u}} \times \widehat{\underline{\mathfrak{u}} \times \Psi} = \det \underline{\mathfrak{u}} \int_{\underline{\mathfrak{q}^N}}^{\hbar \cap \tilde{\mathfrak{h}}} \underline{\mathfrak{u}} \times \Psi = \text{RHS}$$

$$\text{cpt Trg } \Psi \in \mathfrak{h} \Rightarrow \int_{\underline{\mathfrak{q}^N}}^{\hbar} \Psi = \sum_{\alpha}^{\text{fin}} \int_{\underline{\mathfrak{q}^N}}^{\hbar} \Psi u_{\alpha}$$

$u_{\alpha} \prec \hbar_{\alpha}$  lic fin atlas

$$\sum_{\alpha} u_{\alpha} = 1 \text{ part of unity}$$