

$$Q \times \underline{Q} \ni q: \dot{q} = q^\alpha: \dot{q}^\alpha$$

tangent functions $\mathbb{R} \times Q \times \underline{Q} \xrightarrow{\mathcal{F}} \mathbb{R} \ni {}^t\mathcal{F}_{q: \dot{q}}$

$$Q \times \underline{Q}^\sharp \ni q: q = q^\alpha: {}_\alpha q$$

cotangent functions $Q \times \underline{Q}^\sharp \xrightarrow{\mathcal{J}} \mathbb{R} \ni {}_{q: q} \mathcal{J}$

$$\mathcal{J} \times \dot{\mathcal{J}} = \underline{\partial}^t \mathcal{J} \underline{\partial}_t \dot{\mathcal{J}} - \underline{\partial}^t \dot{\mathcal{J}} \underline{\partial}_t \mathcal{J} \text{ Poisson}$$

$${}_\beta q \in \mathbb{R} \xleftarrow{{}_\beta \dot{()}} Q \times \underline{Q}^\sharp \xrightarrow{()^\alpha} \mathbb{R} \ni q^\alpha$$

$${}_\beta \dot{()} \times ()^\alpha = {}_\beta \delta^\alpha$$

Lagrangian $\mathbb{R} \times Q \times \underline{Q} \xrightarrow{\mathcal{L}} \mathbb{R} \ni {}^t\mathcal{L}_{q: \dot{q}}$