

$$\text{dof } \mathcal{U}^\mu : \mathcal{U}^\mu \in \mathbb{R}^d \times \mathbb{R}^d$$

$$\mathcal{U}^\mu : \mathcal{U}^\mu \in \mathbb{R}^d \times \mathbb{R}^d \xrightarrow[\text{Lagrangian}]{\mathcal{L}} \mathbb{R} \ni {}^t\mathcal{L}_{\mathcal{U}}$$

$${}^t\mathcal{L}_{\mathcal{U}}^{g:A} = {}_{\mu\nu}g \mathcal{U}^\mu \mathcal{U}^\nu + q_\mu A \mathcal{U}^\mu$$

$$\boxed{x: \begin{matrix} e \\ X^\mu \\ 0 \end{matrix} : \begin{matrix} {}_0e \\ {}_0X^\mu \end{matrix}} = \begin{cases} e^{-1} {}_0X^\mu X g_{\mu\nu 0} X^\nu - em^2 \\ e^{-1} {}_0X^\mu X g_{\mu\nu 0} X^\nu \end{cases} \quad m=0$$

symmetries

$$\text{local } \begin{cases} \overline{\mathfrak{b} \times X}^\nu = \mathfrak{b} \dot{X}^\nu \\ \mathfrak{b} \times e = \widehat{\mathfrak{b} e} \end{cases}$$

motion

$$\begin{cases} \ddot{X}^\mu = 0 \\ \dot{X}^\mu g_{\mu\nu} \dot{X}^\nu + e^2 m^2 = 0 \end{cases}$$