

$$\mathcal{Q}^{\curvearrowright}_{t_0}$$

$$t|\dot{t}^{\#}\lrcorner Q=\exp\left(\underline{t-\dot{t}}\overline{\mathcal{H}+\mathcal{V}}\right)$$

$$t|\dot{t}^{\#}\lrcorner Q=\stackrel{P}{\left(\exp\left(\underline{t-\dot{t}}\overline{\mathcal{H}+\mathcal{V}}\right)\right)}_{\dot{P}}$$

$$\begin{aligned} \stackrel{P}{\overbrace{e^{-t\Delta/2+\mathcal{V}}}\gamma}&= \int\limits_{d\dot{P}}^Q \dot{P}\gamma \int\limits_{d\mathbb{P}}^{\stackrel{P:\dot{P}}{-t/2|t/2}\lrcorner Q} \exp-\int\limits_{\underline{\mathbb{P}}}^{-t/2|t/2} \mathcal{L}_{\mathbb{P}} \exp\left(-\int\limits_{d\tau}^{-t/2|t/2} \mathcal{V}\left({}^{\tau}\mathbb{P}\right)\right) \\ &= \int\limits_{d\dot{P}}^Q \dot{P}\gamma \int\limits_{dW(\mathbb{P})}^{\stackrel{P:\dot{P}}{-t/2|t/2}\lrcorner Q} \exp\left(-\int\limits_{d\tau}^{-t/2|t/2} \mathcal{V}\left({}^{\tau}\mathbb{P}\right)\right) \end{aligned}$$

$$|t\dot{t}|^{\#}\lrcorner Q=\text{tr}\,\exp\left(\underline{t-\dot{t}}\overline{\mathcal{H}+\mathcal{V}}\right)$$

$$\begin{aligned} \text{RHS} &= \int\limits_Q^{dP} \stackrel{P}{e^{\underline{t-\dot{t}}\overline{\mathcal{H}+\mathcal{V}}}} = \int\limits_Q^{dP} \int\limits_{d\mathbb{P}}^{\stackrel{t|\dot{t}}{P:P}\lrcorner Q} \exp\left(\frac{i}{1/2}\int\limits^{|t\dot{t}|} \mathcal{L}_{\mathbb{P}}\right) \\ &= \int\limits_{d\mathbb{P}}^{|t\dot{t}|\lrcorner Q} \exp\left(\int\limits^{|t\dot{t}|} \mathcal{L}_{\mathbb{P}}\right) = |t\dot{t}|^{\#}\lrcorner Q = \int\limits_{d\mathbb{P}}^{|t\dot{t}|\lrcorner Q} \exp\left(\int\limits_{\underline{\mathbb{P}}}^{|t\dot{t}|} \mathcal{L}_{\mathbb{P}}\right) \exp\left(\int\limits^{|t\dot{t}|} \mathcal{V}(\mathbb{P})\right) \end{aligned}$$

$$\text{tr}\,\,e^{\beta\overline{\mathcal{H}+\mathcal{V}}}=\int\limits_Q^{dP} \stackrel{P}{e^{\beta\overline{\mathcal{H}+\mathcal{V}}}}=\int\limits_{d\mathbb{P}}^{|0\beta|\lrcorner Q} \exp\left(\int\limits_{\underline{\mathbb{P}}}^{|0\beta|} \mathcal{L}_{\mathbb{P}}\right) \exp\left(\int\limits^{|0\beta|} \mathcal{V}(\mathbb{P})\right)$$