

$$\sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \Gamma^{\mathbb{J}} \underset{\text{Poiss}}{=} \sum_{\Gamma}^{\frac{2\pi i \mathbb{Z}}{d}} \Gamma^{\sharp} = \sum_{\Gamma}^{\frac{2\pi i \mathbb{Z}}{d}} \int_{\mathbb{R}}^{\mathbb{R}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}} = \sum_{\mathbb{J}}^{\mathbb{Z}_d} \int_{\mathbb{R}}^{\mathbb{R}} 2\pi i \mathbb{J}^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}}$$

$$\begin{aligned}
\mathbf{\Gamma}^{\mathbb{J}} &= \sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \Gamma^{\mathbb{J} + \mathbb{J}} \underset{\text{per}}{\Rightarrow} \mathbf{\Gamma}^{\mathbb{J}} = \sum_{\Gamma}^{\frac{2\pi i \mathbb{Z}}{d}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}} \\
\Gamma^{\sharp} &= \int_{\mathbb{J}}^{\mathbb{I}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}} = \int_{\mathbb{J}}^{\mathbb{I}} \Gamma^{\mathbb{d}} \sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \Gamma^{\mathbb{J} + \mathbb{J}} = \sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \int_{\mathbb{J}}^{\mathbb{I}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d} + \mathbb{J}}} \\
&= \sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \int_{\mathbb{J}}^{\mathbb{I}} \Gamma^{\mathbb{J} + \mathbb{J}} \mathbf{e}^{\Gamma^{\mathbb{d} + \mathbb{J}}} = \sum_{\mathbb{J}}^{d_{\mathbb{Z}}} \int_{\mathbb{d}}^{\mathbb{J} + \mathbb{I}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}} = \int_{\mathbb{d}}^{\mathbb{R}} \Gamma^{\mathbb{d}} \mathbf{e}^{\Gamma^{\mathbb{d}}} \\
&\Rightarrow \text{LHS} = \mathbf{\Gamma}^0 = \sum_{\Gamma}^{\frac{2\pi i \mathbb{Z}}{d}} \Gamma^{\sharp} = \text{RHS}
\end{aligned}$$