

$$x={}^{i\tau}\mathfrak{e}$$

$$\begin{aligned}{}^xX^\mu &= \sum_n^{\mathbb{N}} \underbrace{{}_{\stackrel{n}{\otimes_m}}\iota_m}_<\!\!\!{}^xX_n^\mu\!\!\!{}_{\otimes_m}^>\!\!\!{}^n\iota_m\\ {}^xX_n^\mu &= \begin{cases} X^\mu - {}^x\cancel{x}iP^\mu & n = 0 \\ \frac{x^n\overset{*}{\partial}^\mu - x^{-n}\partial^\mu}{i\sqrt{n}} & n > 0 \end{cases}\end{aligned}$$

$${}^\tau X_\sigma^\mu = X^\mu + \tau P^\mu - \sum_{n\neq 0}{}^{\sigma n}\mathfrak{c}^{-i\tau}\mathfrak{e}^n\frac{\alpha_n^\mu}{in}$$

$$\mu\in d$$

$$\sigma\in 0|\pi$$

$$\sigma=0:\quad {}^\tau X_0^\mu = X^\mu + \tau P^\mu - \sum_{n\neq 0}\frac{-i\tau\mathfrak{e}^n}{in}\alpha_n^\mu$$

$${}^xX^\mu = X^\mu - {}^x\cancel{x}P^\mu i - \sum_{n\neq 0}\frac{x^{-n}}{in}\alpha_n^\mu$$

$$= X^\mu - {}^x\cancel{x}P^\mu i - \sum_{n>0}\frac{x^{-n}}{in}\alpha_n^\mu + \sum_{n>0}\frac{x^n}{in}\alpha_{-n}^\mu = X^\mu - {}^x\cancel{x}P^\mu i + \sum_{n>0}\frac{x^n\overset{*}{\alpha}_n^\mu - x^{-n}\alpha_n^\mu}{in}$$