

$$\begin{aligned}
D_3^{\mathbb{R}} \times f_3^{\mathbb{R}} &= \frac{D_3 \times f_3}{0} \left| \begin{array}{c} 0 \\ J_3 D_3 J_3 \times f_3^{\sim} \end{array} \right. \\
D_3 \times f_3 &= \frac{\begin{array}{c|c} df \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array} \quad \begin{array}{c|c} 0 \\ d\bar{f} \mathbf{x} 1 \end{array} \quad \begin{array}{c|c} \Gamma \underline{\varepsilon} F - f \underline{\varepsilon} \mathbf{x} \frac{\overset{*}{d}}{0} \Big| 0 \\ \hline 0 & \overset{*}{e} \end{array}}{\begin{array}{c|c} 0 \\ \varepsilon f - F \varepsilon \Gamma \mathbf{x} \frac{d}{0} \Big| 0 \\ \hline \varepsilon \bar{f} - F \varepsilon \Gamma \mathbf{x} \frac{u}{0} \end{array} \quad \begin{array}{c|c} dF \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array}} \\
J_3 D_3 J_3 \times f_3^{\sim} &= \frac{\begin{array}{c|c} d\bar{f}_a \mathbf{x} \frac{\bar{a}}{0} \Big| 0 \\ \hline 0 & 1 \end{array} + d\bar{f} \mathbf{x} \frac{0}{0} \Big| 1 \quad \begin{array}{c|c} 0 \\ 0 \end{array} \quad \begin{array}{c|c} 0 \\ 0 \end{array}}{\begin{array}{c|c} 0 \\ 0 \end{array} \quad \begin{array}{c|c} d\bar{f}_a \mathbf{x} \frac{\bar{a}}{0} \Big| 0 \\ \hline 0 & 1 \end{array} + d\bar{f} \mathbf{x} \frac{0}{0} \Big| 0} \\
D_3 f_3 &= \frac{\begin{array}{c|c} \text{rf} \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array} \quad \begin{array}{c|c} 0 \\ \text{rf} \bar{f} \mathbf{x} 1 \end{array} \quad \begin{array}{c|c} \Gamma \underline{\varepsilon} F \mathbf{x} \frac{\overset{*}{d}}{0} \Big| 0 \\ \hline 0 & \overset{*}{e} \end{array}}{\begin{array}{c|c} \varepsilon f \Gamma \mathbf{x} \frac{d}{0} \Big| 0 \\ \hline 0 & e \end{array} \quad \begin{array}{c|c} \varepsilon \bar{f} \Gamma \mathbf{x} \begin{bmatrix} u \\ 0 \end{bmatrix} \\ \hline 0 \end{array} \quad \begin{array}{c|c} \text{rf} F \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array}} \\
f_3 D_3 &= \frac{\begin{array}{c|c} f \text{rf} \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array} \quad \begin{array}{c|c} 0 \\ \bar{f} \text{rf} \mathbf{x} 1 \end{array} \quad \begin{array}{c|c} \Gamma \bar{f} \underline{\varepsilon} \mathbf{x} \frac{\overset{*}{d}}{0} \Big| 0 \\ \hline 0 & 0 \end{array}}{\begin{array}{c|c} F \varepsilon \Gamma \mathbf{x} \frac{d}{0} \Big| 0 \\ \hline 0 & e \end{array} \quad \begin{array}{c|c} F \varepsilon \Gamma \mathbf{x} \begin{bmatrix} u \\ 0 \end{bmatrix} \\ \hline 0 \end{array} \quad \begin{array}{c|c} F \text{rf} \mathbf{x} \frac{1}{0} \Big| 0 \\ \hline 0 & 1 \end{array}} \\
J_3 D_3 J_3 f_3^{\sim} &= \frac{\begin{array}{c|c} \text{rf} \bar{f}_a \mathbf{x} \frac{\bar{a}}{0} \Big| 0 \\ \hline 0 & 1 \end{array} + \text{rf} \bar{f} \mathbf{x} \frac{0}{0} \Big| 0 \quad \begin{array}{c|c} 0 \\ -\Gamma \underline{\varepsilon} \bar{f}_a \mathbf{x} \frac{d^t \bar{a}}{0} \Big| 0 \end{array} - \Gamma \underline{\varepsilon} \bar{f} \mathbf{x} \frac{0}{0} \Big| 0}{\begin{array}{c|c} 0 \\ -\varepsilon \Gamma \bar{f}_a \mathbf{x} \frac{\bar{d} \bar{a}}{0} \Big| 0 \end{array} - \varepsilon \Gamma \bar{f} \mathbf{x} \frac{0}{0} \Big| \bar{e} \quad \begin{array}{c|c} -\Gamma \underline{\varepsilon} \bar{f}_a \mathbf{x} \begin{bmatrix} u^t \bar{a} \\ 0 \end{bmatrix} \\ \hline 0 \end{array}} \\
f_3^{\sim} J_3 D_3 J_3 &= \frac{\begin{array}{c|c} \bar{f}_a \text{rf} \mathbf{x} \frac{\bar{a}}{0} \Big| 0 \\ \hline 0 & 1 \end{array} + \bar{f} \text{rf} \mathbf{x} \frac{0}{0} \Big| 0 \quad \begin{array}{c|c} 0 \\ -\bar{f}_a \Gamma \underline{\varepsilon} \mathbf{x} \frac{\bar{a} d^t}{0} \Big| 0 \end{array} - \bar{f} \Gamma \underline{\varepsilon} \mathbf{x} \frac{0}{0} \Big| 0}{\begin{array}{c|c} 0 \\ -\bar{f}_a \varepsilon \Gamma \mathbf{x} \frac{\bar{a} \bar{d}}{0} \Big| 0 \end{array} - \bar{f} \varepsilon \Gamma \mathbf{x} \frac{0}{0} \Big| \bar{e} \quad \begin{array}{c|c} -\bar{f}_a \Gamma \underline{\varepsilon} \mathbf{x} \begin{bmatrix} \bar{a} u^t \\ 0 \end{bmatrix} \\ \hline 0 \end{array}}
\end{aligned}$$