

$$\frac{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}}{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}} = \frac{\begin{array}{c|c} \gamma \gamma + \varphi \alpha \alpha & \gamma \alpha + \alpha \gamma \\ \hline \varphi (\gamma \alpha + \alpha \gamma) & \gamma \gamma + \varphi \alpha \alpha \end{array}}$$

$$^X f \in K|X$$

$$^X \gamma|^X \alpha \in K\left(X\right)$$

$$^X K_f \ni \gamma|\alpha$$

$$\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{\gamma|\alpha}_{\dot{\varphi}}=\overline{\gamma\gamma+\alpha\varphi\alpha}|\overline{\gamma\alpha+\alpha\gamma}$$

$$\overline{\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{\gamma|\alpha}_{\dot{\varphi}}}_{\dot{\varphi}}\underbrace{\alpha|\alpha}_{\dot{\varphi}}=\underbrace{\gamma|\alpha}_{\dot{\varphi}}\overline{\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{\alpha|\alpha}_{\dot{\varphi}}}$$

$$\begin{aligned} \text{LHS} &= \overline{\overline{\gamma\gamma+\alpha\varphi\alpha}|\overline{\gamma\alpha+\alpha\gamma}}_{\dot{\varphi}}\underbrace{\alpha|\alpha}_{\dot{\varphi}}=\overline{\overline{\gamma\gamma+\alpha\varphi\alpha}\gamma+\overline{\gamma\alpha+\alpha\gamma}\varphi\alpha}_{\dot{\varphi}}|\overline{\overline{\gamma\gamma+\alpha\varphi\alpha}\alpha+\overline{\gamma\alpha+\alpha\gamma}\gamma}\\ &= \overline{\overline{\gamma\gamma\gamma+\alpha\varphi\alpha\gamma+\gamma\alpha\varphi\alpha+\alpha\gamma\varphi\alpha}_{\dot{\varphi}}|\overline{\gamma\alpha\alpha+\alpha\varphi\alpha\alpha+\gamma\alpha\gamma+\alpha\gamma\gamma}_{\dot{\varphi}}}\\ &= \overline{\overline{\gamma\gamma\gamma+\gamma\alpha\varphi\alpha+\alpha\varphi\gamma\alpha+\alpha\varphi\alpha\gamma}_{\dot{\varphi}}|\overline{\gamma\alpha\alpha+\gamma\alpha\gamma+\alpha\gamma\gamma+\alpha\alpha\varphi\alpha}_{\dot{\varphi}}}\\ &= \overline{\overline{\gamma\gamma\gamma+\alpha\varphi\alpha}_{\dot{\varphi}}+\overline{\alpha\gamma\alpha+\alpha\gamma}_{\dot{\varphi}}}_{\dot{\varphi}}|\overline{\overline{\gamma\alpha\alpha+\alpha\gamma}_{\dot{\varphi}}+\overline{\alpha\gamma\gamma+\alpha\varphi\alpha}_{\dot{\varphi}}}_{\dot{\varphi}}=\underbrace{\gamma|\alpha}_{\dot{\varphi}}\overline{\overline{\gamma\gamma+\alpha\varphi\alpha}_{\dot{\varphi}}|\overline{\gamma\alpha+\alpha\gamma}_{\dot{\varphi}}}=\text{RHS} \end{aligned}$$

$$\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{1|0}_{\dot{\varphi}}=\gamma|\alpha$$

$$\frac{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}}{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}} \frac{\begin{array}{c|c} 1 & 0 \\ \hline \varphi 0 & 1 \end{array}}{\begin{array}{c|c} 1 & 0 \\ \hline \varphi 0 & 1 \end{array}} = \frac{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}}{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}}$$

$$\text{LHS} \, = \, \underbrace{\gamma 1 + \alpha \varphi 0}_{\dot{\varphi}} | \underbrace{\gamma 0 + \alpha 1}_{\dot{\varphi}} = \text{RHS}$$

$$\gamma^2\neq\alpha^2\varphi\Rightarrow\underbrace{\gamma|\alpha}_{\dot{\varphi}}^{-1}=\frac{\gamma}{\gamma^2-\alpha^2\varphi}|\frac{-\alpha}{\gamma^2-\alpha^2\varphi}$$

$$\frac{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}}{\begin{array}{c|c} \gamma & \alpha \\ \hline \varphi \alpha & \gamma \end{array}} \frac{\begin{array}{c|c} \gamma & -\alpha \\ \hline -\varphi \alpha & \gamma \end{array}}{\begin{array}{c|c} \gamma & -\alpha \\ \hline -\varphi \alpha & \gamma \end{array}} = \underbrace{\frac{\gamma^2-\varphi\alpha^2}{\neq 0}}_{\dot{\varphi}} \frac{1}{\varphi 0} \bigg| \frac{0}{1}$$

$$\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{\gamma|-\alpha}_{\dot{\varphi}}=\underbrace{\gamma^2-\alpha^2\varphi}_{\dot{\varphi}}|0\Rightarrow\underbrace{\gamma|\alpha}_{\dot{\varphi}}\underbrace{\frac{\gamma}{\gamma^2-\alpha^2\varphi}|\frac{-\alpha}{\gamma^2-\alpha^2\varphi}}_{\dot{\varphi}}=1|0$$

$${}^x\gamma = 1|x\frac{a}{c}|\frac{b}{d} = \frac{b+xd}{a+xc}$$

$$\#A=2m\colon\quad {}^x\varphi=\prod_{\alpha}^A(x-\alpha)\colon\quad {}^u\psi=\prod_{\alpha}^A(u-{}^{\alpha}\gamma)\colon\quad \lambda=\frac{\overbrace{da-cb}^{2m}}{\prod_{\alpha}^A a+\alpha c}$$

$$\begin{array}{ccccc} & & M_{a+xc}^{-m} & & C_{\gamma} \\ & & \longleftarrow & & \longleftarrow \\ {}^xK_{\lambda\varphi} & & {}^xK_{\gamma\ltimes\psi} & & {}^uK_{\psi} \\ & \searrow & & \nearrow & \\ & & M_{a+xc}^{-m}C_{\gamma} & & \end{array}$$

$${}^{x\gamma}\gamma|\frac{{}^{x\gamma}\P}{(a+xc)^m}\leftarrow\lrcorner{}^{x\gamma}\gamma|{}^{x\gamma}\P\leftarrow\lrcorner{}^u\gamma|{}^u\P$$

$${}^x\gamma-{}^y\gamma=\frac{b+xd}{a+xc}-\frac{b+yd}{a+yc}=\frac{(b+xd)(a+yc)-(a+xc)(b+yd)}{(a+xc)(a+yc)}=(x-y)\frac{da-cb}{(a+xc)(a+yc)}$$

$${}^x\gamma-{}^{\alpha}\gamma=(x-\alpha)\frac{da-cb}{(a+xc)(a+\alpha c)}$$

$${}^{x\gamma}\psi\,(a+xc)^{2m}=(a+xc)^{2m}\,{}^x\overline{\gamma\ltimes\psi}=(a+xc)^{2m}\prod_{\alpha}^A({}^x\gamma-{}^{\alpha}\gamma)$$

$$=(a+xc)^{2m}\prod_{\alpha}^A(x-\alpha)\frac{da-cb}{(a+xc)(a+\alpha c)}={}^x\varphi\prod_{\alpha}^A\frac{da-cb}{a+\alpha c}=\lambda{}^x\varphi$$