

$${}^o\gamma = 0 \implies {}^z\gamma = (z - o) {}^z\mathbf{1}$$

$$\gamma = (z - o) {}^zq + {}^zr$$

$$\deg r < \deg z - o = 1 \implies r = \text{ cst}$$

$$0 = {}^o\gamma = (o - o) {}^oq + r = r$$

$$\gamma \neq \text{ cst} : \quad {}^o\gamma \neq 0 \implies {}^{\overline{o}}\overline{\gamma} > {}^{\mathbb{C}}\overline{\gamma}_{\bullet}$$

$$0 \neq {}^z\gamma - {}^o\gamma = \underbrace{a_m}_{\neq 0} \frac{m}{z - o} + \sum_{n > m} a_n \frac{n}{z - o}$$

$$w^m = - {}^o\gamma / a_m$$

$$0 < \varepsilon < 1 \wedge \frac{{}^{\overline{o}}\overline{\gamma}}{\sum_{n > m} \overline{a_n w^n}} \implies \overline{{}^{o+\varepsilon w}\gamma} < {}^{\overline{o}}\overline{\gamma}$$

$${}^{o+\varepsilon w}\gamma - \underbrace{1 - \varepsilon^m}_{} {}^o\gamma = \varepsilon^m {}^o\gamma + {}^{o+\varepsilon w}\gamma - {}^o\gamma = \varepsilon^m {}^o\gamma + a_m w^m \varepsilon^m + \sum_{n > m} a_n w^n \varepsilon^n$$

$$= \varepsilon^m \underbrace{{}^o\gamma + a_m w^m}_{= 0} + \sum_{n > m} a_n w^n \varepsilon^n = \sum_{n > m} a_n w^n \varepsilon^n$$

$$\begin{aligned} \varepsilon^m {}^{\overline{o}}\overline{\gamma} + \overline{{}^{o+\varepsilon w}\gamma} - {}^{\overline{o}}\overline{\gamma} &= \overline{{}^{o+\varepsilon w}\gamma} - \underbrace{1 - \varepsilon^m}_{} {}^{\overline{o}}\overline{\gamma} = \overline{{}^{o+\varepsilon w}\gamma} - \overline{\underbrace{1 - \varepsilon^m}_{} {}^o\gamma} \leqslant \overline{{}^{o+\varepsilon w}\gamma} - \underbrace{\overline{{}^{o+\varepsilon w}\gamma}}_{\leqslant 1} \\ &= \overline{\sum_{n > m} a_n w^n \varepsilon^n} \leqslant \sum_{n > m} \overline{a_n w^n} \varepsilon^n = \varepsilon^m \varepsilon \sum_{n > m} \overline{a_n w^n} \underbrace{\varepsilon^{n-m-1}}_{\leqslant 1} \leqslant \varepsilon^m \varepsilon \underbrace{\sum_{n > m} \overline{a_n w^n}}_{< {}^{\overline{o}}\overline{\gamma}} < \varepsilon^m {}^{\overline{o}}\overline{\gamma} \end{aligned}$$