

$$\begin{cases} \overline{\overline{A+B}} \leq \overline{\overline{A}} + \overline{\overline{B}} & A:B \in \mathbb{R}^{m \times n} \\ \overline{\overline{AB}} \leq \overline{\overline{A}} \overline{\overline{B}} & A \in \mathbb{R}^{m \times n}: B \in \mathbb{R}^{n \times p} \end{cases}$$

$$\max_{i:j} \overline{\overline{A_{i:j}}} \leq \overline{\overline{A}} \leq \sum_{i:j} \overline{\overline{A_{i:j}}}: \quad \overline{\overline{v}} \max_{i:j} \overline{\overline{A_{i:j}}} \leq \overline{\overline{Av}} \leq \overline{\overline{v}} \sum_{i:j} \overline{\overline{A_{i:j}}}$$

$$A \in \mathbb{R}^{n \times n} \xrightarrow[\text{stet/diff}] Q \mathbb{R}^{n \times n} \ni A^2 = AA: \quad \mathbb{R}^{n \times n} \xrightarrow[\text{lin}] {\bar{A}} Q \mathbb{R}^{n \times n}: \quad \bar{A} Q A = \bar{A} A + A \bar{A}$$

$$\text{matrix Komb } \left( \bar{A} + A \right)^2 - \bar{A}^2 - \left( \bar{A} A + A \bar{A} \right)$$

$$A \in \mathbb{R}^{n \times n} \xrightarrow[\text{diff}] {\left( \right)^3} \mathbb{R}^{n \times n} \ni A^3 = AAA: \quad \text{Abl/aalg A9k}$$

$$A \in \mathbb{R}^{n \times n} \xrightarrow[\text{diff}_2] Q_{hk} \mathbb{R}: \quad {}^A Q_{hk} = A_{hk}^2 \text{ Koeff von } A^2: \quad \text{Hesse-Matrix } \left( \frac{\partial^2 Q_{hk}}{\partial A_{ij} \partial A_{pq}} \right)$$

$$\frac{A \in \mathbb{R}^{n \times n}}{\|\overline{A}\| < 1} \ni A \xrightarrow{\text{stet}} {}^A \mathcal{V} = {}^{I+A} \log = \sum_{k \geq 1} \frac{(-1)^{k-1}}{k} A^k$$

$$p_k(A) = \frac{(-1)^{k-1}}{k} A^k$$

$$\overline{p_k}: R \text{ Konv-Rad} \sum_{k \geq 1} p_k$$

$$\overline{\overline{A}} < 1 \Rightarrow \mathbb{R}^{n \times n} \xrightarrow[\text{lin}]{{}^A p_{-k}} \mathbb{R}^{n \times n}$$

$$\mathbb{R}^{n \times n} \xrightarrow[k-1 \text{ hom}]{{}^{\underline{-k}} p_k} \mathcal{L}(\mathbb{R}^{n \times n}): \overline{p_{-k}}: \text{ Konv-Rad} \sum_{k \geq 2} p_{-k}$$

$$\overline{\overline{A}} < 1 \Rightarrow \mathcal{V} \text{ diff in } A: {}^0 \mathcal{V}$$

$$\overline{\overline{A}} < 1 \Rightarrow \begin{cases} A^k \rightsquigarrow 0 \\ \sum_{k \geq 0} A^k = (I - A)^{-1} \text{ inv} \end{cases} : \quad \overline{\overline{A - I}} < 1 \Rightarrow \begin{cases} A \text{ inv} \\ A^{-1} \text{ Potenz-Reihe} \end{cases}$$

$$\exp A \begin{cases} \text{diag } A \in \mathbb{R}^{n \times n} \\ A \frac{x}{y} = \frac{0}{x} \\ \frac{z}{y} \end{cases}$$

$$\overline{\overline{A - I}} < 1 \Rightarrow {}^{\log A} \exp = A$$

$$\frac{A \in \mathbb{R}^{n \times n}}{A \text{ diagonalisierbar}} \subset \mathbb{R}^{n \times n}$$

dicht  
exp / log stet

$$A:v \in \mathbb{R}^{m \times n} \times \mathbb{R}^n \xrightarrow[\text{bilin/diff}]{{}^F} \mathbb{R}^m \ni Av: \mathbb{R}^{m \times n} \times \mathbb{R}^n \xrightarrow[\text{lin}]{{}^F} \mathbb{R}^m$$