

$$\text{conv/off } U \subset \mathbb{R}^n: \quad U \xrightarrow[\text{+diff}]{} \mathbb{R}^n: \quad \bigwedge_x^U \overline{\underline{\mathcal{V}}_x - I} < 1 \Rightarrow \mathcal{V} \text{ inj}$$

$$\mathbb{R}^2 \setminus 0 \ni x:y \mapsto x^2 - \frac{3}{2} y^2 |xy \begin{cases} \text{loc inv} \\ \text{nicht bij} \end{cases}$$

$$\mathbb{R}^2 \ni x:y \mapsto e^x \cos y | e^x \sin y \in \mathbb{R}^2 \setminus 0 \begin{cases} \text{loc inv} \\ \text{nicht inj} \\ \text{surj} \end{cases}$$

$$\mathbb{R}^2 \xrightarrow[\text{off}]{x:y \in \mathbb{R}^2 \atop x+y \notin \mathbb{Z}\pi} \mathcal{V} \rightarrow \mathbb{R}^2: \quad {}^{x:y} \mathcal{V} = (e^x \cos y : e^y \sin x) \text{ lok Diffeo/glob Diffeo?}$$

Funkt-Matrix/Det/max InjBer/Bildmenge//Inverse

$$\text{Polar-Koord } \mathbb{R}_> \times \mathbb{R} \xrightarrow{\mathcal{V}} \mathbb{R}^2 \setminus 0: \quad {}^{r:t} \mathcal{V} = \underbrace{r \cos t}_{r \sin t}$$

$$\text{find max off } V \subset \mathbb{R}_> \times \mathbb{R}: \quad V \xrightarrow[\text{bij}]{\mathcal{V}} \mathbb{R}^2 \setminus (\mathbb{R}_- \times 0)$$

$$\mathbb{R}^2 \setminus (\mathbb{R}_- \times 0) \xrightarrow[\text{bij}]{g = \mathcal{V}^{-1}} V: \quad \text{explizit } r = g_1(x:y)/t = g_2(x:y): \quad \text{Funkt-Matrix} \begin{vmatrix} \frac{\partial r}{\partial x}(x:y) & \frac{\partial r}{\partial y}(x:y) \\ \frac{\partial t}{\partial x}(x:y) & \frac{\partial t}{\partial y}(x:y) \end{vmatrix}$$

$$\text{Kugel-Koord } \mathbb{R}_> \times \mathbb{R}^2 \ni \underbrace{r:\vartheta:\varphi}_{\text{which } x:y \in \mathbb{R} \times \mathbb{R}^\times} \mapsto \underbrace{r \cos \vartheta \sin \varphi | r \sin \vartheta \sin \varphi | r \cos \varphi}_{\in \mathbb{R}^3 \setminus 0}$$

$${}^{x:y} \mathcal{V} = \left( xy: \frac{x}{y} \right) \text{ which } x:y \in \mathbb{R} \times \mathbb{R}^\times \text{ inv Funkt-Matrix}$$

$$v \in \mathbb{R}^n \xrightarrow[\text{diff}]{\mathfrak{v}} \mathbb{R}^n \ni v^n \overline{v^n} / {}^v \mathfrak{v}$$

$$x:y \in \mathbb{R}^2 \xrightarrow[\text{diffeo}]{\mathcal{V}} \mathbb{R}^2 \ni e^x + y: e^y + y: \quad \text{Bild}$$