

$$\mathbb{1} \xleftarrow[\text{ell sa 1st ord}]{\mathbb{1}} \mathcal{D}_{\mathbb{1}} \sqsubset \mathbb{1} \text{ fermionic}$$

$$\mathbb{1} = \mathbb{1}_{\text{pp}} = \frac{\mathbb{1}^k}{k \in \mathbb{Z}} \text{ pure point spectrum}$$

$$\eta_s^{\mathbb{1}} = \sum_{k \neq 0} \frac{\text{sgn}_k \mathbb{1}^k}{s \overline{\mathbb{1}^k}_k} = \sum_{k \neq 0} \frac{\mathbb{1}^k / \overline{\mathbb{1}^k}_k}{s \overline{\mathbb{1}^k}_k} = \sum_{k \neq 0} \frac{\mathbb{1}^k}{\overline{\mathbb{1}^k}_k^{s+1}}$$

$$\int\limits_{dt}^{0|\infty} t^{(s-1)/2} \text{tr} \ \mathbb{1} \ \mathfrak{e}^{-\mathbb{1}t} = \Gamma_{(s+1)/2} \eta_s^{\mathbb{1}}$$

$$\text{tr} \ \mathbb{1} \ \mathfrak{e}^{-\mathbb{1}t} = \sum_k \ \mathbb{1}^k \ \mathfrak{e}^{-\mathbb{1}^k t} = \sum_{k \neq 0} \ \mathbb{1}^k \ \mathfrak{e}^{-\mathbb{1}^k t}$$

$$k \neq 0 \Rightarrow 0|\infty \ni t \xrightarrow[\text{trafo}]{\mathbb{1}^k} t = \tau \in 0|\infty$$

$$\int\limits_{dt}^{0|\infty} t^{(s-1)/2} \ \mathbb{1}^k \ \mathfrak{e}^{-\mathbb{1}^k t} = \mathbb{1}^k \ \overline{\mathbb{1}^k}^{1-s} \int\limits_{dt}^{0|\infty} (s-1)/2 \left(\mathbb{1}^k t \right) \ \mathfrak{e}^{-\mathbb{1}^k t}$$

$$= \mathbb{1}^k \ \overline{\mathbb{1}^k}^{1-s} \ \mathbb{1}^k \int\limits_{d\left(\mathbb{1}^k t\right)}^{0|\infty} (s-1)/2 \overline{\mathbb{1}^k t} \ \mathfrak{e}^{-\mathbb{1}^k t}$$

$$= \frac{\overline{\mathbb{1}^k}_k^{-s} \overline{\mathbb{1}^k}_k}{\mathbb{1}^k} \int\limits_{d\left(\mathbb{1}^k t\right)}^{0|\infty} (s-1)/2 \overline{\mathbb{1}^k t} \ \mathfrak{e}^{-\mathbb{1}^k t} = \text{sgn}_k \ \mathbb{1}^k \ \overline{\mathbb{1}^k}_k^{-s} \int\limits_{d\tau}^{0|\infty} \tau^{(s-1)/2} \ \mathfrak{e}^{-\tau} = \Gamma_{(s+1)/2} \frac{\text{sgn}_k \ \mathbb{1}^k}{s \overline{\mathbb{1}^k}_k}$$