

$k = 1$: IIA sugra

Witten

$$-\begin{cases} \mathcal{X}\mathcal{Y}\mathcal{Z} \\ \mathcal{X}\mathcal{Z}\mathcal{Y} \end{cases} = \mathcal{Q}^{-2} \left(-\boxed{\mathcal{X}} - \overline{\frac{2}{\mathcal{Y}/\mathcal{Q}}} + \overline{\frac{2}{\mathcal{Z}}} \right) + \left(\overline{\frac{2}{\mathcal{X}}} + \overline{\frac{2}{\mathcal{Z} + \mathcal{X} \wedge \mathcal{Y}}} \right) + \mathcal{Z} \wedge \mathcal{Z} \wedge \mathcal{Y}$$
$$-\begin{cases} \mathcal{X}\mathcal{Y} \\ \mathcal{X}\mathcal{Z} \end{cases} = -\boxed{\mathcal{X}} + \overline{\frac{2}{\mathcal{Q}}} + H e^{-3\mathcal{Q}/2} \overline{\frac{2}{\mathcal{X}}} + e^{\mathcal{Q}} \overline{\frac{2}{\mathcal{Z}}} + e^{-\mathcal{Q}/2} \overline{\frac{2}{\mathcal{Z} - \mathcal{Z}\mathcal{X}}} + \overline{\frac{2}{\mathcal{Z}}} \mathcal{Z}$$