

$$D=9$$

$$E_8^6 = GL_2^{\mathbb{R}} \colon \text{ scalar coset } GL_2^{\mathbb{R}}$$

$$E_7^6 = O_{1:1} \colon \text{ scalar coset } \mathbb{R}_> \ni \mathbb{Q}$$

$$\begin{cases}\mathfrak{Q}\mathfrak{Q} \\ \mathcal{Z} \\ \chi\end{cases} = \boxed{\mathfrak{Q}} + \frac{2}{\underline{\mathbb{Q}}} - \mathfrak{e}^{2\mathbb{Q}/\sqrt{7}} \frac{2}{\underline{\mathcal{Z}}} - \mathfrak{e}^{-4\mathbb{Q}/\sqrt{7}} \frac{2}{\underline{\chi}} - \frac{2}{\underline{\mathcal{Z}}} \chi$$

$$E_6^6 = 1 \colon \text{ impossible}$$

$$D_8^6 = O_{1:1} \times O_{1:1} \colon \text{ scalar coset } \mathbb{R}_> \times \mathbb{R}_>$$