

left option

right option

$$s:t \overleftarrow{\varphi \mathbf{x} \psi} := s \varphi \text{ } ^{t^-} s \psi$$

$$s:t \overrightarrow{\varphi \mathbf{x} \psi} = s \varphi \text{ } ^{st^-} \psi$$

$$\begin{cases} s:t \overrightarrow{\neg} \gamma = ^{st^-} \gamma \\ s:t \overleftarrow{\neg} \gamma = ^{t^-} s \gamma \end{cases}$$

$$\overrightarrow{\neg} \gamma = 1 \mathbf{x} \gamma$$

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$$s:t \overleftarrow{\neg \gamma \varphi \mathbf{x} \psi} = s:t \overrightarrow{\neg} \gamma \text{ } ^{s:t} \overleftarrow{\varphi \mathbf{x} \psi} = s:t \overrightarrow{\neg} \gamma \text{ } s \varphi \text{ } ^{t^-} s \psi = \overleftarrow{s \text{ } ^{t^-} s} \gamma \text{ } s \varphi \text{ } ^{t^-} s \psi = \text{ } ^t \gamma \text{ } s \varphi \text{ } ^{t^-} s \psi = \text{ } ^t \gamma \text{ } ^{s:t} \overleftarrow{\varphi \mathbf{x} \psi} = \text{ } ^{s:t} \overleftarrow{1 \mathbf{x} \gamma \overleftarrow{\varphi \mathbf{x} \psi}}$$

$$s:t \overrightarrow{\neg \gamma \varphi \mathbf{x} \psi} = s:st \overrightarrow{\neg} \gamma \text{ } ^{s:t} \overrightarrow{\varphi \mathbf{x} \psi} = s:st \overrightarrow{\neg} \gamma \text{ } s \varphi \text{ } ^{st^-} \psi = \overleftarrow{s \text{ } ^{st^-} s} \gamma \text{ } s \varphi \text{ } ^{st^-} \psi = \text{ } ^t \gamma \text{ } s \varphi \text{ } ^{st^-} \psi = \text{ } ^t \gamma \text{ } ^{s:t} \overrightarrow{\varphi \mathbf{x} \psi} = \text{ } ^{s:t} \overrightarrow{1 \mathbf{x} \gamma \overrightarrow{\varphi \mathbf{x} \psi}}$$

$$\overleftarrow{\overleftarrow{g} \mathbf{x} 1} = \overleftarrow{g} \mathbf{x} \overleftarrow{g} \Rightarrow \overleftarrow{\overleftarrow{u} \mathbf{x} 1} = \overleftarrow{u} \neg$$

$$\overrightarrow{\overrightarrow{g} \mathbf{x} 1} = \overrightarrow{g} \mathbf{x} \overrightarrow{g} \Rightarrow \overrightarrow{\overrightarrow{u} \mathbf{x} 1} = \overrightarrow{u} \neg$$

$$s:t \overleftarrow{\overleftarrow{g} \mathbf{x} 1 \varphi \mathbf{x} \psi} = s:t \overleftarrow{\overleftarrow{g} \varphi \mathbf{x} \psi} = \overleftarrow{s \text{ } ^{t^-} s} \varphi \text{ } ^{t^-} s \psi = \text{ } ^{g^-} s \varphi \text{ } ^{t^-} s \psi = \text{ } ^{g^-} s \varphi \text{ } ^{(g^- t)^-} \text{ } ^{g^-} s \psi = \text{ } ^{g^- s: g^- t} \overleftarrow{\varphi \mathbf{x} \psi} = \text{ } ^{s:t} \overleftarrow{\overleftarrow{g} \mathbf{x} \overleftarrow{g} \overleftarrow{\varphi \mathbf{x} \psi}}$$

$$s:t \overrightarrow{\overrightarrow{g} \mathbf{x} 1 \varphi \mathbf{x} \psi} = \text{ } ^{s:t} \overrightarrow{\overrightarrow{g} \varphi \mathbf{x} \psi} = \text{ } ^s \overrightarrow{\overrightarrow{g} \varphi} \text{ } ^{st^-} \psi = \text{ } ^{sg} \varphi \text{ } ^{st^-} \psi = \text{ } ^{sg} \varphi \text{ } ^{sg(tg)^-} \psi = \text{ } ^{sg:tg} \overrightarrow{\varphi \mathbf{x} \psi} = \text{ } ^{s:t} \overrightarrow{\overrightarrow{g} \mathbf{x} \overrightarrow{g} \overrightarrow{\varphi \mathbf{x} \psi}}$$

$$\overbrace{\mathbb{L}^{\lrcorner} \mathbf{x} 1}^{i \mathbf{x} \rceil} = \mathbb{L}^{\lrcorner} \mathbf{x} 1$$

$$\overbrace{\mathbb{L}^{\lrcorner} \mathbf{x} 1}^{i \mathbf{x} \lceil} = \mathbb{L}^{\lrcorner} \mathbf{x} 1$$

$$\overbrace{b \mathbf{x} \overleftarrow{u} \mathbf{x} 1}^{i \mathbf{x} \rceil} = b \mathbf{x} \overleftarrow{u} \mathbf{x} = \overbrace{b \mathbf{x} \overleftarrow{u}}^{i \mathbf{x} \lrcorner}$$

$$\mathbb{L} \mathbf{x} C \overrightarrow{\mathbf{x}} \mathbb{H} \ni \mathbb{L}^{\lrcorner} = b_i \mathbf{x} \overleftarrow{u}^i \Rightarrow \text{LHS} = \mathbb{L}^{\lrcorner}^{i \mathbf{x} \lrcorner} = \text{RHS}$$

$$\overbrace{b \mathbf{x} \overrightarrow{u} \mathbf{x} 1}^{i \mathbf{x} \lceil} = b \mathbf{x} \overrightarrow{u} \mathbf{x} = \overbrace{b \mathbf{x} \overrightarrow{u}}^{i \mathbf{x} \lrcorner}$$

$$\mathbb{L} \mathbf{x} C \overleftarrow{\mathbf{x}} \mathbb{H} \ni \mathbb{L}^{\lrcorner} = b_i \mathbf{x} \overrightarrow{u}^i \Rightarrow \text{LHS} = \mathbb{L}^{\lrcorner}^{i \mathbf{x} \lrcorner} = \text{RHS}$$

$$\overbrace{1 \mathbf{x} \overleftarrow{g}}^{\lceil} = 1 \mathbf{x} \overrightarrow{g} \Rightarrow \overbrace{1 \mathbf{x} \overleftarrow{u}}^{\lceil} = 1 \mathbf{x} \overrightarrow{u}$$

$$\overbrace{1 \mathbf{x} \overrightarrow{g}}^{\lceil} = 1 \mathbf{x} \overleftarrow{g} \Rightarrow \overbrace{1 \mathbf{x} \overrightarrow{u}}^{\lceil} = 1 \mathbf{x} \overleftarrow{u}$$

$$\overrightarrow{s:t} \overbrace{1 \mathbf{x} \overleftarrow{g} \varphi \mathbf{x} \psi} = \overrightarrow{s:t} \overbrace{\varphi \mathbf{x} \overleftarrow{g} \psi} = {}^s \varphi \overbrace{t^{-s} \overleftarrow{g} \psi} = {}^s \varphi \overbrace{g^{-t^{-s}} \psi} = {}^s \varphi \overbrace{\overleftarrow{tg} s} = {}^{s:tg} \overbrace{\varphi \mathbf{x} \psi} = \overrightarrow{s:t} \overbrace{1 \mathbf{x} \overrightarrow{g} \varphi \mathbf{x} \psi}$$

$$\overrightarrow{s:t} \overbrace{1 \mathbf{x} \overrightarrow{g} \varphi \mathbf{x} \psi} = \overrightarrow{s:t} \overbrace{\varphi \mathbf{x} \overrightarrow{g} \psi} = {}^s \varphi \overbrace{st^{-} \overrightarrow{g} \psi} = {}^s \varphi \overbrace{st^{-g} \psi} = {}^s \varphi \overbrace{s \overleftarrow{g^{-t}}} = {}^{s:g^{-t}} \overbrace{\varphi \mathbf{x} \psi} = \overrightarrow{s:t} \overbrace{1 \mathbf{x} \overleftarrow{g} \varphi \mathbf{x} \psi}$$

$$\left\{ \begin{array}{l} \mathbb{L} \mathbf{x} \overrightarrow{\mathbb{H}} \overrightarrow{\mathbb{H}} \mathbb{C} \mathbf{x} C \overleftarrow{\mathbf{x}} \mathbb{H} \\ \mathbb{L} \mathbf{x} \overrightarrow{\mathbb{H}} \overrightarrow{\mathbb{H}} \mathbb{C} \mathbf{x} C \overleftarrow{\mathbf{x}} \mathbb{H} \end{array} \right\} \ni \left\{ \begin{array}{l} \overrightarrow{\mathbb{L}^{\lrcorner} i \mathbf{x} \overrightarrow{\mathbb{H}}} i \mathbf{x} 1 \mathbf{x} \overleftarrow{u} \\ \overleftarrow{\mathbb{L}^{\lrcorner} i \mathbf{x} \overrightarrow{\mathbb{H}}} i \mathbf{x} 1 \mathbf{x} \overrightarrow{u} \end{array} \right.$$

$$\downarrow \left(\begin{array}{l} i \mathbf{x} \rceil \\ i \mathbf{x} \lceil \end{array} \right) \downarrow \qquad \qquad \qquad \downarrow$$

$$\mathbb{L} \mathbf{x} \overrightarrow{\mathbb{H}} \overrightarrow{\mathbb{H}} \mathbb{C} \mathbf{x} C \overleftarrow{\mathbf{x}} \mathbb{H} \ni \left\{ \begin{array}{l} \overrightarrow{\mathbb{L}^{\lrcorner} i \mathbf{x} \overrightarrow{\mathbb{H}}} i \mathbf{x} 1 \mathbf{x} \overleftarrow{u} \\ \overleftarrow{\mathbb{L}^{\lrcorner} i \mathbf{x} \overrightarrow{\mathbb{H}}} i \mathbf{x} 1 \mathbf{x} \overrightarrow{u} \end{array} \right.$$

$$\begin{aligned} \overbrace{\mathbb{L}^{\neg \mathbf{x}] \mathbf{x} \mathbf{1}}_{\nearrow} \mathbf{x} \mathbf{1} \mathbf{x} \overleftarrow{u}} &= \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \overrightarrow{u} \\ \overbrace{\mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \overrightarrow{u}}_{\nwarrow} &= \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \overrightarrow{u} \end{aligned}$$

$$\begin{aligned} \text{LHS} &= \overbrace{\mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \overleftarrow{u}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} = \overbrace{\mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} \overbrace{\mathbf{x} \mathbf{1} \mathbf{x} \overleftarrow{u}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \mathbf{x} \overrightarrow{u} \\ &= \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \text{RHS} \end{aligned}$$

$$\begin{aligned} \text{LHS} &= \overbrace{\mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \overrightarrow{u}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} = \overbrace{\mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} \overbrace{\mathbf{x} \mathbf{1} \mathbf{x} \overrightarrow{u}}^{\mathbf{x} \mathbf{1}] \mathbf{x} \mathbf{1}} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \mathbf{x} \overrightarrow{u} \\ &= \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \mathbb{L}^{\neg \mathbf{x} \mathbf{1}} \mathbf{x} \mathbf{1} \mathbf{x} \mathbf{1} \overrightarrow{u} = \text{RHS} \end{aligned}$$