

$$\mathbb{T} \xrightarrow{\begin{cases} \lceil \\ \rceil \end{cases}} \mathbb{T} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}}$$

$\left\{ \begin{array}{l} \text{left opt} \\ \text{right opt} \end{array} \right.$

$$\begin{aligned} \mathbb{C}_{\ell/r}^{\frac{1}{2}} &\xrightarrow[\text{bi-falt}]{\begin{cases} \lceil \\ \rceil \end{cases}} \mathbb{C}_{\ell/r}^{\frac{1}{2}} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}} \\ &\Rightarrow \mathbb{L}^{\lceil \rceil^{\lceil \rceil^{\lceil \rceil}}} = \mathbb{L}^{\lceil \rceil^{\lceil \rceil^{\lceil \rceil}}} \\ &\mathbb{L}^{\lceil \rceil^{\lceil \rceil^{\lceil \rceil}}} = \mathbb{L}^{\lceil \rceil^{\lceil \rceil^{\lceil \rceil}}} \end{aligned}$$

$$\begin{array}{ccc} \mathbb{T} & \xrightarrow{\begin{cases} \lceil \\ \rceil \end{cases}} & \mathbb{T} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}} \\ \downarrow \begin{cases} \lceil \\ \rceil \end{cases} & & \downarrow \begin{cases} \lceil \times \lceil \\ \rceil \times \lceil \end{cases} \\ \mathbb{T} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}} & \xrightarrow{\begin{cases} \iota \times \lceil \\ \iota \times \rceil \end{cases}} & \mathbb{T} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}} \times \mathbb{C}_{\ell/r}^{\frac{1}{2}} \end{array}$$

$$\begin{array}{ccc}
\mathbb{L} \times \mathbb{C} \Delta \mathbb{H} & \xleftarrow{\delta} & \mathbb{L} \\
\downarrow \iota \times \delta_G & & \downarrow \delta \\
\mathbb{L} \times \mathbb{C} \Delta \mathbb{H} \times \mathbb{C} \Delta \mathbb{H} & \xleftarrow{\delta \times \iota_G} & \mathbb{L} \times \mathbb{C} \Delta \mathbb{H}
\end{array}$$

$$u|\gamma = \int^h_s u^s \gamma$$

$$\mathbb{L} \times \mathbb{H} \Delta \mathbb{C} \xrightarrow[\text{cog}]{} \mathbb{L}$$

$$\delta \mathbb{L} = \mathbb{T}_i \times u^i \Rightarrow \underline{\mathbb{L}} \underline{\delta} \mathbb{L} = \underline{\mathbb{L}} \underline{\mathbb{T}}_i \underline{u^i} \underline{\gamma}$$

$$\text{LHS} = \underline{\mathbb{L}} \underline{\mathbb{X}} \underline{\gamma} \underline{\delta} \mathbb{L} = \underline{\mathbb{L}} \underline{\mathbb{X}} \underline{\gamma} \delta \mathbb{L} = \underline{\mathbb{L}} \underline{\mathbb{X}} \underline{\gamma} \underline{\mathbb{T}}_i \underline{\times} u^i = \text{RHS}$$

$$\delta \mathbb{L}_i = \mathbb{T}_i^j \times u_j^i \Rightarrow \underline{\mathbb{L}} \underline{\delta} \mathbb{L}_i = \underline{\mathbb{L}} \underline{\mathbb{T}}_i^j \underline{u_j^i} \underline{\gamma}$$

$$\underline{\iota \times \delta_G} \delta = \underline{\delta \times \iota_G} \delta$$

$$\mathbb{T}_i \times \underline{\delta_G} u^i = \mathbb{T}_i^j \times u_j^i \times u^i$$

$$\text{LHS} = \underline{\iota \times \delta_G} \underline{\mathbb{T}_i \times u^i} = \underline{\iota \times \delta_G} \underline{\delta \mathbb{L}} = \underline{\delta \times \iota_G} \underline{\delta \mathbb{L}} = \underline{\delta \times \iota_G} \underline{\mathbb{T}_i \times u^i} = \underline{\delta \mathbb{T}_i} \times u^i = \text{RHS}$$

$$\mathbb{L} \overset{\sharp}{\delta}_{\gamma\tau} = \underbrace{\mathbb{L} \overset{\sharp}{\delta}_\gamma}_{\gamma} \overset{\sharp}{\delta}_\tau$$

$$\begin{aligned}
\text{LHS } \mathbb{T} &= \underbrace{\mathbb{L} \mathbb{T}_i}_{\gamma} \overbrace{u^i | \mathfrak{T}}^{\gamma\tau} = \underbrace{\mathbb{L} \mathbb{T}_i}_{\gamma} \overbrace{\delta_G u^i | \mathfrak{T} \mathbf{x} \mathfrak{T}}^{\gamma\tau} = \underbrace{\mathbb{L} \mathbf{x} \mathfrak{T} \mathbf{x} \mathfrak{T}}_{\gamma\tau} | \overbrace{\mathbb{T}_i \mathbf{x} \delta_G u^i}^{\gamma\tau} \\
&= \underbrace{\mathbb{L} \mathbf{x} \mathfrak{T} \mathbf{x} \mathfrak{T}}_{\gamma\tau} | \underbrace{\mathbb{T}_i^j \mathbf{x} u_j^i \mathbf{x} u^i}_{\gamma\tau} = \underbrace{\mathbb{L} \mathbb{T}_i^j}_{\gamma\tau} \underbrace{u_j^i | \mathfrak{T} u^i}_{\gamma\tau} = \underbrace{\mathbb{L} \overset{\sharp}{\delta}_\gamma}_{\gamma} \mathbb{T}_i \overbrace{u^i | \mathfrak{T}}^{\gamma\tau} = \text{RHS } \mathbb{T}
\end{aligned}$$