

$$\begin{array}{ccc}
{}^{\ell}\mathbb{C}_{2r}^{\mathbb{C}} & & {}^{=}\mathbb{C}_{2r}^{\mathbb{C}} \\
\downarrow & \searrow Q & \downarrow \\
& {}^r\mathbb{C}_r^{\mathbb{C}} & \\
& \nearrow Q & \nearrow Q \\
{}^{\ell}\mathbb{C}_{\ell}^{\mathbb{U}} \dashv {}^{\ell}\mathbb{C}_{2r}^{\mathbb{C}} & & \mathbb{C}^{\mathbb{U}} \dashv {}^{=}\mathbb{C}_{2r}^{\mathbb{C}}
\end{array}$$

$$\eta|\xi \mapsto \dot{\eta}\xi$$

$$x = \dot{\eta}\xi = \dot{\tau}^2\lambda\sigma$$

$$u = \dot{\tau}\sigma$$

$$\dot{u}x = \dot{\sigma}\underline{\tau\dot{\tau}}^2\lambda\sigma = \dot{\sigma}^2\lambda\sigma = \dot{\xi}\xi$$

$$x\dot{u} = \dot{\tau}^2\lambda\underline{\sigma\dot{\sigma}}\tau = \dot{\tau}^2\lambda\tau = \dot{\eta}\eta$$

$$\dot{u}x\dot{u} = \dot{\sigma}\underline{\tau\dot{\tau}}^2\lambda\underline{\sigma\dot{\sigma}}\tau = \dot{\sigma}^2\lambda\tau = \dot{\xi}\eta$$

$$(g\sigma)^T \left(\overset{T}{g}^{-1}\tau \right) = \overset{T}{\sigma} \overset{T}{g} \overset{T}{g}^{-1}\tau = \overset{T}{\sigma}\tau$$

$$\dim_{\mathbb{C}} {}^r\mathbb{C}_r = \ell + \ell(\ell - 1) + 2\ell(r - \ell) = \ell^2 + 2\ell(r - \ell) = 2\ell r - \ell^2$$

$$\dim_{\mathbb{C}} {}^{\ell}\mathbb{C}_{\ell}^{\mathbb{C}} = \ell^2$$