

$S^d \Rightarrow L^2(\mathcal{F}^S)$ Hilbert space

$M^{d+} \Rightarrow U^M \in L^2(\mathcal{F}^{\partial M})$ vacuum

$${}_{\varphi}U^M = \int_{\Phi|_{\partial M} = \varphi}^{\mathcal{F}^M} \mathcal{D}\Phi \exp\left(-\frac{2\pi i}{h}\mathcal{L}(\Phi)\right)$$

$$\Phi \in \mathcal{F}^M \Rightarrow \mathcal{L}(\Phi) = \int^M \mathcal{L}_{\Phi}$$

$$\mathcal{L}(\Phi) = \mathcal{L}_0(\Phi) + \mathcal{V}(\Phi)$$

$$\exp\left(-\frac{2\pi i}{h}\mathcal{L}(\Phi)\right) = \exp\left(-\frac{2\pi i}{h}(\mathcal{L}_0(\Phi) + \mathcal{V}(\Phi))\right) = \exp\left(-\frac{2\pi i}{h}\mathcal{L}_0(\Phi)\right) \exp\left(-\frac{2\pi i}{h}\mathcal{V}(\Phi)\right)$$

$$\mathcal{D}\Phi \exp\left(-\frac{2\pi i}{h}\mathcal{L}_0(\Phi)\right) = d\mathcal{W}(\Phi) \text{ Wiener meas}$$

$$\mathcal{D}\Phi \exp\left(-\frac{2\pi i}{h}\mathcal{L}(\Phi)\right) = d\mathcal{W}(\Phi) \exp\left(-\frac{2\pi i}{h}\mathcal{V}(\Phi)\right)$$

$${}_{\varphi}U^M = \int_{\Phi|_{\partial M} = \varphi}^{\mathcal{F}^M} d\mathcal{W}(\Phi) \exp\left(-\frac{2\pi i}{h}\mathcal{V}(\Phi)\right)$$