

Sugiyama

$G_2$  holonomy  $\Rightarrow$  conf algebra

$$\text{holonomy reduction } \text{SO}_7/G_2 = \begin{cases} \text{tricritical Ising-model conf alg} \\ 7 \\ \text{Virasoro cc } \frac{7}{10} \\ \text{s-stress tensor } (T^{3I}:G^{3I}) \end{cases}$$

internal  $7_{\mathbb{R}}^0$ :  $G_2$  holonomy

$$H_{\mathbb{R}}^* (7_{\mathbb{R}}^0) = \begin{cases} 11 \\ 00 \\ b_2 = b_5 \\ b_3 = b_4 \end{cases}$$

$$\chi = 0$$

point moduli  $(7_{\mathbb{R}}^0)_{\text{geom}} \asymp H_{\mathbb{R}}^3 (7_{\mathbb{R}}^0)$ :  $\mathfrak{X}$  closed 3-form  $G_2$  inv

$$7_{\mathbb{R}}^0 \text{ sigma model conf algebra} \quad \begin{cases} (T:G) & \text{s-stress tensor} \\ (K:\mathfrak{X}) & \text{current spin (2:3/2)} \\ (*\mathfrak{X}:M) & \text{current spin (2:5/2)} \end{cases}$$

string moduli  $(7_{\mathbb{R}}^0)_{\text{CFT}} \asymp H_{\mathbb{R}}^{2:3} (7_{\mathbb{R}}^0)$ :  $b_2 + b_3$