

$$X_c^{1/2} \ni v \mapsto {}^v\mathfrak{L} \in \text{Aut } X$$

$${}_i\mathfrak{L} \text{ Basis von } X_c^{0|1} \Rightarrow {}^v\mathfrak{L} = {}_i\mathfrak{L} {}^v\mathfrak{L} \text{ Basis von } X_v^{0|1}$$

$$\begin{aligned} & {}^v\mathfrak{L}^1 \mid \cdot \mid {}^v\mathfrak{L}^p \mid {}^v\mathfrak{L}^1 \mid \cdot \mid {}^v\mathfrak{L}^q = {}^v\mathfrak{L}_1^1 \cdot {}^v\mathfrak{L}_1^p {}^v\mathfrak{L}_1^1 \cdot {}^v\mathfrak{L}_1^q \mid \dots \mid {}^v\mathfrak{L}_n^1 \cdot {}^v\mathfrak{L}_n^p {}^v\mathfrak{L}_n^1 \cdot {}^v\mathfrak{L}_n^q \\ & \det \frac{{}^v\mathfrak{L}^1}{\cdot} = \sum_{1 \leq \ell_1 < \dots < \ell_q \leq n} {}^{k|\ell} (-1) \det \frac{{}^v\mathfrak{L}_1^1 \mid \cdot \mid {}^v\mathfrak{L}_1^p}{\cdot \mid \cdot \mid k_1} \det \frac{{}^v\mathfrak{L}_{\ell_1}^1 \mid \cdot \mid {}^v\mathfrak{L}_{\ell_1}^p}{\cdot \mid \cdot \mid k_{\ell_1}} \dots \det \frac{{}^v\mathfrak{L}_{\ell_q}^1 \mid \cdot \mid {}^v\mathfrak{L}_{\ell_q}^p}{\cdot \mid \cdot \mid k_{\ell_q}} \end{aligned}$$

$${}_{-i}\mathfrak{L} = {}_i\mathfrak{L} {}_{-i}\mathfrak{L}$$

$$\partial_\xi^i \mathfrak{e}^{x\xi} = x^i \mathfrak{e}^{x\xi}$$

$${}_{-i}\mathfrak{L} \partial_\xi^i \mathfrak{e}^{x\xi} = {}_{-i}\mathfrak{L} \partial_\xi^i \mathfrak{e}^{x\xi} = {}_i\mathfrak{L} {}_{-i}\mathfrak{L} x^i \mathfrak{e}^{x\xi} = \underbrace{x^i {}_i\mathfrak{L}}_{=x} {}_{-i}\mathfrak{L} \mathfrak{e}^{x\xi} = x {}_{-i}\mathfrak{L} \mathfrak{e}^{x\xi}$$

$$\det \frac{{}^v\mathfrak{L}^1}{\cdot} \frac{{}^v\mathfrak{L}^p}{\cdot} \frac{{}^v\mathfrak{L}^1}{\cdot} \frac{{}^v\mathfrak{L}^p}{\cdot} \frac{{}^v\mathfrak{L}^1}{\cdot} \frac{{}^v\mathfrak{L}^p}{\cdot} \mathfrak{e}^{x\xi} = \det \frac{{}^v\mathfrak{L}_1^1}{\cdot} \frac{{}^v\mathfrak{L}_1^p}{\cdot} \frac{{}^v\mathfrak{L}_{\ell_1}^1}{\cdot} \frac{{}^v\mathfrak{L}_{\ell_1}^p}{\cdot} \dots \frac{{}^v\mathfrak{L}_{\ell_q}^1}{\cdot} \frac{{}^v\mathfrak{L}_{\ell_q}^p}{\cdot} \mathfrak{e}^{x\xi}$$

$$x {}_{-i}\mathfrak{L} = x \underbrace{\mathcal{V}^j {}^v\mathfrak{L}^j}_{=x} = \mathcal{V}^j \underbrace{x^j {}^v\mathfrak{L}^j}_{=x}$$

$${}^v\mathfrak{L}_i^v = \overbrace{{}^v\mathfrak{L}_i^v}^i = \frac{\partial {}^v\mathfrak{L}_i^v}{\partial v^i} = {}_j\mathfrak{L} \underbrace{{}^v\mathfrak{L}_i^v}_{=x} {}^v\mathfrak{L}_i^v = {}_i\mathfrak{L} \underbrace{{}^v\mathfrak{L}_i^v}_{\in \mathfrak{g}(X)} = {}_i\mathfrak{L} \underbrace{{}^v\mathfrak{L}_i^v}_{\in \mathfrak{g}(X)}$$

$${}^v\mathfrak{L}_j^v \partial_\xi^i \mathfrak{e}^{x\xi} = {}^v\mathfrak{L}_j^v \partial_\xi^i \mathfrak{e}^{x\xi} = {}_i\mathfrak{L} \underbrace{{}^v\mathfrak{L}_j^v}_{=x} x^i \mathfrak{e}^{x\xi} = \underbrace{x^i {}_i\mathfrak{L}}_{=x} \underbrace{{}^v\mathfrak{L}_j^v}_{=x} \mathfrak{e}^{x\xi} = x \underbrace{{}^v\mathfrak{L}_j^v}_{=x} \mathfrak{e}^{x\xi}$$

$$\det \frac{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline 1 \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline \mathcal{V}_{\cdot}^q \mathfrak{h}^{\cdot} \\ \cdot \\ \hline \mathcal{V}_{\cdot}^v \mathfrak{h}^{\cdot} \end{array}}{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline 1 \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline \mathcal{V}_{\cdot}^q \mathfrak{h}^{\cdot} \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}} = \mathcal{V}^1 \otimes \mathcal{V}^q \det \frac{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline 1 \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline \mathcal{V}_{\cdot}^q \mathfrak{h}^{\cdot} \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline 1 \mathfrak{h}^{\cdot} \end{array}}{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline 1 \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline \mathcal{V}_{\cdot}^q \mathfrak{h}^{\cdot} \\ \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}}$$

$$\det \frac{\begin{array}{c} \mathcal{V}_{\cdot}^v \mathfrak{h}^{\cdot} \\ \hline \cdot \\ \hline \mathcal{V}_{\cdot}^v \mathfrak{h}^{\cdot} \end{array}}{\begin{array}{c} \mathcal{V}_{\cdot}^v \mathfrak{h}^{\cdot} \\ \hline \cdot \\ \hline \mathcal{V}_{\cdot}^v \mathfrak{h}^{\cdot} \end{array}} = \det \left| \begin{array}{c} \mathcal{V}^1 \\ \cdot \\ \mathcal{V}^q \end{array} \right| \det \frac{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}}{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}} = \mathcal{V}^1 \otimes \mathcal{V}^q \det \frac{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}}{\begin{array}{c} v_{\mathfrak{N}}^{\cdot} \\ \hline \cdot \\ \hline v_{\mathfrak{N}}^{\cdot} \\ \hline q \mathfrak{h}^{\cdot} \end{array}}$$

$$L | t^{-x} T_v = L^v \mathfrak{N} + x t^{-v} \underline{\mathfrak{N}}$$

$${}^x T_v = \frac{\begin{array}{c} {}_1 L^v \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline {}_p L^v \mathfrak{N}^{\cdot} \\ \hline x {}_1 \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline x {}_q \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \end{array}}{\begin{array}{c} {}_1 L^v \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline {}_p L^v \mathfrak{N}^{\cdot} \\ \hline x {}_1 \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline x {}_q \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \end{array}}$$

$$\begin{aligned} & L^1 | \cdot | L^p | t^1 | \cdot | t^q | T_x = L | t | T_x = L^v \mathfrak{N} + x t^{-v} \underline{\mathfrak{N}} \\ & = L^i {}_i L^v \mathfrak{N} + t^j x {}_j \mathfrak{T}^{-v} \mathfrak{N} = L^1 | \cdot | L^p | t^1 | \cdot | t^q \frac{\begin{array}{c} {}_1 L^v \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline {}_p L^v \mathfrak{N}^{\cdot} \\ \hline x {}_1 \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline x {}_q \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \end{array}}{\begin{array}{c} {}_1 L^v \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline {}_p L^v \mathfrak{N}^{\cdot} \\ \hline x {}_1 \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \\ \hline \cdot \\ \hline x {}_q \mathfrak{T}^{-v} \mathfrak{N}^{\cdot} \end{array}} \end{aligned}$$

$$\det \frac{\begin{array}{c} v_{\mathfrak{N}} \\ \hline 1 \\ \cdot \\ \hline \end{array}}{\begin{array}{c} v_{\mathfrak{N}} \\ \hline p \\ \hline x_{-} \mathfrak{N} \\ \cdot \\ \hline x_{-} \mathfrak{N} \end{array}} = \underline{\gamma}^1 \times \underline{\gamma}^q \det {}^x T_v$$

$$\begin{aligned} {}^v \mathfrak{h}_j &= x_j {}^v \mathfrak{L} = x_j \mathfrak{T} {}^v \mathfrak{N} \\ &\quad \begin{array}{c} v_{\mathfrak{N}} \\ \hline 1 \\ \cdot \\ \hline \end{array} \quad \begin{array}{c} {}^v \mathfrak{L} \\ \hline 1 \\ \cdot \\ \hline \end{array} \\ \text{LHS} &= \underline{\gamma}^1 \times \underline{\gamma}^q \det \frac{\begin{array}{c} v_{\mathfrak{N}} \\ \hline p \\ \hline x_1 \mathfrak{L} \\ \cdot \\ \hline x_q \mathfrak{L} \end{array}}{\begin{array}{c} v_{\mathfrak{N}} \\ \hline p \\ \hline x_1 \mathfrak{T} {}^v \mathfrak{N} \\ \cdot \\ \hline x_q \mathfrak{T} {}^v \mathfrak{N} \end{array}} = \text{RHS} \end{aligned}$$