

$$D_{\underbrace{\triangle_\omega}_\omega} \underbrace{Z_{\triangle_\bullet}}_{\mathbb{C}^{|n|}} \ni \mathbf{1}$$

$$\zeta \overbrace{+^zG_w^{-|n|}\mathbf{1}}^w = \zeta +^zD_w^n \overbrace{\zeta + z}^w - 2z^w \mathbf{1}$$

$$\begin{aligned} \mathcal{Z} &= \mathfrak{t}_z {}^z B_z^{1/2} \mathfrak{t}_z \\ {}_+^o G_{\mathcal{Z}} &= \mathcal{Z} \mathfrak{t}_z^{-1} = \mathfrak{t}_z {}^z B_z^{1/2} = \overbrace{{}^z B_z^{1/2} \mathfrak{t}_z}^* = \overbrace{\mathfrak{t}_{z^z B_z^{-1/2}} {}^z B_z^{1/2}}^* = \overbrace{\mathfrak{t}_{z^z} {}^z B_z^{1/2}}^* = {}^z B_z^{1/2} \mathfrak{t}_{z^z} \\ {}_+^z G_z &= {}_+^o G_{\mathcal{Z}} {}^o G_{\mathcal{Z}} = \mathfrak{t}_{z^z} {}^z B_z^{1/2} {}^z B_z^{1/2} \mathfrak{t}_{z^z} = \mathfrak{t}_{z^z} {}^z B_z \mathfrak{t}_{z^z} \\ \overbrace{\zeta + z}^w - 2z^w {}_+^z G_w &= \zeta \mathfrak{t}_z \mathfrak{t}_{-w}^* \mathfrak{t}_{-2z^w} \mathfrak{t}_{z^w} {}^z B_w \mathfrak{t}_{w^z}^* = \zeta \mathfrak{t}_z \mathfrak{t}_{-w}^* \mathfrak{t}_{-z^w} {}^z B_w \mathfrak{t}_{w^z}^* \\ &= \overbrace{\zeta + z}^w - z^w {}^z B_w \stackrel{\text{L}\bar{\text{O}}\text{O}}{=} \overbrace{\zeta}^{w^z} - w^z = \zeta \\ \Rightarrow \zeta {}_+^z G_w^{-1} &= \overbrace{\zeta + z}^w - 2z^w \Rightarrow {}_+^z G_w^{-1} = \mathfrak{t}_z \mathfrak{t}_{-w}^* \mathfrak{t}_{-2z^w} = \mathfrak{t}_{\sim}^* \mathfrak{t}_{-w} \mathfrak{t}_{-z^w} \\ \Rightarrow \underline{{}_+^z G_w^{-1}} &= \underline{\zeta + z} \mathfrak{t}_{-w}^* = \zeta + {}^z B_w^{-1} \Rightarrow \det \underline{{}_+^z G_w^{-1}}^{-n} = \zeta + {}^z D_w^n \\ \zeta \overbrace{y^n \mathbf{1}}^w &= \det \zeta \underline{y}^{-n} \zeta y \mathbf{1} \Rightarrow \text{LHS} = \det \underline{{}_+^z G_w^{-1}}^{-n} \zeta {}_+^z G_w^{-1} \mathbf{1} = \zeta + {}^z D_w^n \overbrace{\zeta + z}^w - 2z^w \mathbf{1} \end{aligned}$$