

$$D_{\bigtriangledown^2_\omega} Z \triangleleft^\mu_{\bullet} \mathbb{C} \xleftarrow[\text{u-rep}]{{}_-K^\mu} G \ltimes D_{\bigtriangledown^2_\omega} Z \triangleleft^\mu_{\bullet} \mathbb{C}$$

$$\zeta|z \widehat{{}_{-K_g^\mu} \mathfrak{q}} = \zeta \widehat{{}_z g^{\mu zg} \mathfrak{q}} = {}^{\zeta z} \widehat{{}_z g^{|zg}} \mathfrak{q}$$

$${}_-K_g^\mu \widehat{{}_{\dot{g}}} \widehat{{}_{-K_{\dot{g}}} \mathfrak{q}} = {}_-K_{g\dot{g}}^\mu \mathfrak{q}$$

$${}^z \text{LHS} = {}^z \underline{g} \widehat{{}_{-K_{\dot{g}}}^\mu \mathfrak{q}} = {}^z \underline{g} \widehat{{}_z g} \widehat{{}_{zg} \mathfrak{q}} = {}^z \widehat{{}_z g} \widehat{{}_{zg} \mathfrak{q}} = {}^z \text{RHS}$$

$$\widehat{{}_{-K_g^\mu} \mathfrak{q}} \mathbin{\boxtimes} \widehat{{}_{-K_g^\mu} \mathfrak{q}} = \mathfrak{q} \mathbin{\boxtimes} \mathfrak{q}$$

$$\begin{aligned} \text{LHS} &= \int_{dz}^D {}^z \widehat{{}_{-K_g^\mu} \mathfrak{q}} \mathbin{\boxtimes} \widehat{{}_z K_z^\mu} \widehat{{}_{-K_g^\mu} \mathfrak{q}} = \int_{dz}^D \widehat{{}_z g} \widehat{{}_z g} \mathfrak{q} \mathbin{\boxtimes} \widehat{{}_z K_z^\mu} \widehat{{}_z g} \widehat{{}_z g} \mathfrak{q} \\ &= \int_{dz}^D {}^z g \mathfrak{q} \mathbin{\boxtimes} \widehat{{}_z \dot{g}} \widehat{{}_{-K_z^\mu}} \widehat{{}_z g} \widehat{{}_z g} \mathfrak{q} = \int_{dz}^D \widehat{{}_z g} \mathfrak{q} \mathbin{\boxtimes} \widehat{{}_z K_z^\mu} \widehat{{}_z g} \widehat{{}_z g} \mathfrak{q} = \text{RHS} \end{aligned}$$

$${}^z \mathfrak{q} = {}^z \mathcal{D}_w^\mu \mathfrak{q}$$

$$\overline{g}^1 \ltimes \mathcal{D}_w^\mu \mathfrak{q} = \mathcal{D}_{wg}^\mu \mathfrak{q}$$

$$\mathcal{D} = K^{\mathbb{C}}$$

$$\det {}^z \mathcal{D}_w = {}^z \Delta_w^p$$

$$B = K^{\mathbb{C}} \Rightarrow {}^z B_w^\mu = {}^z B_w^{-\mu}$$

$${}^z \underline{g} \widehat{{}_z g} B_{wg}^{-1} {}^w \underline{\dot{g}}^* = {}^z B_w^{-1}$$

$$\int_{dx}^D {}^z K_x \widehat{{}^x K_x^{-1}} {}^x K_w = {}^z B_w^{-1/2} \mathfrak{t}_{-w}^* C \mathfrak{t}_{-z} {}^z B_w^{-1/2}$$

$$\mathbb{1} \stackrel{\text{inv}}{\underset{B}{\triangleright}} \hat{B} \Rightarrow \left\{ \begin{array}{l} B_w^{-1} \mathbb{1} \\ w \in D \\ \mathbb{1} \in \mathbb{1} \end{array} \right\} \mathbb{C} \stackrel{\text{inv}}{\underset{G}{\triangleleft}} \overset{D}{\underset{\mathbb{1}}{\triangleright}} \hat{B}$$

$$g \ltimes \underbrace{B_w^{-1} \mathbb{1}}_{\in \mathbb{1}} = B_{wg^{-1}} \underbrace{w \underline{g}^{-1} \mathbb{1}}_{\in \mathbb{1}}$$

$$\int_{dx}^D z B_x^{-1} {}^x B_x {}^x B_z^{-1} = {}^0 \underline{g}^{-1} z \left( \int_{dx}^D {}^0 B_x^{-1} {}^x B_x {}^x B_0^{-1} \right) {}^0 \underline{g}^* z = C$$

$$\begin{aligned} \int_{dx}^D z B_x^{-1} {}^x B_x {}^x B_z^{-1} &= \int_{dx}^D {}^0 g B_x^{-1} {}^x B_x {}^x B_{0g}^{-1} = \int_{dx}^D {}^0 g B_{xg}^{-1} {}^{xg} B_{xg} {}^{xg} B_{0g}^{-1} \\ &= \int_{dx}^D {}^0 \underline{g}^{-1} {}^0 B_x^{-1} {}^x \underline{g}^* \overbrace{{}^x \underline{g}^{-1} {}^x B_x^{-1} {}^x \underline{g}^*}^{{}^x \underline{g}^{-1} {}^x B_x^{-1} {}^x \underline{g}^*} {}^x \underline{g}^{-1} {}^x B_0^{-1} {}^0 \underline{g}^* \\ &= \int_{dx}^D {}^0 \underline{g}^{-1} {}^0 B_x^{-1} {}^x \underline{g}^* {}^x B_x {}^x \underline{g}^{-1} {}^x B_0^{-1} {}^0 \underline{g}^* = {}^0 \underline{g}^{-1} \underbrace{\int_{dx}^D {}^0 B_x^{-1} {}^x B_x {}^x B_0^{-1} {}^0 \underline{g}^*}_{{}^0 \underline{g}^{-1} \int_{dx}^0 B_x^{-1} {}^x B_x {}^x B_0^{-1} {}^0 \underline{g}^*} \end{aligned}$$

$${}^{zg}\mathcal{D}_{wg} = {}^w\underline{\hat{g}}\, {}^z\mathcal{D}_w\, {}^z\underline{g} \in K^{\mathbb{C}}$$

$$\begin{array}{ccc} Z_{\bigtriangledown_{\sim}^{\mu}\mathbb{C}\mathbf{x}T^{-\nu}} & \xrightarrow{{}^z\mathcal{D}_w^{\mu}} & Z_{\bigtriangledown_{\sim}^{\mu}\mathbb{C}\mathbf{x}T^{-\nu}} \\ \uparrow {}^{zg^{\mu}}\underline{\hat{g}}^{-\nu} & & \downarrow {}^w\underline{\hat{g}}^{\mu}\, {}^w\underline{\hat{g}}^{\nu} \\ Z_{\bigtriangledown_{\sim}^{\mu}\mathbb{C}\mathbf{x}T^{-\nu}} & \xrightarrow{{}^{zg}\mathcal{D}_{wg}^{\mu}} & Z_{\bigtriangledown_{\sim}^{\mu}\mathbb{C}\mathbf{x}T^{-\nu}} \end{array}$$

$${}^o\underline{k} \in \mathbf{U}|K^{\mu}$$

$${}^z\mathcal{D}_z = {}^o\underline{\hat{g}}_z\, {}^o\underline{\hat{g}}_z$$

$${}^o\mathcal{D}_o = I$$

$$\text{LHS} = {}^o\underline{\hat{g}}_{zg}\, {}^o\underline{\hat{g}}_{zg} = {}^o\underline{k}\, {}^*\underline{\hat{g}}_z g I {}^o\underline{k}\, {}^o\underline{\hat{g}}_z g = \overbrace{{}^o\underline{k}\, {}^o\underline{\hat{g}}_z\, {}^zg}^* {}^o\underline{k}\, {}^o\underline{\hat{g}}_z\, {}^zg = {}^z\underline{\hat{g}}\, {}^o\underline{\hat{g}}_z\, {}^o\underline{k}\, {}^o\underline{\hat{g}}_z\, {}^zg = {}^z\underline{\hat{g}}\, {}^o\underline{\hat{g}}_z\, {}^o\underline{\hat{g}}_z\, {}^zg = \text{RHS}$$

$${}^D\bigtriangledown Z_{\bigtriangledown_{\sim}^{\mu}\mathbb{C}\mathbf{x}T^{-\nu}} \ni \mathfrak{q}$$

$$\mathfrak{q}\mathbf{x}\mathfrak{q} = \int\limits_{dz}^D {}^z\mathfrak{q}\, \mathbf{x}\, {}^z\mathfrak{q} = \int\limits_{dz}^D {}^z\mathfrak{q}\, \mathbf{x}\, {}^z\mathcal{D}_z\, {}^z\mathfrak{q} = \int\limits_{dz}^D {}^z\mathfrak{q}\, \mathbf{x}\, {}^o\underline{\hat{g}}_z\, {}^o\underline{\hat{g}}_z\, {}^z\mathfrak{q} = \int\limits_{dz}^D \underbrace{{}^o\underline{\hat{g}}_z\, {}^z\mathfrak{q}}_{} \underbrace{{}^o\underline{\hat{g}}_z\, {}^z\mathfrak{q}}_{} =$$

$$D_{\bigtriangledown_\omega^2} Z_{\bigtriangledown_\sim^\mu \mathbb{C} \boxtimes T^{-\nu}} \xleftarrow[\text{u-rep}]{\bowtie} G \bowtie D_{\bigtriangledown_\omega^2} Z_{\bigtriangledown_\sim^\mu \mathbb{C} \boxtimes T^{-\nu}}$$

$$\zeta^{|z|} \widehat{g_{TK}^{\nu\mu} \mathfrak{q}} = \zeta \widehat{z \underline{g}^{\nu z} g^{\mu z g} \mathfrak{q}} = z \underline{g}^{-\nu} \zeta^z \underline{g}^{|z g} \mathfrak{q}$$

$$\begin{aligned} g \bowtie \underline{g} \bowtie \mathfrak{q} &= \underline{g} \underline{g} \bowtie \mathfrak{q} \\ g \underset{\nu}{\bowtie} \widehat{\underline{g} \bowtie \mathfrak{q}} &= \underline{g} \underline{g} \underset{\nu}{\bowtie} \mathfrak{q} \end{aligned}$$

$${}^z \text{LHS} = {}^z \underline{g} \widehat{{}^z \underline{g} \bowtie \mathfrak{q}} = {}^z \underline{g} \underset{zg}{\underline{g}} \widehat{{}^z \underline{g} \underline{g}} \mathfrak{q} = {}^z \widehat{\underline{g} \underline{g}} {}^z \underline{g} \mathfrak{q} = {}^z \text{RHS}$$

$$\widehat{g \bowtie \mathfrak{q}} \star \widehat{g \bowtie \mathfrak{q}} = \mathfrak{q} \star \mathfrak{q}$$

$$\begin{aligned} \text{LHS} &= \int_{dz}^D {}^z \widehat{\underline{g} \bowtie \mathfrak{q}} \star {}^z \widehat{\mathcal{D}_z \underline{g} \bowtie \mathfrak{q}} = \int_{dz}^D \underbrace{{}^z \underline{g}}_{zg} \mathfrak{q} \star \widehat{{}^z \mathcal{D}_z \underline{g}} \widehat{{}^z \underline{g} \mathfrak{q}} \\ &= \int_{dz}^D {}^z \mathfrak{q} \star \widehat{{}^z \underline{g} \mathcal{D}_z {}^z \underline{g} \mathfrak{q}} = \int_{dz}^D \widehat{{}^z \mathfrak{q}} \star \widehat{{}^z \mathcal{D}_{zg} {}^z \underline{g} \mathfrak{q}} = \int_{dz}^D {}^z \mathfrak{q} \star \widehat{{}^z \mathcal{D}_z {}^z \mathfrak{q}} = \text{RHS} \end{aligned}$$