

$$I \in \begin{bmatrix} r+s \\ r \end{bmatrix}$$

$${}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I = \frac{\mathfrak{I} \in {}^r_{\mathbb{K}}_{r+s}}{\mathfrak{I}_I \in {}^r_{\mathbb{K}}_I \text{ inv}} \subset_{\text{off}} {}^r_{\mathbb{K}}_{r+s}$$

$$\pi \text{ off} \Rightarrow \mathbb{K}_r {}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I \subset_{\text{off}} {}^r_{\mathbb{K}}_s^\times$$

$${}^r_{\mathbb{C}} \mathbb{K}_{r+s} = \bigcup_I {}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I$$

$$\pi \text{ surj} \Rightarrow {}^r_{\mathbb{K}}_s^\times = \mathbb{K}_r {}^r_{\mathbb{C}} \mathbb{K}_{r+s} = \bigcup_I \mathbb{K}_r {}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I$$

$${}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I = \frac{\mathfrak{I}|\mathfrak{J} P_I}{\mathfrak{I} \in {}^r_{\mathbb{C}} \mathbb{K}_r}$$

$$\mathfrak{J} \in {}^r_{\mathbb{K}}_s \xrightarrow[\text{bij}] {\Phi_I} \mathbb{K}_r {}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I \ni \mathbb{K}_r \underline{1|\mathfrak{J}} P_I \sqsubset \mathbb{K}_{r+s}$$

$$\begin{cases} \mathbb{K}_r \underline{\mathfrak{I}|\mathfrak{J}} P_I & \in \mathbb{K}_r {}^r_{\mathbb{C}} \mathbb{K}_{r+s}^I \xrightarrow[\text{bij}] {\Phi_I^{-1}} {}^r_{\mathbb{K}}_s \ni \\ \mathbb{K}_r \mathfrak{I} & \end{cases} \underbrace{\begin{cases} \mathfrak{I}^{-1} \mathfrak{J} \\ \underline{\mathfrak{I} P_L}^{-1} \quad \underline{\mathfrak{J} P_L}^{-1} \end{cases}}_{r|s}$$

$$\Phi_I^{-1} \text{ well-def}$$

$$\mathfrak{N} \underline{\mathfrak{I}|\mathfrak{J}} P_I = \underline{\mathfrak{N} \mathfrak{I}|\mathfrak{N} \mathfrak{J}} P_I \mapsto \widehat{\mathfrak{N} \mathfrak{I}}^{-1} \underline{\mathfrak{N} \mathfrak{J}} = \mathfrak{I}^{-1} \mathfrak{N}^{-1} \mathfrak{J} = \mathfrak{I}^{-1} \mathfrak{J}$$

$$\Phi_I^{-1} \circ \Phi_I = \text{id} = \Phi_I \circ \Phi_I^{-1}$$

$$\begin{aligned}\Phi_I^{-1} \circ \Phi_I (\Delta) &= \Phi_I^{-1} \left(\mathbb{K}_r \underbrace{1|\Delta}_{\mathcal{P}_I} \right) = 1^{-1} \Delta = \Delta \\ \Phi_I \circ \Phi_I^{-1} \left(\mathbb{K}_r \underbrace{\Gamma|\Delta}_{\mathcal{P}_I} \right) &= \Phi_I \left(\Gamma^{-1} \Delta \right) = \mathbb{K}_r \underbrace{1|\Gamma^{-1} \Delta}_{\mathcal{P}_I} = \mathbb{K}_r \underbrace{\Gamma^{-1} \Gamma| \Delta}_{\mathcal{P}_I} = \mathbb{K}_r \underbrace{\Gamma|\Delta}_{\mathcal{P}_I}\end{aligned}$$

$$\begin{array}{ccc} {}^r \mathbb{K}_s^J & & \\ \downarrow {}_I \Phi^J & \searrow {}_I \Phi & \\ {}^r \mathbb{K}_s^I & \nearrow {}_J \Phi & \mathbb{K}_{r \mathbb{C}} {}^r \mathbb{K}_{r+s}^I \cap \mathbb{K}_{r \mathbb{C}} {}^r \mathbb{K}_{r+s}^J \end{array}$$

$${}_I \Phi^J (\Delta) = {}_J \Phi^{-1} \circ {}_I \Phi (\Delta) = {}_J \Phi^{-1} \left(\mathbb{K}_r \underbrace{1|\Delta}_{\mathcal{P}_I} \right) = \underbrace{\widehat{1|\Delta} P_I \bar{P}_J^{-1}}_{r|}^{-1} \underbrace{\widehat{1|\Delta} P_I \bar{P}_J^{-1}}_{|s}$$