

$$\begin{array}{ccc}
H \times_{\nu} N^{\pm} N & \ni & \sigma \\
\downarrow \nu & & \downarrow \\
H^{\pm} N & \ni & \nu \boxtimes \sigma \rangle^{H \times N}_{H \times N} \\
\downarrow & & \downarrow \nu \\
H \times N \sqcap^{\pm} N & \ni &
\end{array}$$

$$H^{\pm} N = \bigcup_{\nu \in H \times N \sqcap^{\pm} N} H \times_{\nu} N \stackrel{\pm}{\models} N$$

$$g \ltimes \nu \in N^{\pm} \xleftarrow{\quad} \underline{H \times H} \ltimes N^{\pm} \ni g:\nu$$

$$n^g \ltimes \nu = \overbrace{g^{-1}ng}^{\nu}$$

$$g \ltimes \underbrace{g \ltimes n}_{\nu} = \underbrace{gg \ltimes \nu}_{\nu}$$

$$n^g \ltimes \underbrace{g \ltimes \nu}_{\nu} = \overbrace{g^{-1}ng}^{\dot{g} \ltimes \nu} = \overbrace{\dot{g}^{-1}\underbrace{g^{-1}ng}_{\nu}\dot{g}}^{\nu} = \overbrace{\dot{g}\dot{g}^{-1}\underbrace{n}_{\nu}\dot{g}\dot{g}}^{\nu} = n^{\dot{g}\dot{g}} \ltimes \nu$$

$$N \underset{\text{ex}}{\triangleleft} H \times_{\nu} N = \frac{g \in H \times N}{g \ltimes \nu * \nu \in N^{\pm}} \triangleleft H \times N$$

$$n^m \ltimes \nu = \overbrace{m^{-1}nm}^{\nu} = m^{-\nu} n^{\nu} m^{\nu} * n^{\nu}$$

