

$\mathcal{P}_m \ni p_m$  Prädikat-Symbole

$$\text{Primformeln } \mathcal{P}\overline{O \cup X} = \frac{p_m t_1 \dots t_m}{p_m \in \mathcal{P}_m : t_i \in \overline{O \cup X}}$$

$$\text{Symbol alg } < \mathcal{P}\overline{O \cup X} | \neg : \# | \# > \begin{cases} p_m t_1 \dots t_m \\ \neg \\ \# \\ \# \\ \# \\ \# \end{cases}$$

$$1\text{-stellig} \quad \begin{cases} \neg & \text{non} & \neg A = \bar{A} \\ \wedge_x & x \in X & \text{Quantoren } \# = \begin{cases} \wedge_x \\ \vee_x \end{cases} \\ \vee_x & x \in X & \end{cases}$$

$$2\text{-stellig Junktoren} \quad \begin{cases} \wedge & \text{und} & \wedge AB = A \wedge B \\ \vee & \text{oder} & \vee AB = A \vee B \\ \rightarrow & \text{implies} & \rightarrow AB = A \rightarrow B \end{cases} \quad \# = \begin{cases} \wedge \\ \vee \\ \rightarrow \end{cases}$$

Formeln=ableitbar  $\overline{\mathcal{P}\overline{O \cup X}}$

Variablen=Zahlen  $F_0 = \underset{\text{null}}{0} : F_1 = \underset{\text{next}}{+1} : F_2 = \underset{\text{add}}{+} : F'_2 = \underset{\text{mult}}{\bullet} : P_2 = \underset{\text{gleich}}{=} : P'_2 = \underset{\text{kleiner}}{<}$

$$x < y \Rightarrow \bigwedge_z x + z < y + z : \text{ Formel } \rightarrow \underbrace{< xy}_{\text{prim}} \bigwedge_z \underbrace{< \underbrace{+xz}_{\text{term}} \underbrace{+yz}_{\text{term}}}_{\text{prim}}$$

Variablen=Mengen  $F_0 = \underset{\text{leer}}{\emptyset} : F_2 = \underset{\text{union}}{\cup} : F'_2 = \underset{\text{schnitt}}{\cap} : P_2 = \underset{\text{gleich}}{=} : P'_2 = \underset{\text{element}}{\in}$

$$X \neq Y \Rightarrow \overbrace{\bigvee_Z Z \in X \sqcup Y}^{\text{prim}} \vee \overbrace{\bigvee_W W \in Y \sqcup X}^{\text{prim}} : \text{ Formel } \rightarrow \neg \underbrace{= XY}_{\text{prim}} \vee \bigvee_Z \wedge \underbrace{\in ZX}_{\text{prim}} \neg \underbrace{\in ZY}_{\text{prim}} \bigvee_W \wedge \underbrace{\in WY}_{\text{prim}} \neg \underbrace{\in WX}_{\text{prim}}$$

$$\bigwedge A \in \overline{\mathcal{PO} \cup X} \bigvee_{\text{Trg}}^{\text{eind}} |A| \subset X \text{ finit} \quad \begin{cases} |p_m t_1 \cdot t_m| = |t_1| \cup \dots \cup |t_n| \\ |\bar{A}| = |A| \\ |A \sharp B| = |A| \cup |B| \\ |\sharp_x A| = |A| \llcorner x = \frac{y \in |A|}{y \neq x} \end{cases}$$

$$\text{fin subset } Y \in 2_0^X \ni \begin{cases} \widetilde{p_m t_1 \cdot t_m} = |t_1| \cup \dots \cup |t_n| \\ \widetilde{\sharp} A | Y = Y \\ \widetilde{\sharp} \underbrace{A_1 | Y_1 : A_2 | Y_2}_{x} = Y_1 \cup Y_2 \\ \widetilde{\sharp} A | Y = Y \llcorner x \end{cases}$$

$$\xrightarrow[\text{Satz}]{\text{Rek}} \bigvee_* |S_n A_1 \cup \dots \cup A_n| = \widetilde{S} \underbrace{A_1 : |A_1| \cup \dots \cup |A_n|}_{A_n}$$

$$\text{Formel } A \text{ Satz} \Leftrightarrow |A| = \emptyset$$

$$\neg \bigwedge_X \in XY \text{ kein Mengen-Satz}$$

$$|\neg \bigwedge_X \in XY| = |\bigwedge_x \in XY| = |\in XY| \llcorner X = |X| \cup |Y| \llcorner X = X \cup Y \llcorner X = Y$$

$$\neg \bigwedge_x \neg \bigvee_y < yx \text{ Zahlen-Satz}$$

$$\begin{aligned} |\neg \bigwedge_x \neg \bigvee_y < yx| &= |\bigwedge_x \neg \bigvee_y < yx| = |\neg \bigvee_y < yx| \llcorner x = |\bigvee_y < yx| \llcorner x \\ &= |< yx| \llcorner y \llcorner x = |y| \cup |x| \llcorner y \llcorner x = y \cup x \llcorner y \llcorner x = \emptyset \end{aligned}$$

$$\bigwedge A \in \overline{\mathcal{PO} \cup X} \bigvee_{\text{rang}}^{\text{eind}} \text{rg } A \in \mathbb{N} \left\{ \begin{array}{l} \text{rg } p_m t_1 \cdots t_m = 0 \\ \text{rg } \bar{A} = 1 + \text{rg } A \\ \text{rg } \sharp_x A = 1 + \text{rg } A \\ \text{rg } A \sharp B = 1 + \text{rg } A + \text{rg } B \end{array} \right.$$

$$k \in \mathbb{N} \Leftrightarrow \left\{ \begin{array}{l} \widetilde{p_m t_1 \cdots t_m} = 0 \\ \widetilde{\sharp} \begin{bmatrix} A & k \end{bmatrix} = 1 + k \\ \widetilde{\sharp} \begin{bmatrix} A & k \end{bmatrix} = 1 + k \\ \sharp \underbrace{A_1 | k_1}_{\sharp} \underbrace{A_2 | k_2}_{\sharp} = 1 + k_1 + k_2 \end{array} \right.$$

$$\xrightarrow[\text{Satz}]{\text{Rek}} \bigvee_* \text{rg } S_n A_1 \cdots A_n = \widetilde{S}_n \underbrace{A_1| \text{rg } A_1 \cdots A_n | \text{rg } A_n}$$