

$$G^\pi \ni \rho$$

$$\text{Diagram 1} = \int da \, a^- \text{Diagram 2}$$

$$^a \overline{k^\pi}^b = \int_{db} {}^a k_b^\pi {}^b$$

$$\int da \, {}^a \bar{k}_b^\pi {}^a k_c^\pi = {}^b \delta_c$$

$$G_-^\pi \xleftarrow[K \text{ inv}]{\mathcal{I}} H^\pi K \triangle_2 \mathbb{C}$$

$${}^u\overline{k^{\varrho}\gamma} = {}^uk\gamma$$

$$\mathcal{I} \underbrace{k^{\varrho}} = k^{\pi} \mathcal{I} \mathcal{I}$$

$$\gamma_{\pi} \bowtie \gamma = \underbrace{\mathcal{I}\gamma}_{\pi} \bowtie \underbrace{\mathcal{I}\gamma}_{\pi}$$

$${}^a\overline{\mathcal{I}\gamma} = \int_{du}^{H\lrcorner K} {}^a\mathcal{I}_u{}^u\gamma$$

$${}^a\mathcal{I}_{uk^{-1}} = \int \frac{db}{db} {}^ak_b^\pi {}^b\mathcal{I}_u$$

$$\begin{aligned} \int_{du}^{H \nabla K} {}^a \mathcal{I}_{uk^{-1}} {}^u \gamma &= \int_{dv}^{H \nabla K} {}^a \mathcal{I}_v {}^{vk} \gamma = \int_{dv}^{H \nabla K} {}^a \mathcal{I}_v {}^v \overline{k^{\circ} \gamma} = {}^a \overline{\mathcal{I} k^{\circ} \gamma} \\ &= {}^a \overline{k^{\pi} \mathcal{I} \gamma} = \int_{db} {}^a k_b^{\pi} {}^b \overline{\mathcal{I} \gamma} = \int_{db} {}^a k_b^{\pi} \int_{du}^{H \nabla K} {}^b \mathcal{I}_u {}^u \gamma = \int_{du}^{H \nabla K} \int_{db} {}^a k_b^{\pi} {}^b \mathcal{I}_u {}^u \gamma \end{aligned}$$

$${}^u\mathcal{I}_v = \int_{da} {}^a\bar{\mathcal{I}}_u {}^a\mathcal{I}_v = \int_{da} {}^u\mathcal{I}_a {}^a\mathcal{I}_v$$

$$\mathfrak{I}_{\pi} \bowtie \mathfrak{I} = \int_{du}^{H\mathfrak{I}K} \int_{dv}^{H\mathfrak{I}K} {}^u\overline{\mathfrak{I}} {}^u\mathcal{I}_v {}^v\mathfrak{I}$$

$$\text{LHS} = \mathcal{I}\mathfrak{I} \bowtie \mathcal{I}\mathfrak{I} = \int_{da} {}^a\overline{\mathcal{I}}\mathfrak{I} {}^a\widehat{\mathcal{I}\mathfrak{I}} = \int_{da} \int_{du}^{H\mathfrak{I}K} \overline{{}^a\mathcal{I}_u} {}^u\mathfrak{I} \int_{dv}^{H\mathfrak{I}K} {}^a\mathcal{I}_v {}^v\mathfrak{I} = \int_{du}^{H\mathfrak{I}K} {}^u\overline{\mathfrak{I}} \int_{dv}^{H\mathfrak{I}K} {}^v\mathfrak{I} \int_{da} {}^a\overline{\mathcal{I}_u} {}^a\mathcal{I}_v = \text{RHS}$$

$${}^{uk}\mathcal{I}_{vk} = {}^u\mathcal{I}_v$$

$$\begin{aligned} {}^{uk^{-1}}\mathcal{I}_{vk^{-1}} &= \int_{da} {}^a\overline{\mathcal{I}}_{{}^{uk^{-1}}} {}^a\mathcal{I}_{vk^{-1}} = \overline{\int_{da} \int_{db} {}^a\overline{k_b^{\pi}} \mathcal{I}_u \int_{dc} {}^a\overline{k_c^{\pi}} {}^c\mathcal{I}_v} \\ &= \int_{da} \int_{db} {}^a\overline{k_b^{\pi}} {}^b\overline{\mathcal{I}_u} \int_{dc} {}^a\overline{k_c^{\pi}} {}^c\mathcal{I}_v = \int_{db} \int_{dc} \int_{da} \frac{{}^a\overline{k_b^{\pi}} {}^a\overline{k_c^{\pi}}}{2} \left(= {}^b\overline{\delta_c} \right) {}^b\overline{\mathcal{I}_u} {}^c\mathcal{I}_v = \int_{db} {}^b\overline{\mathcal{I}_u} {}^b\mathcal{I}_v = {}^u\mathcal{I}_v \end{aligned}$$

$${}^u\widehat{\mathcal{I}_o} = {}^u\mathcal{I}_o = \int_{da} {}^u\mathcal{I}_a {}^a\mathcal{I}_o$$

$$\bigwedge^h_H {}^{uh}\mathcal{I}_o = {}^u\mathcal{I}_o$$

$${}^{uh}\mathcal{I}_o = {}^{uh}\mathcal{I}_{oh} = {}^u\mathcal{I}_o$$

$$v = ok = o\acute{k} \Rightarrow {}^u\mathcal{I}_v = {}^{uk^{-1}}\mathcal{I}_o = {}^{u/v}\mathcal{I}_o$$

$${}^u\mathcal{I}_v = {}^u\mathcal{I}_{ok} = {}^{uk^{-1}}\mathcal{I}_o$$

$$v = ok = o\acute{k} \Rightarrow \acute{k} = hk \Rightarrow u\acute{k}^{-1} = u\acute{k}^{-1}h^{-1} \Rightarrow {}^{u\acute{k}^{-1}}\mathcal{I}_o = {}^{uk^{-1}h^{-1}}\mathcal{I}_o = {}^{uk^{-1}}\mathcal{I}_o$$

$$^u\overline{\mathcal{I}_o\ast \mathfrak{I}}=\int_{dk}^K\, ^{uk^{-1}}\mathcal{I}_o\, ^{ok}\mathfrak{I}_{\, v=ok}=\int_{dv}^{H^{\neg}K}\, ^u\mathcal{I}_v\, ^v\mathfrak{I}$$

$$\mathfrak{I}\overline{\underbrace{\mathcal{I}_o\ast \mathfrak{I}}}= \mathfrak{I}\overline{\mathfrak{I}}_{\pi}\mathfrak{I}$$

$$\text{LHS} \, = \, \int_{du}^{H^{\neg}K} \, ^{u\bar{}}\overline{^u\mathcal{I}_o\ast \mathfrak{I}} = \int_{du}^{H^{\neg}K} \, ^{u\bar{}}\int_{dv}^{H^{\neg}K} \, ^u\mathcal{I}_v\, ^v\mathfrak{I} = \int_{du}^{H^{\neg}K} \int_{dv}^{H^{\neg}K} \, ^{u\bar{}}\, ^u\mathcal{I}_v\, ^v\mathfrak{I} = \, \text{RHS}$$

$$^u\mathcal{I}_o=H^{\frac{u}{\lambda}}_{\lambda}K\int_{H^{\frac{\sharp}{\sharp}}K}^{d\lambda}\mathcal{I}_o^{\lambda}$$

$$\mathcal{I}_o^{\lambda}=\int_{du}^{H^{\neg}K}\overline{H^{\frac{u}{\lambda}}_{\lambda}K}\, ^u\mathcal{I}_o$$