

$$\text{unit alg } \mathbb{C}\mathbb{D} \ni \mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2 = \mathbb{C} \frac{E_+ = E:E_- = F:q^h}{EF - FE = E_+ \rtimes E_- = \frac{q^h - q^{-h}}{q - q^{-1}}: \quad q^h E q^{-h} = q^2 E: \quad q^h F q^{-h} = q^{-2} F} \text{ relations}$$

$$q^h = \frac{q}{0} \bigg| \frac{0}{q^{-1}}$$

$$EF - FE = E_+ \rtimes E_- = \frac{q^h - q^{-h}}{q - q^{-1}}$$

$$\begin{cases} q^h E q^{-h} &= q^2 E \\ q^h F q^{-h} &= q^{-2} F \\ q^h E_{\pm} q^{-h} &= q^{\pm 2} E_{\pm} \end{cases}$$

$$\mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2 \rtimes \mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2 \xleftarrow{\Delta} \mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2$$

$$K = q^{h/2}$$

$$\Delta E^{\pm} = E_{\pm} \rtimes q^{h/2} + q^{-h/2} \rtimes E_{\pm}$$

$$\Delta q^h = q^h \rtimes q^h$$

$$\Delta E = E \rtimes K + K^{-1} \rtimes E$$

$$\Delta F = F \rtimes K + K^{-1} \rtimes F$$

$$\Delta K = K \rtimes K$$

$$\mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2 \xrightarrow[\text{antipode}]{S} \mathbb{C}_{\mathbb{N}}\mathfrak{N}_{\mathfrak{E}}^2\mathbb{C}_2$$

$$\begin{cases} SE &= -qE \\ SF &= -q^{-1}F \\ SK &= K^{-1} \end{cases} \begin{cases} SE_{\pm} &= -q^{\pm}E_{\pm} \\ Sq^h &= q^{-h} \end{cases}$$

$$\text{Majid Ueno SchmII} \begin{cases} KE = qEK & KF = q^{-1}FK \\ E \rtimes F &= \frac{K^2 - K^{-2}}{q - q^{-1}} \\ \Delta E = E \rtimes K + K^{-1} \rtimes E & \Delta F = F \rtimes K + K^{-1} \rtimes F \\ SE = -qE & SF = -q^{-1}F \end{cases}$$

$$\text{Kassel Shari SchmI} \left\{ \begin{array}{ll} \mathbb{K}\mathbb{E} = q^2\mathbb{E}\mathbb{K} & \mathbb{K}\mathbb{F} = q^{-2}\mathbb{F}\mathbb{K} \\ \mathbb{E} \rtimes \mathbb{F} & = \frac{\mathbb{K} - \mathbb{K}^{-1}}{q - q^{-1}} \\ \Delta\mathbb{E} = \mathbb{E}\mathbf{z}\mathbb{K} + \mathbb{I}\mathbf{z}\mathbb{E} & \Delta\mathbb{F} = \mathbb{F}\mathbf{z}\mathbb{I} + \mathbb{K}^{-1}\mathbf{z}\mathbb{F} \\ S\mathbb{E} = -\mathbb{E}\mathbb{K}^{-1} & S\mathbb{F} = -\mathbb{K}\mathbb{F} \end{array} \right.$$

$$\text{Zhang} \left\{ \begin{array}{ll} \mathcal{K}\mathcal{E} = q^2\mathcal{E}\mathcal{K} & \mathcal{K}\mathcal{F} = q^{-2}\mathcal{F}\mathcal{K} \\ \mathcal{E} \rtimes \mathcal{F} & = \frac{\mathcal{K} - \mathcal{K}^{-1}}{q - q^{-1}} \\ \Delta\mathcal{E} = \mathcal{E}\mathbf{z}\mathcal{I} + \mathcal{K}\mathbf{z}\mathcal{E} & \Delta\mathcal{F} = \mathcal{F}\mathbf{z}\mathcal{K}^{-1} + \mathcal{I}\mathbf{z}\mathcal{F} \\ S\mathcal{E} = -\mathcal{K}^{-1}\mathcal{E} & S\mathcal{F} = -\mathcal{F}\mathcal{K} \end{array} \right.$$

$$\left\{ \begin{array}{l} \mathbb{E} = EK = \mathcal{F} \\ \mathbb{F} = K^{-1}F = \mathcal{E} \\ \mathbb{K} = K^2 = \mathcal{K}^{-1} \end{array} \right.$$